



JEE Main Online Exam 2026

Questions & Solution
22nd January 2026 | Morning

MATHEMATICS

SECTION-A

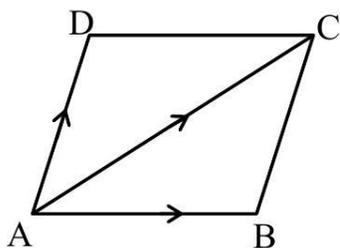
1. Let $\overline{AB} = 2\hat{i} + 4\hat{j} - 5\hat{k}$ and $\overline{AD} = \hat{i} + 2\hat{j} + \lambda\hat{k}$, $\lambda \in \mathbf{R}$. Let the projection of the vector $\vec{v} = \hat{i} + \hat{j} + \hat{k}$ on the diagonal \overline{AC} of the parallelogram ABCD be of length one unit. If α, β , where $\alpha > \beta$, be the roots of the equation $\lambda^2 x^2 - 6\lambda x + 5 = 0$, then $2\alpha - \beta$ is equal to
- (1) 1 (2) 4 (3) 3 (4) 6

Ans. [3]

Sol.

$$\overline{AC} = 3\hat{i} + 6\hat{j} + (\lambda - 5)\hat{k}$$

$$\widehat{AC} = 1 \Rightarrow 3 + 6 + \lambda - 5 = \sqrt{9 + 36 + (\lambda - 5)^2}$$



$$\Rightarrow \lambda^2 + 8\lambda + 16 = \lambda^2 - 10\lambda + 70$$

$$\Rightarrow \lambda = \frac{54}{18} = 3$$

$$\therefore \text{Quadratic : } 9x^2 - 18x + 5 = 0 \Rightarrow x = \frac{1}{3}, \frac{5}{3}$$

$$\therefore 2\alpha - \beta = \frac{10 - 1}{3} = 3$$

2. Let the relation R on the set $M = \{1, 2, 3, \dots, 16\}$ be given by

$$R = \{(x, y) : 4y = 5x - 3, x, y \in M\}.$$

Then the minimum number of elements required to be added in R, in order to make the relation symmetric, is equal to

- (1) 1 (2) 2 (3) 4 (4) 3

Ans. [2]

Sol.

$$R = \{(3, 3), (7, 8), (11, 13)\}$$

to make it symmetric $(8, 7), (13, 11)$ must be added.

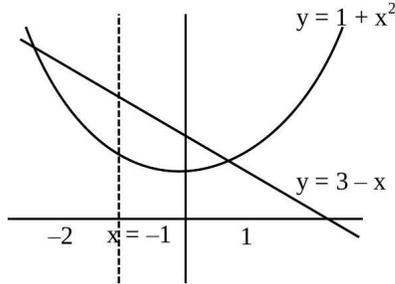
3. Let the line $x = -1$ divide the area of the region $\{(x, y) : 1 + x^2 \leq y \leq 3 - x\}$ in the ratio $m : n, \gcd(m, n) = 1$.

Then $m + n$ is equal to

- (1) 25 (2) 28 (3) 26 (4) 27

Ans. [4]

Sol.



$$\frac{m}{n} = \frac{\int_{-1}^1 [(3-x) - (1+x^2)] dx}{\int_{-2}^{-1} [(3-x) - (1+x^2)] dx} = \frac{20}{7}$$

$$\therefore m + n = 20 + 7 = 27$$

4. Two distinct numbers a and b are selected at random from $1, 2, 3, \dots, 50$. The probability, that their product ab is divisible by 3, is

- (1) $\frac{561}{1225}$ (2) $\frac{664}{1225}$ (3) $\frac{272}{1225}$ (4) $\frac{8}{25}$

Ans. [2]

Sol. Req. probability = $1 - (\text{product not divisible by } 3)$

Multiple of 3 = 16

Not multiple of 3 = 34

$$= 1 - \frac{{}^{34}C_2}{{}^{50}C_2} = \frac{664}{1225}$$

5. Let $f(x) = x^{2025} - x^{2000}, x \in [0, 1]$ and the minimum value of the function $f(x)$ in the interval $[0, 1]$ be $(80)^{80} (n)^{-81}$. Then n is equal to

- (1) -81 (2) -40 (3) -41 (4) -80

Ans. [1]

Sol. $f(x) = x^{2025} - x^{2000}$

$$f'(x) = 0 \Rightarrow x = \left(\frac{2000}{2025}\right)^{1/25} = \alpha \text{ (say)}$$

$$\therefore f(0) = 0, f(1) = 0, f(\alpha) = \left(\frac{80}{81}\right)^{80} \cdot \frac{-1}{81} = 80^{80} \cdot (-81)^{-81}$$

6. Let $P(\alpha, \beta, \gamma)$ be the point on the line $\frac{x-1}{2} = \frac{y+1}{-3} = z$ at a distance $4\sqrt{14}$ from the point $(1, -1, 0)$ and nearer to the origin. Then the shortest distance, between the lines $\frac{x-\alpha}{1} = \frac{y-\beta}{2} = \frac{z-\gamma}{3}$ and $\frac{x+5}{2} = \frac{y-10}{1} = \frac{z-3}{1}$, is equal to
- (1) $7\sqrt{\frac{5}{4}}$ (2) $4\sqrt{\frac{7}{5}}$ (3) $4\sqrt{\frac{5}{7}}$ (4) $2\sqrt{\frac{7}{4}}$

Ans. [2]

Sol. Let $P(2\lambda + 1, -3\lambda - 1, \lambda)$

Then $4\lambda^2 + 9\lambda^2 + \lambda^2 = 16 \cdot 14 \Rightarrow \lambda = \pm 4 \Rightarrow -4$ (nearer to origin)

$\therefore P(-7, 11, -4)$

$$\therefore \text{Shortest distance} = \frac{\begin{vmatrix} 2 & -1 & 7 \\ 1 & 2 & 3 \\ 2 & 1 & 1 \end{vmatrix}}{\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 3 \\ 2 & 1 & 1 \end{vmatrix}}$$

$$= \frac{28}{\sqrt{1+25+9}} = \frac{4\sqrt{7}}{\sqrt{5}}$$

7. If a random variable x has the probability distribution

x	0	1	2	3	4	5	6	7
p(x)	0	2k	k	3k	2k ²	2k	k ² + k	7k ²

then $P(3 < x \leq 6)$ is equal to

- (1) 0.34 (2) 0.22 (3) 0.64 (4) 0.33

Ans. [4]

Sol. $\sum P(x_i) = 1$

$$\Rightarrow 9k + 10k^2 = 1$$

$$\Rightarrow 10k^2 + 9k - 1 = 0 \Rightarrow k = \frac{1}{10}$$

$$P(3 < x \leq 6) = 3k + 3k^2$$

$$= \frac{3}{10} + \frac{3}{100} = 0.33$$

$$= 0.33$$

8. The number of distinct real solutions of the equation $x|x+4| + 3|x+2| + 10 = 0$ is

- (1) 3 (2) 1 (3) 0 (4) 2

Ans. [2]

Sol. **Case I** $x < -4$

$$x(-(x+4)) + 3(-(x+2)) + 10 = 0$$

$$x^2 + 7x - 4 = 0$$

$$\Rightarrow x = -\frac{7 + \sqrt{65}}{2} \text{ or } -\frac{7 - \sqrt{65}}{2}$$

Case II $-4 \leq x < -2$

$$x(x+4) + 3(-(x+2)) + 10 = 0$$

$$x^2 + x + 4 = 0$$

$D < 0$ No solution

Case III $x \geq -2$

$$x(x+4) + 3(x+2) + 10 = 0$$

$$x^2 + 7x + 16 = 0$$

$D < 0$ No solution

\Rightarrow No. of solution = 1.

9. Let $f: [1, \infty) \rightarrow \mathbf{R}$ be a differentiable function, If $6 \int_1^x f(t) dt = 3xf(x) + x^3 - 4$ for all $x \geq 1$, then the value of $f(2) - f(3)$ is
- (1) -4 (2) -3 (3) 4 (4) 3

Ans. [4]

Sol. $6 \int_1^x f(t) dt = 3xf(x) + x^3 - 4$

Diff. both side

$$6f(x) = 3xf'(x) + 3f(x) + 3x^2$$

$$3f(x) = 3xf'(x) + 3x^2$$

$$x \frac{dy}{dx} - y = -x^2$$

$$\frac{x \frac{dy}{dx} - y}{x^2} = -1$$

$$\Rightarrow \frac{d}{dx} \left(\frac{y}{x} \right) = -1$$

$$\frac{y}{x} = -x + C$$

$$\Rightarrow f(x) = -x^2 + Cx$$

$$\text{at } x=1, y=1 \Rightarrow C=2$$

$$f(x) = -x^2 + 2x$$

$$f(2) - f(3) = 3$$

10. If the line $\alpha x + 2y = 1$, where $\alpha \in \mathbf{R}$, does not meet the hyperbola $x^2 - 9y^2 = 9$, then a possible value of α is:
- (1) 0.6 (2) 0.8 (3) 0.5 (4) 0.7

Ans. [2]

Sol. $y = \frac{1 - \alpha x}{2}$

Put this in equation of hyperbola

$$\therefore x^2 - 9\left(\frac{1 - \alpha x}{2}\right)^2 = 9$$

$$(4 - 9\alpha^2)x^2 + 18\alpha x - 45 = 0$$

\therefore line does not intersect hyperbola

$$\therefore D < 0$$

$$\Rightarrow \alpha^2 - \frac{5}{9} > 0$$

$$\Rightarrow \alpha \in \left(-\infty, -\frac{\sqrt{5}}{3}\right) \cup \left(\frac{\sqrt{5}}{3}, \infty\right)$$

Here $\frac{\sqrt{5}}{3} \approx 0.74$

11. If the image of the point $P(1, 2, a)$ in the line $\frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$ is $Q(5, b, c)$, then $a^2 + b^2 + c^2$ is equal

to

(1) 293

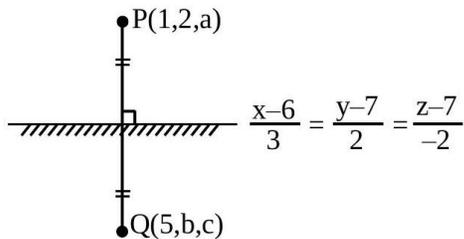
(2) 264

(3) 298

(4) 283

Ans. [3]

Sol.



Point $M \equiv \left(3, \frac{b}{2} + 1, \frac{c+a}{2}\right)$ satisfies the line

$$\frac{3-6}{3} = \frac{\frac{b}{2} + 1 - 7}{2} = \frac{\frac{c+a}{2} - 7}{-2}$$

$$-1 = \frac{b-12}{4} = \frac{c+a-14}{-4}$$

$$\Rightarrow b = 8 \dots(1) \text{ \& } c + a = 18 \dots(2)$$

Now $PQ \perp L$

$$\Rightarrow (4i + (b-2)j + (c-a)k) \cdot (3i + 2j - 2k) = 0$$

$$\Rightarrow 12 + 2(b-2) - 2(c-a) = 0$$

$$\Rightarrow 6 + (b-2) - (c-a) = 0$$

$$\Rightarrow b - c + a + 4 = 0$$

$$\Rightarrow 8 - c + a + 4 = 0$$

$$\Rightarrow c - a = 12 \quad \dots(3)$$

From (2) & (3)

$$c = 15 \text{ \& } a = 3$$

$$\text{So } a^2 + b^2 + c^2 = 9 + 64 + 225 = 298$$

12. Let the set of all values of r , for which the circles $(x+1)^2 + (y+4)^2 = r^2$ and $x^2 + y^2 - 4x - 2y - 4 = 0$ intersect at two distinct points be the interval (α, β) . Then $\alpha\beta$ is equal to

- (1) 25 (2) 20 (3) 21 (4) 24

Ans. [1]

Sol. $(x-2)^2 + (y-1)^2 = 3^2$ & $(x+1)^2 + (y+4)^2 = r^2$

$$|r_1 - r_2| < c_1 c_2 < r_1 + r_2$$

$$|r-3| < \sqrt{(2+1)^2 + (1+4)^2} < r+3$$

$$|r-3| < \sqrt{34} \text{ \& } r+3 > \sqrt{34}$$

$$-\sqrt{34} < r-3 < \sqrt{34} \text{ \& } r > \sqrt{34} - 3$$

$$\text{i.e. } r = (3 - \sqrt{34}, 3 + \sqrt{34}) \cap (\sqrt{34} - 3, \infty)$$

$$\text{i.e. } r \in (\sqrt{34} - 3, \sqrt{34} + 3)$$

$$\therefore \alpha\beta = (\sqrt{34} - 3)(\sqrt{34} + 3)$$

$$= 34 - 9 = 25$$

13. If $A = \begin{bmatrix} 2 & 3 \\ 3 & 5 \end{bmatrix}$, then the determinant of the matrix $(A^{2025} - 3A^{2024} + A^{2023})$ is

- (1) 28 (2) 12 (3) 24 (4) 16

Ans. [4]

Sol. $A = \begin{bmatrix} 2 & 3 \\ 3 & 5 \end{bmatrix} \Rightarrow A^2 = \begin{bmatrix} 13 & 21 \\ 21 & 34 \end{bmatrix}$

$$|A^{2025} - 3A^{2024} + A^{2023}|$$

$$= |A^{2023} (A^2 - 3A + I)|$$

$$= |A|^{2023} |A^2 - 3A + I|$$

$$= 1 \cdot \begin{vmatrix} 8 & 12 \\ 12 & 20 \end{vmatrix} = 160 - 144 = 16$$

14. If the domain of the function $f(x) = \sin^{-1}\left(\frac{5-x}{3+2x}\right) + \frac{1}{\log_e(10-x)}$ is $(-\infty, \alpha] \cup [\beta, \gamma) - \{\delta\}$, then

$6(\alpha + \beta + \gamma + \delta)$ is equal to

- (1) 70 (2) 66 (3) 67 (4) 68

Ans. [1]

Sol. $-1 \leq \frac{5-x}{2x+3} \leq 1$ & $10-x > 0, 10-x \neq 1$

$$\left| \frac{5-x}{2x+3} \right| \leq 1 \text{ \& } x < 10 \text{ \& } x \neq 9$$

$$(5-x)^2 - (2x+3)^2 \leq 0 \text{ \& } x < 10 \text{ \& } 4x \neq 9$$

$$(x+8)(3x-2) \geq 0 \text{ \& } x < 10 \text{ \& } x \neq 9$$

$$\Rightarrow (-\infty, -8] \cup \left[\frac{2}{3}, 10 \right) - \{9\}$$

$$\Rightarrow 6(\alpha + \beta + \gamma + \delta) = 6\left(-8 + \frac{2}{3} + 10 + 9\right) = 70$$

15. The value of $\int_{-\pi/2}^{\pi/2} \left(\frac{1}{[x]+4} \right) dx$, where $[\cdot]$ denotes the greatest integer function, is

(1) $\frac{1}{60}(21\pi - 1)$

(2) $\frac{1}{60}(\pi - 7)$

(3) $\frac{7}{60}(3\pi - 1)$

(4) $\frac{7}{60}(\pi - 3)$

Ans. [3]

Sol. $I = \int_{-\pi/2}^{\pi/2} \frac{1}{[x]+4} dx$

$$\begin{aligned} I &= \int_{-\pi/2}^{-1} \frac{dx}{2} + \int_{-1}^0 \frac{dx}{3} + \int_0^1 \frac{dx}{4} + \int_1^{\pi/2} \frac{dx}{5} \\ &= \frac{1}{2} \left(-1 + \frac{\pi}{2} \right) + \frac{1}{3}(1) + \frac{1}{4}(1) + \left(\frac{\pi}{2} - 1 \right) \frac{1}{5} \\ &= \frac{7\pi}{20} - \frac{7}{60} = \frac{7}{60}(3\pi - 1) \end{aligned}$$

16. The coefficient of x^{48} in $(1+x) + 2(1+x)^2 + 3(1+x)^3 + \dots + 100(1+x)^{100}$ is equal to :

(1) $100 \cdot {}^{100}C_{49} - {}^{100}C_{50}$

(2) ${}^{100}C_{50} + {}^{101}C_{49}$

(3) $100 \cdot {}^{100}C_{49} - {}^{100}C_{48}$

(4) $100 \cdot {}^{101}C_{49} - {}^{101}C_{50}$

Ans. [4]

Sol. Let $1+x=r$

$$\therefore S = 1 \cdot r + 2 \cdot r^2 + 3 \cdot r^3 + \dots + 100r^{100} \dots (1)$$

$$rS = 1 \cdot r^2 + 2 \cdot r^3 + \dots + 99r^{100} + 100r^{101} \dots (2)$$

(1) - (2) gives

$$S = -\frac{(1+x)^{101}}{x^2} + \frac{(x+1)}{x^2} + \frac{100(1+x)^{101}}{x}$$

$$\therefore \text{coefficient } x^{48} \text{ in } S$$

$$= -\text{coefficient of } x^{48} \text{ in } \frac{(1+x)^{101}}{x^2} + 100 \cdot \text{Coefficient of } x^{48} \text{ in } \frac{(1+x)^{101}}{x}$$

$$= 100 \cdot {}^{101}C_{49} - {}^{101}C_{50}$$

17. If the chord joining the points $P_1(x_1, y_1)$ and $P_2(x_2, y_2)$ on the parabola $y^2 = 12x$ subtends a right angle at the vertex of the parabola, then $x_1x_2 - y_1y_2$ is equal to
(1) 288 (2) 280 (3) 284 (4) 292

Ans. [1]

Sol. $(x_1, y_1) = (3t_1^2, 6t_1)$ & $(x_2, y_2) = (3t_2^2, 6t_2)$

$$t_1t_2 = -4$$

$$x_1x_2 = 9(t_1t_2)^2, y_1y_2 = 36t_1t_2$$

$$x_1x_2 - y_1y_2 = 9(16) - 36(-4)$$

$$= 144 + 144$$

$$= 288$$

18. The number of solutions of $\tan^{-1}4x + \tan^{-1}6x = \frac{\pi}{6}$, where $-\frac{1}{2\sqrt{6}} < x < \frac{1}{2\sqrt{6}}$ is equal to

(1) 3

(2) 0

(3) 1

(4) 2

Ans. [3]

Sol. $\tan^{-1}4x + \tan^{-1}6x = \frac{\pi}{6}$

$$\Rightarrow \tan^{-1}\left(\frac{4x+6x}{1-24x^2}\right) = \frac{\pi}{6}$$

$$\Rightarrow \frac{10x}{1-24x^2} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow 24x^2 + 10\sqrt{3}x - 1 = 0$$

$$x = \frac{-10\sqrt{3} \pm \sqrt{300+96}}{48}$$

$$x = \frac{\sqrt{396} - 10\sqrt{3}}{48}$$

Only 1 solution in $\left(-\frac{1}{2\sqrt{6}}, \frac{1}{2\sqrt{6}}\right)$

19. Let the solution curve of the differential equation $xdy - ydx = \sqrt{x^2 + y^2}dx$, $x > 0$, $y(1) = 0$, be $y = y(x)$. Then $y(3)$ is equal to

(1) 4

(2) 6

(3) 1

(4) 2

Ans. [1]

Sol. $\frac{xdy - ydx}{x^2} = \frac{\sqrt{x^2 + y^2}}{x^2} dx$

$$d\left(\frac{y}{x}\right) = \sqrt{1 + \frac{y^2}{x^2}} \cdot \frac{1}{x} dx$$

$$\int \frac{d\left(\frac{y}{x}\right)}{\sqrt{1 + \left(\frac{y}{x}\right)^2}} = \int \frac{1}{x} dx$$

$$\Rightarrow \ln\left(\frac{y}{x} + \sqrt{1 + \frac{y^2}{x^2}}\right) = \ln x + \ln k = \ln kx$$

$$\Rightarrow y + \sqrt{x^2 + y^2} = kx^2$$

$$0 + 1 = k$$

$$\Rightarrow y + \sqrt{x^2 + y^2} = x^2$$

$$y + \sqrt{9 + y^2} = 9 \Rightarrow y = 4$$

20. If the sum of the first four terms of an A.P. is 6 and the sum of its first six terms is 4, then the sum of its first twelve terms is

(1) -20

(2) -24

(3) -26

(4) -22

Ans. [4]

Sol. Sum of first 4 term $S_4 = 6$

$$\frac{4}{2}(2a + 3d) = 6 \Rightarrow 2a + 3d = 3 \quad \dots(1)$$

Sum of first 6 terms $S_6 = 4$

$$\frac{6}{2}(2a + 5d) = 4 \Rightarrow 2a + 5d = \frac{4}{3} \quad \dots(2)$$

eq.(2) - eq.(1)

$$(2a + 5d) - (2a + 3d) = \frac{4}{3} - 3$$

$$\Rightarrow d = -\frac{5}{6}$$

$$\therefore 2a + 3\left(-\frac{5}{6}\right) = 3 \Rightarrow a = \frac{11}{4}$$

$$S_{12} = \frac{12}{2} \left\{ 2 \times \frac{11}{4} + (12-1)\left(-\frac{5}{6}\right) \right\}$$

$$S_{12} = 6\left(-\frac{22}{6}\right) = -22$$

SECTION-B

21. Let $\alpha = \frac{-1 + i\sqrt{3}}{2}$ and $\beta = \frac{-1 - i\sqrt{3}}{2}$, $i = \sqrt{-1}$. If $(7 - 7\alpha + 9\beta)^{20} + (9 + 7\alpha - 7\beta)^{20} +$

$(-7 + 9\alpha + 7\beta)^{20} + (14 + 7\alpha + 7\beta)^{20} = m^{10}$, then m is _____.

Ans. [49]

Sol. $(7 - 7\omega + 9\omega^2)^{20} + (9 + 7\omega - 7\omega^2)^{20} + (-7 + 9\omega + 7\omega^2)^{20} + (14 + 7\omega + 7\omega^2)^{20} = m^{10}$

$$\Rightarrow \frac{(7\omega - 7\omega^2 + 9\omega^3)^{20}}{\omega^{20}} + (9 + 7\omega - 7\omega^2)^{20} + \frac{(-7\omega^2 + 9\omega^3 + 7\omega^4)^{20}}{\omega^{40}} + (14 + 7(\omega + \omega^2))^{20} = m^{10}$$

$$\Rightarrow (9 + 7\omega - 7\omega^2)^{20} \cdot \omega + (9 + 7\omega - 7\omega^2)^{20} + (9 + 7\omega - 7\omega^2)^{20} \cdot \omega^2 + (14 - 7)^{20} = m^{10}$$

$$\Rightarrow 0 + 7^{20} = m^{10}$$

$$\Rightarrow (7^2)^{10} = m^{10}$$

Hence, $M = 49$

22. Let A be a 3×3 matrix such that $A + A^T = O$. If $A \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix} = \begin{bmatrix} 3 \\ 3 \\ 2 \end{bmatrix}$, $A^2 \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix} = \begin{bmatrix} -3 \\ 19 \\ -24 \end{bmatrix}$ and

$\det(\text{adj}(2\text{adj}(A+I))) = (2)^\alpha \cdot (3)^\beta \cdot (11)^\gamma$, α, β, γ are non-negative integers, then $\alpha + \beta + \gamma$ is equal to _____

Ans. [18]

Sol. $A \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix} = \begin{bmatrix} 3 \\ 3 \\ 2 \end{bmatrix}$ and $A^2 \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix} = A \begin{bmatrix} 3 \\ 3 \\ 2 \end{bmatrix} = \begin{bmatrix} -3 \\ 19 \\ -24 \end{bmatrix}$

$$\det. (\text{adj}(2\text{adj}(A+I))) = |2\text{adj}(A+I)|^2 = 64 |\text{adj}(A+I)|^2 = 64 |A+I|^4$$

$$\text{Let } A = \begin{bmatrix} 0 & a & b \\ -a & 0 & c \\ -b & -c & 0 \end{bmatrix} \Rightarrow \begin{cases} -a = 3 \\ -b + c = 2 \\ 3a + 2b = -3 \end{cases} \because (A \text{ is Skew symmetric matrix})$$

$$\Rightarrow \begin{cases} a = -3 \\ b = 3 \\ c = 5 \end{cases}$$

$$\therefore |A+I| = \begin{vmatrix} 1 & -3 & 3 \\ 3 & 1 & 5 \\ -3 & -5 & 1 \end{vmatrix} = 44$$

23. If $\int (\sin x)^{\frac{-11}{2}} (\cos x)^{\frac{-5}{2}} dx =$

$$-\frac{p_1}{q_1} (\cot x)^{\frac{9}{2}} - \frac{p_2}{q_2} (\cot x)^{\frac{5}{2}} - \frac{p_3}{q_3} (\cot x)^{\frac{1}{2}} + \frac{p_4}{q_4} (\cot x)^{\frac{-3}{2}} + C,$$

where p_i and q_i are positive integers with $\gcd(p_i, q_i) = 1$ for $i = 1, 2, 3, 4$ and C is the constant of integration, then $\frac{15p_1p_2p_3p_4}{q_1q_2q_3q_4}$ is equal to _____.

Ans. [16]

Sol. $\int (\tan x)^{-11/2} \cdot \sec^8 x dx$

$$= \int (\tan x)^{-11/2} (1 + \tan^2 x)^3 \sec^2 x dx$$

Put $\tan x = t$,

$$\sec^2 x dx = dt$$

$$\Rightarrow \int t^{-11/2} (1 + t^2)^3 dt = \int t^{-11/2} (1 + t^6 + 3t^2 + 3t^4) dt$$

$$= \int (t^{-11/2} + t^{1/2} + 3t^{-7/2} + 3t^{-3/2}) dt$$

$$= -\frac{2}{9}(\cot x)^{9/2} - \frac{6}{5}(\cot x)^{5/2} - 6(\cot x)^{1/2} + \frac{2}{3}(\cot x)^{-3/2} + C$$

$$\Rightarrow p_1 = 2, p_2 = 6, p_3 = 6, p_4 = 2$$

$$\& q_1 = 9, q_2 = 5, q_3 = 1, q_4 = 3$$

$$\frac{15p_1p_2p_3p_4}{q_1q_2q_3q_4} = \frac{15 \cdot 2 \cdot 6 \cdot 6 \cdot 2}{9 \cdot 5 \cdot 1 \cdot 3} = 16$$

24. If $\frac{\cos^2 48^\circ - \sin^2 12^\circ}{\sin^2 24^\circ - \sin^2 6^\circ} = \frac{\alpha + \beta\sqrt{5}}{2}$, where $\alpha, \beta \in \mathbb{N}$, then $\alpha + \beta$ is equal to _____ .

Ans. [4]

Sol. Use $\sin(A+B)\sin(A-B) = \sin^2 A - \sin^2 B$

$$\begin{aligned} \cos(A+B)\cos(A-B) &= \cos^2 A - \sin^2 B \\ \frac{\cos 60^\circ \cos 36^\circ}{\sin 30^\circ \sin 18^\circ} &= \frac{\sqrt{5}+1}{\sqrt{5}-1} \times \frac{\sqrt{5}+1}{\sqrt{5}+1} = \frac{(\sqrt{5}+1)^2}{4} \\ &= \frac{3+\sqrt{5}}{2} \end{aligned}$$

$$\alpha = 3; \beta = 1$$

$$\text{So, } (\alpha + \beta) = 4$$

25. Let ABC be a triangle. Consider four points p_1, p_2, p_3, p_4 on the side AB, five points p_5, p_6, p_7, p_8, p_9 on the side BC and four points $p_{10}, p_{11}, p_{12}, p_{13}$ on the side AC. None of these points is a vertex of the triangle ABC. Then the total number of pentagons, that can be formed by taking all the vertices from the points p_1, p_2, \dots, p_{13} , is _____ .

Ans. [660]

Sol. Case 1 :

2 from AB, 2 from BC, 1 from AC

$$\binom{4}{2} \cdot \binom{5}{2} \cdot \binom{4}{1} = 6 \cdot 10 \cdot 4 = 240$$

Case 2 :

2 from AB, 1 from BC, 2 from AC

$$\binom{4}{2} \cdot \binom{5}{1} \cdot \binom{4}{2} = 6 \cdot 5 \cdot 6 = 180$$

Case 3 :

1 from AB, 2 from BC, 2 from AC

$$\binom{4}{1} \cdot \binom{5}{2} \cdot \binom{4}{2} = 4 \cdot 10 \cdot 6 = 240$$



JEE Main Online Exam 2026

Questions & Solution
22nd January 2026 | Morning

PHYSICS

SECTION-A

26. A solid sphere of mass 5 kg and radius 10 cm is kept in contact with another solid sphere of mass 10 kg and radius 20 cm. The moment of inertia of this pair of spheres about the tangent passing through the point of contact is ____ kg.m².

- (1) 0.36 (2) 0.72 (3) 0.18 (4) 0.63

Ans. [4]

Sol.
$$I = \frac{7}{5} [m_1 R_1^2 + m_2 R_2^2]$$

$$= \frac{7}{5} [5(10)^2 + 10 \times (20)^2] \times 10^{-4}$$

$$I = 63 \times 10^{-2} \text{ kg m}^2$$

$$I = 0.63 \text{ kg m}^2$$

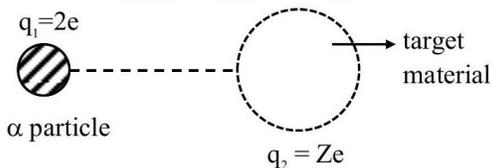
27. 7.9MeV α -particle scatters from a target material of atomic number 79. From the given data the estimated diameter of nuclei of the target material is (approximately) ____ m.

$$\left[\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ Nm}^2 / \text{C}^2 \text{ and electron charge} = 1.6 \times 10^{-19} \text{ C} \right]$$

- (1) 5.76×10^{-14} (2) 1.44×10^{-13} (3) 2.88×10^{-14} (4) 1.69×10^{-12}

Ans. [1]

Sol. By mechanical energy conservation



$$(Me)_i = (Me)_f$$

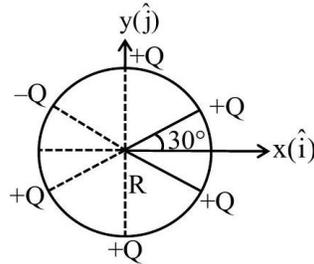
$$PE_i + KE_i = PE_f + KE_f$$

$$0 + 7.9 \times 10^6 \times 1.6 \times 10^{-19} = \frac{k(2e)(Ze)}{r} + 0$$

$$r = \frac{9 \times 10^9 \times 2 \times (1.6 \times 10^{-19})^2 \times 79}{7.9 \times 10^6 \times 1.6 \times 10^{-19}} = 2.88 \times 10^{-14} \text{ m}$$

$$\text{For diameter} \Rightarrow D = 2r = 5.76 \times 10^{-14} \text{ m}$$

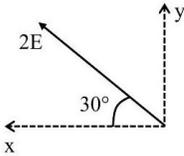
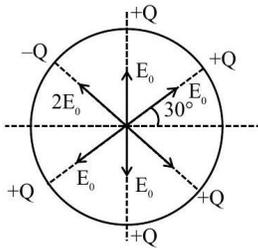
28. Six point charges are kept 60° apart from each other on the circumference of a circle of radius R as shown in figure. The net electric field at the centre of the circle is ____ . (ϵ_0 is permittivity of free space)



(1) $-\frac{5Q}{8\pi\epsilon_0 R^2}(\hat{i} + \sqrt{3}\hat{j})$ (2) $-\frac{Q}{4\pi\epsilon_0 R^2}(\sqrt{3}\hat{i} - \hat{j})$ (3) $-\left(\frac{5Q}{8\pi\epsilon_0 R^2}\right)(\hat{i} - 3\hat{j})$ (4) $\frac{Q}{4\pi\epsilon_0 R^2}(\sqrt{3}\hat{i} - \hat{j})$

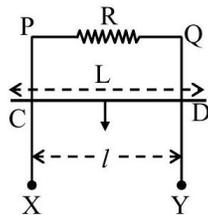
Ans. [2]

Sol. Let $\frac{kQ}{r^2} = E_0$



$$\begin{aligned} \vec{E}_{\text{net}} &= 2E_0 \cos 30^\circ (-\hat{i}) + 2E_0 \sin 30^\circ (\hat{j}) \\ &= \frac{2kQ}{r^2} \left[\frac{\sqrt{3}}{2} (-\hat{i}) + \frac{1}{2} \hat{j} \right] = \frac{-1Q}{4\pi\epsilon_0 r^2} (\sqrt{3}\hat{i} - \hat{j}) \end{aligned}$$

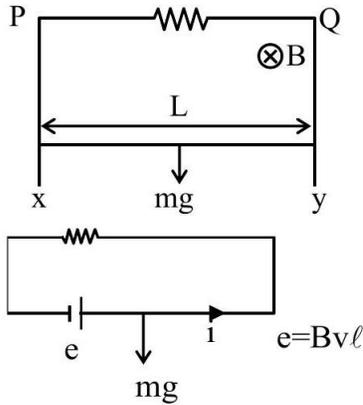
29. XPQY is a vertical smooth long loop having a total resistance R where PX is parallel to QY and separation between them is l . A constant magnetic field B perpendicular to the plane of the loop exists in the entire space. A rod CD of length L ($L > l$) and mass m is made to slide down from rest under the gravity as shown in figure. The terminal speed acquired by the rod is ____ m/s. (g = acceleration due to gravity)



(1) $\frac{2mgR}{B^2 l^2}$ (2) $\frac{8mgR}{B^2 l^2}$ (3) $\frac{2mgR}{B^2 L^2}$ (4) $\frac{mgR}{B^2 l^2}$

Ans. [4]

Sol.



at equilibrium (Or for terminal velocity)

$$mg = iBl \Rightarrow mg = \left(\frac{Bv\ell}{R} \right) Bl$$

$$V = \frac{mgR}{B^2 \ell^2}$$

30. The escape velocity from a spherical planet A is 10 km/s. The escape velocity from another planet B whose density and radius are 10% of those of planet A, is _____ m/s.

- (1) 1000 (2) $200\sqrt{5}$ (3) $100\sqrt{10}$ (4) $1000\sqrt{2}$

Ans. [3]

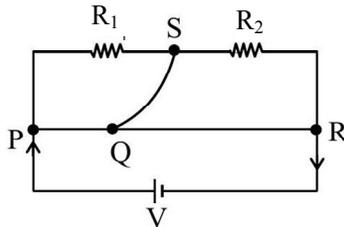
Sol.
$$V_e = \sqrt{\frac{2GM}{R}} = \sqrt{\frac{2G \times \rho \times \frac{4\pi R^3}{3}}{R}} \Rightarrow V_e \propto \sqrt{\rho} \times R$$

$$\frac{(V_e)_B}{(V_e)_A} = \sqrt{\frac{\rho_B}{\rho_A}} \times \frac{R_B}{R_A} = \sqrt{\frac{0.1\rho_A}{\rho_A}} \times \left(\frac{0.1R_A}{R_A} \right)$$

$$\frac{(V_e)_B}{(V_e)_A} = \frac{1}{10} \times \frac{1}{\sqrt{10}}$$

$$(V_e)_B = \frac{10 \times 1000}{10\sqrt{10}} = 100\sqrt{10} \text{ m/sec}$$

31. A meter bridge with two resistances R_1 and R_2 as shown in figure was balanced (null point) at 40 cm from the point P. The null point changed to 50 cm from the point P, when 16Ω resistance is connected in parallel to R_2 . The values of resistances R_1 and R_2 are _____.



(1) $R_2 = 16\Omega, R_1 = \frac{16}{3}\Omega$

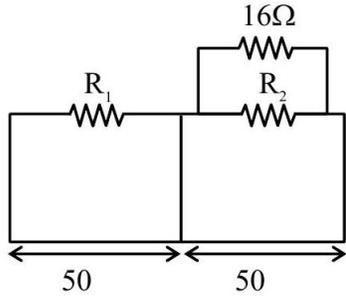
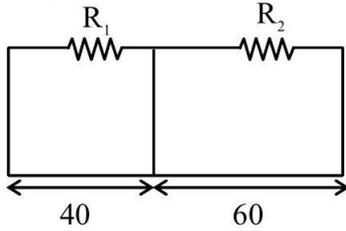
(2) $R_2 = 4\Omega, R_1 = \frac{4}{3}\Omega$

(3) $R_2 = 8\Omega, R_1 = \frac{16}{3}\Omega$

(4) $R_2 = 12\Omega, R_1 = \frac{12}{3}\Omega$

Ans. [3]

Sol.



$$\frac{R_1}{R_2} = \frac{40}{60} = \frac{2}{3} \quad \dots(1)$$

$$\frac{R_1}{\left(\frac{R_2 \times 16}{R_2 + 16}\right)} = \frac{50}{50} \Rightarrow R_1 = \frac{16R_2}{16 + R_2} \quad \dots(2)$$

$$\frac{2}{3}R_2 = \frac{16R_2}{16 + R_2}$$

$$\frac{32}{3} + \frac{2R_2}{3} = 16$$

$$\frac{2R_2}{3} = 16 - \frac{32}{3} = \frac{16}{3}$$

$$R_2 = 8\Omega$$

By equation (1)

$$R_1 = \frac{2}{3}R_2 = \frac{16}{3}\Omega$$

32. A projectile is thrown upward at an angle 60° with the horizontal. The speed of the projectile is 20 m/s when its direction of motion is 45° with the horizontal. The initial speed of the projectile is _____ m/s .

(1) $40\sqrt{2}$

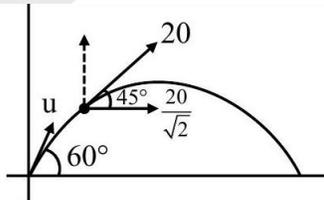
(2) 40

(3) $20\sqrt{3}$

(4) $20\sqrt{2}$

Ans. [4]

Sol.



$$u \cos 60^\circ = \frac{20}{\sqrt{2}}$$

$$\frac{u}{2} = \frac{20}{\sqrt{2}}$$

$$u = \frac{40}{\sqrt{2}}$$

$$u = 20\sqrt{2} \text{ m/s}$$

33. Given below are two statements:

Statement I: Pressure of fluid is exerted only on a solid surface in contact as the fluid-pressure does not exist everywhere in a still fluid.

Statement II: Excess potential energy of the molecules on the surface of a liquid, when compared to interior, results in surface tension.

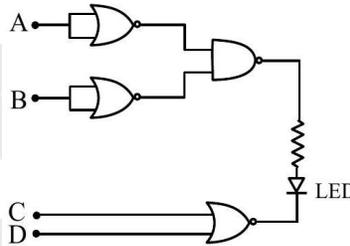
In the light of the above statements, choose the correct answer from the options given below.

- (1) Statement I is true but Statement II is false
- (2) Both Statement I and Statement II are false
- (3) Both Statement I and Statement II are true
- (4) Statement I is false but Statement II is true

Ans. [4]

Sol. According to pascal's law pressure at any point in liquid at rest is same in all direction. It exist at every point in the liquid not just at boundaries. So statement (1) is false. For interior molecule net cohesive forces are zero statement (2) is correct.

34. Find the correct combination of A, B, C and D inputs which can cause the LED to glow.



(1) 0100

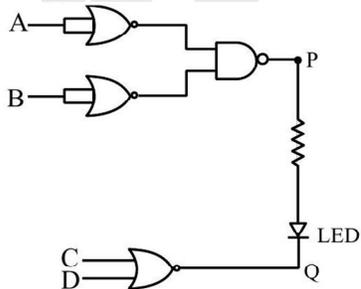
(2) 0011

(3) 1000

(4) 1101

Ans. [4]

Sol.

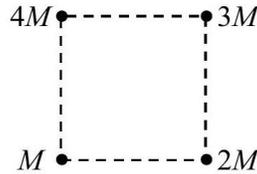


LED will glow in forward biasing :

P higher potential - 1

Q lower potential - 0

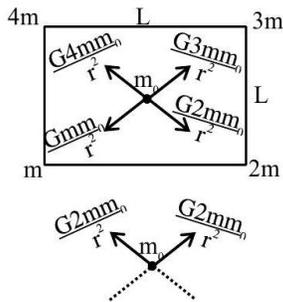
35. Net gravitational force at the centre of a square is found to be F_1 when four particles having mass $M, 2M, 3M$ and $4M$ are placed at the four corners of the square as shown in figure and it is F_2 when the positions of $3M$ and $4M$ are interchanged. The ratio $\frac{F_1}{F_2}$ is $\frac{\alpha}{\sqrt{5}}$. The value of α is ____ .



- (1) 2 (2) 3 (3) 1 (4) $2\sqrt{5}$

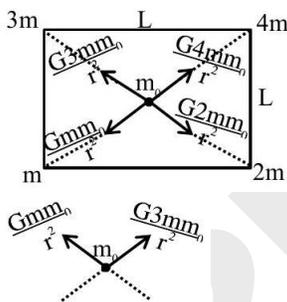
Ans. [1]

Sol. Initial configuration



$$F = 2\sqrt{2} \frac{Gmm_0}{r^2}$$

New configuration



$$F' = \sqrt{10} \frac{Gmm_0}{r^2} \Rightarrow \frac{F}{F'} = 2\sqrt{2} \cdot \frac{1}{\sqrt{10}} = \frac{2}{\sqrt{5}}$$

$$\therefore \alpha = 2$$

36. The minimum frequency of photon required to break a particle of mass 15.348 amu into 4α particles is ____ kHz .

[mass of He nucleus = 4.002 amu, $1\text{amu} = 1.66 \times 10^{-27}$ kg, $h = 6.6 \times 10^{-34}$ J.s and $c = 3 \times 10^8$ m/s]

- (1) 9×10^{19} (2) 9×10^{20} (3) 14.94×10^{20} (4) 14.94×10^{19}

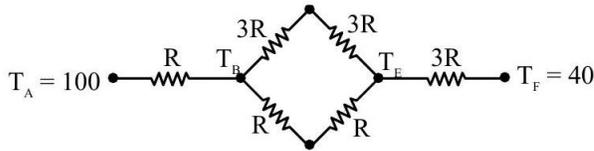
Ans. [4]

Sol. $h\nu = (4 \times 4.002 - 15.348) \times 1.66 \times 10^{-27} \times (3 \times 10^8)^2$

$$\nu = 14.94 \times 10^{19} \text{ kHz}$$

Ans. [1]

Sol. Let $\left[R = \frac{\ell}{3KA} \right]$



$$\left[H = \frac{100 - 40}{\frac{11R}{2}} \right] \quad \dots(1)$$

$$H = \frac{100 - T_B}{R} \quad \dots(2)$$

$$H = \frac{T_E - 40}{3R} \quad \dots(3)$$

using (1) and (2)

$$120 = 1100 - 11 T_A$$

$$T_B = 89^\circ \text{C}$$

using (1) and (3)

$$T_E = 73^\circ \text{C}$$

39. A thin convex lens of focal length 5 cm and a thin concave lens of focal length 4 cm are combined together (without any gap) and this combination has magnification m_1 when an object is placed 10 cm before the convex lens. Keeping the positions of convex lens and object undisturbed a gap of 1 cm is introduced between the lenses by moving the concave lens away, which lead to a change in magnification of total lens

system to m_2 . The value of $\left| \frac{m_1}{m_2} \right|$ is _____ .

(1) $\frac{5}{9}$

(2) $\frac{5}{27}$

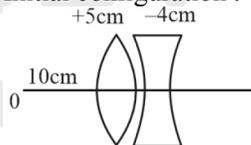
(3) $\frac{3}{2}$

(4) $\frac{25}{27}$

Ans. [Dropped by JEE]

Sol. None of the given options are correct.

Initial configuration :



$$\frac{1}{f} = \frac{1}{5} - \frac{1}{4} = -\frac{1}{20}$$

$$f = -20 \text{ cm}$$

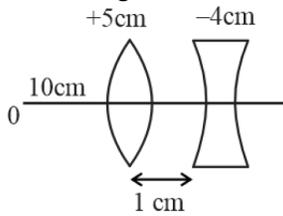
$$u = -10 \text{ cm}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$v = \frac{uf}{u+f}$$

$$m_1 = \frac{v}{u} = \frac{f}{u+f} = \frac{-20}{-10-20} = +\frac{2}{3}$$

New configuration :



1st refraction

$$u = -10 \text{ cm}, f = 5 \text{ cm}$$

$$v = \frac{uf}{u+f} = +10 \text{ cm}$$

$$m = -1$$

2nd refraction

$$u = +9 \text{ cm}$$

$$f = -4 \text{ cm}$$

$$m' = \frac{f}{u+f} = \frac{-4}{5}$$

$$m_2 = mm'$$

$$= (-1) \left(\frac{-4}{5} \right) = \frac{4}{5}$$

$$\frac{m_1}{m_2} = \frac{2}{3} \times \frac{5}{4} = \frac{5}{6}$$

40. Consider an equilateral prism (refractive index $\sqrt{2}$). A ray of light is incident on its one surface at a certain angle i . If the emergent ray is found to graze along the other surface then the angle of refraction at the incident surface is close to _____ .

(1) 15°

(2) 20°

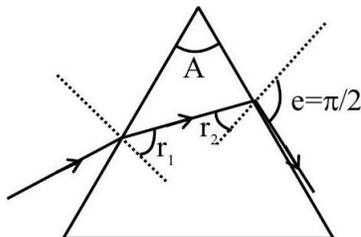
(3) 40°

(4) 30°

Ans. [1]

Sol. Equilateral prism.

$$A = 60^\circ$$



$$\mu \sin r_2 = 1 \cdot \sin e = 1$$

$$\sin r_2 = \frac{1}{\mu} = \frac{1}{\sqrt{2}}$$

$$r_2 = 45^\circ$$

$$\therefore r_1 = A - r_2 = 15^\circ$$

41. The volume of an ideal gas increases 8 times and temperature becomes $(1/4)^{\text{th}}$ of initial temperature during a reversible change. If there is no exchange of heat in this process ($\Delta Q = 0$) then identify the gas from the following options (Assuming the gases given in the options are ideal gases) :

(1) CO_2 (2) O_2 (3) NH_3 (4) He

Ans. (4)

Sol. $PV^\gamma = \text{constant}$

$$TV^{\gamma-1} = \text{constant}$$

$$TV^{\gamma-1} = \left(\frac{T}{4}\right)(8V)^{(\gamma-1)}$$

$$4 = 8^{(\gamma-1)}$$

$$2^2 = 2^{3\gamma-3}$$

$$2 = 3(\gamma-1)$$

$$\gamma = \frac{5}{3}$$

Gas is a monoatomic gas

Answer is He .

42. Electric field in a region is given by $\vec{E} = Ax\hat{i} + By\hat{j}$, where $A = 10 \text{ V/m}^2$ and $B = 5 \text{ V/m}^2$. If the electric potential at a point $(10, 20)$ is 500 V , then the electric potential at origin is _____ V.

(1) 1000 (2) 500 (3) 2000 (4) 0

Ans. [3]

Sol. $\vec{E} = 10x\hat{i} + 5y\hat{j}$

$$V_{\text{at}(10,20)} = 500 \text{ V}$$

$$\Delta V = - \int \vec{E} \cdot d\vec{r}$$

$$500 - V_0 = - \int_{(0,0)}^{(10,20)} (10x\hat{i} + 5y\hat{j}) \cdot (dx\hat{i} + dy\hat{j})$$

$$500 - V_0 = - \left[5x^2 + \frac{5y^2}{2} \right]_{(0,0)}^{(10,20)}$$

$$V_0 - 500 = \left(500 + 5 \times \frac{400}{2} \right) - (0 - 0)$$

$$V_0 - 500 = 500 + 1000$$

$$V_0 = 2000 \text{ V}$$

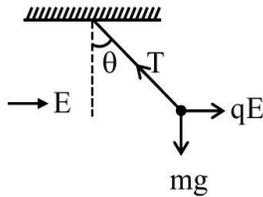
43. A simple pendulum has a bob with mass m and charge q . The pendulum string has negligible mass. When a uniform and horizontal electric field \vec{E} is applied, the tension in the string changes. The final tension in the string, when pendulum attains an equilibrium position is _____ .

(g : acceleration due to gravity)

(1) $mg - qE$ (2) $mg + qE$ (3) $\sqrt{m^2g^2 + q^2E^2}$ (4) $\sqrt{m^2g^2 - q^2E^2}$

Ans. [3]

Sol.



$$T = \sqrt{(qE)^2 + (mg)^2}$$

44. Match the LIST-I with LIST-II

	List-I		List-II
A.	Spring constant	I.	$ML^2 T^{-2} K^{-1}$
B.	Thermal conductivity	II.	$ML^0 T^{-2}$
C.	Boltzmann constant	III.	$ML^2 T^{-3} A^{-2}$
D.	Inductive reactance	IV.	$MLT^{-3} K^{-1}$

Choose the correct answer from the options given below:

(1) A-II, B-I, C-IV, D-III

(2) A-I, B-IV, C-II, D-III

(3) A-III, B-II, C-IV, D-I

(4) A-II, B-IV, C-I, D-III

Ans. [4]

Sol. (A) $F = Kx$

$$[MLT^{-2}] = [K][L]$$

$$[K] = ML^0 T^{-2}$$

(B) Thermal conductivity

$$\frac{dQ}{dt} = \frac{kA}{\ell} \Delta T$$

$$ML^2 T^{-3} = \frac{[k]L^2 K}{L}$$

$$[K^1] = MLT^{-3} K^{-1}$$

(C) Boltzmann constant

$$[K] = ML^2 T^{-2} K^{-1}$$

(D) Inductive reactance

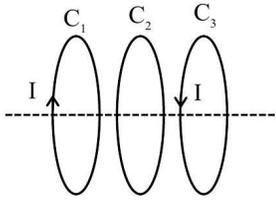
$$\frac{[V]}{[I]} = \frac{ML^2 T^{-3} A^{-1}}{A} = ML^2 T^{-3} A^{-2}$$

45. Three identical coils C_1, C_2 and C_3 are closely placed such that they share a common axis. C_2 is exactly midway. C_1 carries current I in anti-clockwise direction while C_3 carries current I in clockwise direction. An induced current flows through C_2 will be in clockwise direction when

- (1) C_1 and C_3 move with equal speeds away from C_2
- (2) C_1 moves towards C_2 and C_3 moves away from C_2
- (3) C_1 moves away from C_2 and C_3 moves towards C_2
- (4) C_1 and C_3 move with equal speeds towards C_2

Ans. [2]

Sol.



Magnetic field through the coil is

$$\vec{B} = (B_{C_2} - B_{C_1}) \hat{i}$$

$$\phi = (B_{C_2} - B_{C_1}) A$$

$$\varepsilon = \frac{-d\phi}{dt}$$

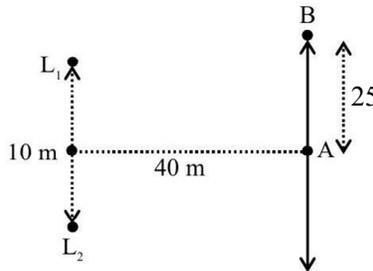
Find the direction according to Lenz's law

If coil move away then magnetic field decreases & vice versa

Correct Ans. (2)

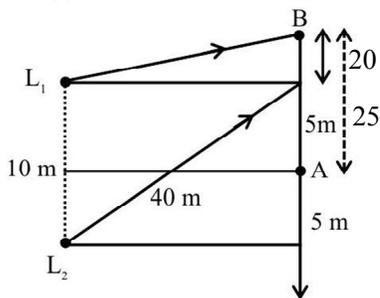
SECTION-B

46. Two loudspeakers (L_1 and L_2) are placed with a separation of 10 m, as shown in figure. Both speakers are fed with an audio input signal of same frequency with constant volume. A voice recorder, initially at point A, at equidistance to both loud speakers, is moved by 25 m along the line AB while monitoring the audio signal. The measured signal was found to undergo 10 cycles of minima and maxima during the movement. The frequency of the input signal is ____ Hz

 (Speed of sound in air is 324 m/s and $\sqrt{5} = 2.23$)


Ans. [600]

Sol.


 Point B will 10th maxima

$$\Delta x = L_2 B - L_1 B$$

$$L_1 B = \sqrt{20^2 + 40^2} = 20\sqrt{5} \text{ m} = 44.6 \text{ m}$$

$$L_2 B = \sqrt{40^2 + 30^2} = 50 \text{ m}$$

$$\Delta x = 50 - 44.6 = 5.4 \text{ m}$$

$$\Delta x = n\lambda$$

$$5.4 = 10 \times \lambda$$

$$\lambda = 0.54 \text{ m}$$

$$V = f\lambda$$

$$f = \frac{324}{0.54} = 600 \text{ Hz}$$

47. The electric field of a plane electromagnetic wave, travelling in an unknown non-magnetic medium is given by, $E_y = 20\sin(3 \times 10^6 x - 4.5 \times 10^{14} t)$ V/m (where x, t and other values have S.I. units). The dielectric constant of the medium is _____ .

(speed of light in free space is 3×10^8 m/s)

Ans. [4]

Sol. $n = \frac{C}{V}$

$$V = \frac{\omega}{k} = \frac{4.5 \times 10^{14}}{3 \times 10^6} = \frac{3}{2} \times 10^8$$

$$n = 2$$

$$n = \sqrt{\mu_r \epsilon_r} \quad (\mu_r = 1)$$

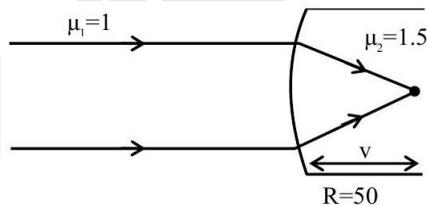
$$2 = \sqrt{\epsilon_r}$$

$$\epsilon_r = 4$$

48. A parallel beam of light travelling in air (refractive index 1.0) is incident on a convex spherical glass surface of radius of curvature 50 cm . Refractive index of glass is 1.5 . The rays converge to a point at a distance x cm from the centre of the curvature of the spherical surface. The value of x is _____ cm .

Ans. [100]

Sol.



$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R} \Rightarrow \frac{1.5}{v} - \frac{1}{\infty} = \frac{1.5 - 1}{50}$$

$$V = 150 \text{ cm}$$

$x \rightarrow$ measure from center

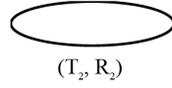
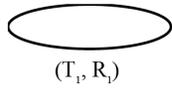
$$x = V - R$$

$$= 150 - 50 = 100 \text{ cm}$$

49. A circular disc has radius R_1 and thickness T_1 . Another circular disc made of the same material has radius R_2 and thickness T_2 . If the moment of inertia of both discs are same and $\frac{R_1}{R_2} = 2$ then $\frac{T_1}{T_2} = \frac{1}{\alpha}$. The value of α is ____ .

Ans. [16]

Sol.



$$m_1 = \pi R_1^2 T_1 \rho$$

$$m_2 = \pi R_2^2 T_2 \rho$$

$$I_1 = \frac{m_1 R_1^2}{2}$$

$$I_2 = \frac{m_2 R_2^2}{2}$$

$$I_1 = I_2$$

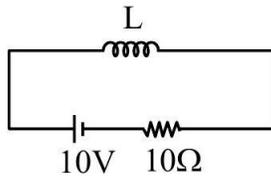
$$\frac{\pi R_1^2 T_1 \rho R_1^2}{2} = \frac{\pi R_2^2 T_2 \rho R_2^2}{2} \Rightarrow \frac{T_1}{T_2} = \frac{1}{16}$$

50. Inductance of a coil with 10^4 turns is 10 mH and it is connected to a dc source of 10 V with internal resistance of 10Ω . The energy density in the inductor when the current reaches $\left(\frac{1}{e}\right)$ of its maximum value is $\alpha\pi \times \frac{1}{e^2} \text{ J/m}^3$. The value of α is ____ . ($\mu_0 = 4\pi \times 10^{-7} \text{ Tm/A}$).

Ans. [20]

Sol. $L = 10 \times 10^{-3} \text{ H}$

$$N = 10^4$$



$$I_0 = \frac{10}{10} = 1 \text{ A (max current)}$$

$$I = \frac{1}{e}$$

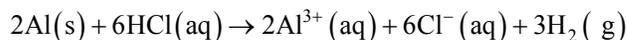
$$E_d = \frac{B^2}{2\mu_0}$$

$$B = \mu_0 n I$$

$$L = \mu_0 n^2 \pi R^2 \ell$$

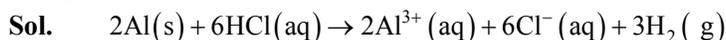
$$E_d = \frac{\mu_0 n^2 I^2}{2} = \frac{4\pi \times 10^{-7} \times 10^8 \times \frac{1}{e^2}}{2} = \frac{20\pi}{e^2}$$

56. In the reaction,



- (1) 11.2 L $\text{H}_2(g)$ at STP is produced for every mole of HCl consumed.
- (2) 67.2 L $\text{H}_2(g)$ at STP is produced for every mole of Al that reacts.
- (3) 12 L $\text{HCl}(aq)$ is consumed for every 6 L $\text{H}_2(g)$ produced.
- (4) 33.6 L $\text{H}_2(g)$ is produced regardless of temperature and pressure for every mole of Al that reacts.

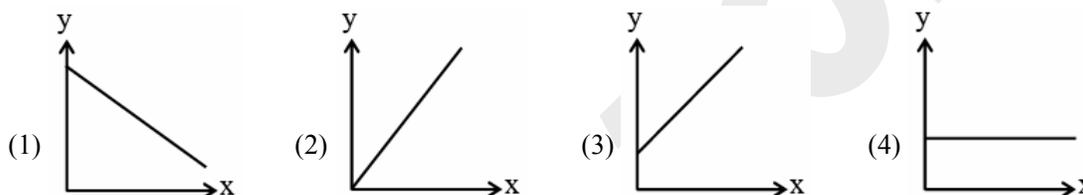
Ans.[1]



$$\begin{aligned} \text{Mole of } \text{H}_2 \text{ produced} \\ &= 2 \times \text{mole of HCl used} \\ &= \frac{2}{3} \times \text{mole of Al used} \end{aligned}$$

57. Consider a solution of $\text{CO}_2(g)$ dissolved in water in a closed container.

Which one of the following plots correctly represents variation of \log (partial pressure of CO_2 in vapour phase above water) [y-axis] with \log (mole fraction of CO_2 in water) [x-axis] at 25°C ?



Ans.[3]

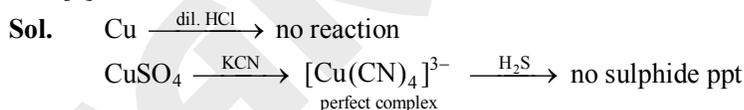
Sol. From Henry's law :

$$\begin{aligned} P(g) &= K_H \cdot X(g) \\ \log P(g) &= \log K_H + \log X(g) \end{aligned}$$

58. A first row transition metal (M) does not liberate H_2 gas from dilute HCl. 1 mol of aqueous solution of MSO_4 is treated with excess of aqueous KCN and then $\text{H}_2\text{S}(g)$ is passed through the solution. The amount of MS (metal sulphide) formed from the above reaction is ____ mol.

- (1) 2
- (2) 1
- (3) 3
- (4) 0

Ans.[4]



59. The correct order of reactivity of CH_3Br in methanol with the following nucleophiles is F^- , I^- , $\text{C}_2\text{H}_5\text{O}^-$ and $\text{C}_6\text{H}_5\text{O}^-$

- (1) $\text{I}^- > \text{C}_6\text{H}_5\text{O}^- > \text{F}^- > \text{C}_2\text{H}_5\text{O}^-$
- (2) $\text{I}^- > \text{C}_2\text{H}_5\text{O}^- > \text{C}_6\text{H}_5\text{O}^- > \text{F}^-$
- (3) $\text{I}^- > \text{C}_2\text{H}_5\text{O}^- > \text{F}^- > \text{C}_6\text{H}_5\text{O}^-$
- (4) $\text{I}^- > \text{F}^- > \text{C}_6\text{H}_5\text{O}^- > \text{C}_2\text{H}_5\text{O}^-$

Ans.[2]

Sol. Order of nucleophilicity :



60. Match the LIST-I with LIST-II

List-I Thermodynamic Process		List-II Magnitude in kJ	
A.	Work done in reversible, isothermal expansion of 2 mol of ideal gas from 2 dm^3 to 20 dm^3 at 300 K .	I.	4
B.	Work done in irreversible isothermal expansion of 1 mol ideal gas from 1 m^3 to 3 m^3 at 300 K against A constant pressure of 3 kPa .	II.	11.5
C.	Change in internal energy for adiabatic expansion of a 1 mol ideal gas with change of temperature = 320 K and $\bar{C}_V = \frac{3}{2}R$.	III.	6
D.	Change in enthalpy at constant pressure of 1 mole ideal gas with change of temperature = 337 K and $\bar{C}_p = \frac{5}{2}R$.	IV.	7

Choose the correct answer from the option given below :

(1) A-III, B-II, C-IV, D-I

(2) A-II, B-III, C-I, D-IV

(3) A-I, B-II, C-III, D-IV

(4) A-II, B-I, C-III, D-IV

Ans.[2]

Sol. Option (A)

$$\begin{aligned}W &= -nRT \ln \frac{V_2}{V_1} \\&= \frac{-2 \times 8.314 \times 300}{1000} \times \ln \left(\frac{20}{2} \right) \text{ kJ} \\&= -11.5 \text{ kJ}\end{aligned}$$

Option (B)

$$\begin{aligned}W &= -P_{\text{ext}}[V_2 - V_1] \\&= -3[3 - 1] \\&= -6 \text{ kJ}\end{aligned}$$

Option (C)

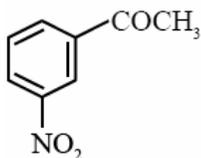
$$\begin{aligned}\Delta U &= nC_V \Delta T \\&= 1 \times \frac{3}{2} \times \frac{8.314 \times 320}{1000} \text{ kJ} \\&= 3.99\end{aligned}$$

Option (D)

$$\begin{aligned}\Delta H &= nC_p \Delta T \\&= 1 \times \frac{5}{2} \times \frac{8.314 \times 337}{1000} \text{ kJ} \\&= 7 \text{ kJ}\end{aligned}$$

61. Given below are two statements :

Statement I : Benzene is nitrated to give nitrobenzene, which on further treatment with $\text{CH}_3\text{COCl}/\text{AlCl}_3$ will give



Statement II : NO_2 group is a m-directing, and deactivating group.

In the light of the above statements, choose the most appropriate answer from the options given below.

- (1) Statement I is correct but Statement II is incorrect.
- (2) Both Statement I and Statement II are correct.
- (3) Statement I is incorrect but Statement II is correct.
- (4) Both Statement I and Statement II is are incorrect.

Ans.[3]

Sol. Nitrobenzene does not give Fridel-Craft acylation since it is highly deactivated ring.

62. $\text{A} \rightarrow$ products (First order reaction).

Three sets of experiment were performed for a reaction under similar experimental conditions.

Run 1 \Rightarrow 100 mL of 10 M solution of reactant A

Run 2 \Rightarrow 200 mL of 10 M solution of reactant A

Run 3 \Rightarrow 100 mL of 10 M solution of reactant A + 100 mL of H_2O added.

The correct variation of rate of reaction is

- (1) Run 1 = Run 2 = Run 3
- (2) Run 3 < Run 1 = Run 2
- (3) Run 3 < Run 1 < Run 2
- (4) Run 1 < Run2 < Run3

Ans.[2]

Sol. For Ist order reaction

$$\text{Rate} = k[\text{A}]$$

with decrease in concentration of A , rate of reaction decreases.

63. Match the **LIST-I** with **LIST-II**

List-I Reagents		List-II Name of Reaction involving carbonyl compound	
A.	$\text{NH}_2 - \text{NH}_2, \text{KOH}$	I.	Tollen's Test
B.	$\text{Ag}(\text{NH}_3)_2 \text{OH}$	II.	Clemmensen Reduction
C.	Aq. CuSO_4 , Sodium Potassium tartarate, KOH	III.	Wolff-Kishner Reduction
D.	$\text{Zn} - \text{Hg}, \text{HCl}$	IV.	Fehling's Test

Choose the correct answer from the options given below

- (1) A-III, B-I, C-IV, D-II
- (2) A-II, B-I, C-IV, D-III
- (3) A-IV, B-III, C-II, D-I
- (4) A-III, B-IV, C-I, D-II

Ans.[1]

Sol. Theoretical (NCERT Based)

64. Given below are two statements :

Statement I: The halogen that makes longest bond with hydrogen in HX, has the smallest covalent radius in its group.

Statement II : A group 15 element's hydride EH_3 has the lowest boiling point among corresponding hydrides of other group 15 elements. The maximum covalency of that element E is 4 .

In the light of the above statements, choose the correct answer from the options given below.

- (1) Both Statement I and Statement II are true.
- (2) Statement I is false but Statement II is true.
- (3) Both Statement I and Statement II are false.
- (4) Statement I is true but Statement II is false.

Ans.[3]

Sol. $\text{HF} < \text{HCl} < \text{HBr} < \text{HI}$ (bond length order)

$\text{F} < \text{Cl} < \text{Br} < \text{I}$ (radius order)

$\text{PH}_3 < \text{AsH}_3 < \text{NH}_3 < \text{SbH}_3 < \text{BiH}_3$ (Boiling point order)

Maximum possible covalency of phosphorous is 6

65. Given below are two statements:

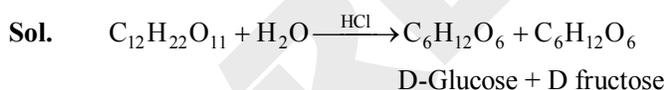
Statement I: Sucrose is dextrorotatory. However sucrose upon hydrolysis gives a solution having mixture of products. This solution shows laevorotation.

Statement II : Hydrolysis of sucrose gives glucose and fructose. Since the laevorotation of glucose is more than the dextrorotation of fructose the resulting solution becomes laevorotatory.

In the light of the above statements, choose the correct answer from the options given below.

- (1) Statement I is false but Statement II is true.
- (2) Both Statement I and Statement II are false.
- (3) Both Statement I and Statement II are true.
- (4) Statement I is true but Statement II is false.

Ans.[4]

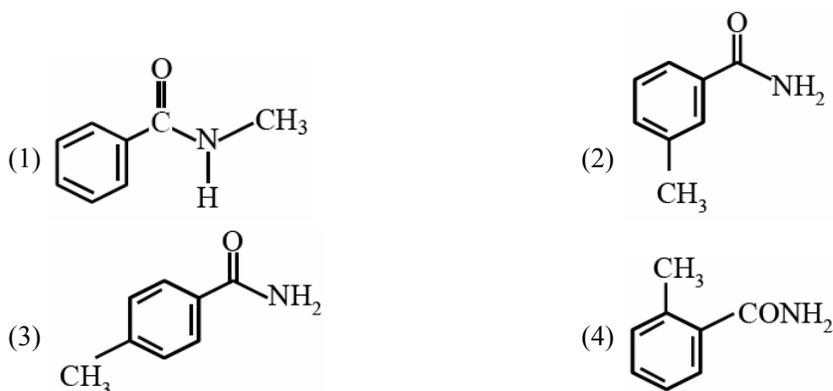
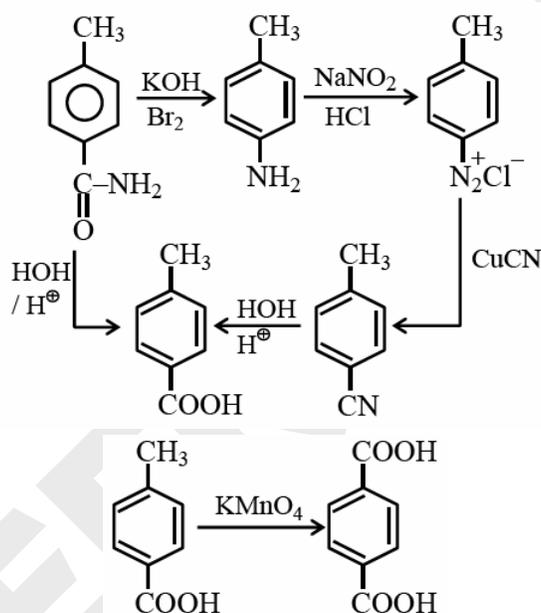


$$[\alpha]_{\text{D-sucrose}} = +66.5^\circ, [\alpha]_{\text{D-Glucose}} = +52.5^\circ,$$

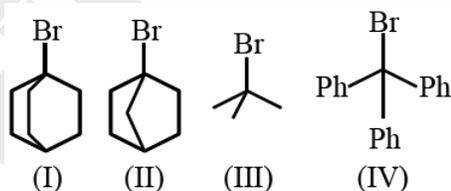
$$[\alpha]_{\text{D-Fructose}} = -92.4^\circ$$

\Rightarrow Sucrose is dextrorotatory and hydrolysed product is laevorotatory.

66. 'A' is a neutral organic compound (M. F : $\text{C}_8\text{H}_9\text{ON}$). On treatment with aqueous $\text{Br}_2 / \text{HO}^{(-)}$, 'A' forms a compound ' B ' which is soluble in dilute acid. ' B ' on treatment with aqueous $\text{NaNO}_2 / \text{HCl} (0 - 5^\circ\text{C})$ produces a compound ' C ' which on treatment with $\text{CuCN} / \text{NaCN}$ produces 'D' Hydrolysis of 'D' produces ' E ' which is also obtainable from the hydrolysis of 'A'. 'E' on treatment with acidified KMnO_4 produces 'F'. 'F' contains two different types of hydrogen atoms. The structure of ' A ' is


Ans.[3]
Sol.


67. The correct order of the rate of reaction of the following reactants with nucleophile by S_N1 mechanism is :
(Given : Structure I and II are rigid)



- (1) IV < III < II < I (2) III < I < II < IV (3) II < I < III < IV (4) I < II < III < IV

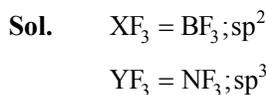
Ans.[3]
Sol. Rate of $S_N1 \propto$ Stability of C^\oplus formed

(I) and (II) are unstable due to Bredt's rule, (I) has more +I effect.

(II) < (I) < (III) < (IV)

68. Two p-block elements X and Y form fluorides of the type EF_3 . The fluoride compound XF_3 is a Lewis acid and YF_3 is a Lewis base. The hybridization of the central atoms of XF_3 and YF_3 respectively are
- (1) Both sp^3 (2) sp^2 and sp^3 (3) sp^3 and sp^2 (4) Both sp^2

Ans.[2]



69. As compared with chlorocyclohexane, which of the following statements correctly apply to chlorobenzene ?
- A. The magnitude of negative charge is more on chlorine atoms
B. The C – Cl bond has partial double bond character
C. C – Cl bond is less polar
D. C – Cl bond is longer due to repulsion between delocalised electrons of the aromatic ring and lone pairs of electrons of chlorine.
E. The C – Cl bond is formed using sp^2 hybridised orbital of carbon.
- Choose the correct answer from the options given below :
- (1) A, C and E only (2) B, C and D only
(3) A, D and E only (4) B, C and E only

Ans.[4]

Sol. Chlorocyclohexane is more polar due to -I effect of -Cl,
Whereas chlorobenzene has $-I > +M$, so it is less polar & also has partial double bond character.

70. Given below are two statements:
- Statement I:** The Henry's law constant K_H is constant with respect to variations in solution's concentration over the range for which the solutions is ideally dilute.
- Statement II :** K_H does not differ for the same solute in different solvents.
- In the light of the above statements, choose the correct answer from the options.
- (1) Statement I is false but Statement II is true.
(2) Statement I is true but Statement II is false.
(3) Both Statement I and Statement II are true.
(4) Both Statement I and Statement II are false.

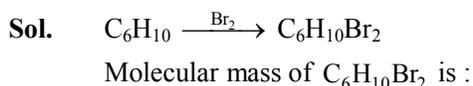
Ans.[2]

Sol. K_H depends on the nature of gas and solvent.

SECTION-B

71. The cycloalkane (X) on bromination consumes one mole of bromine per mole of (X) and gives the product (Y) in which C : Br ratio is 3 : 1. The percentage of bromine in the product (Y) is ____ %. (Nearest integer)
(Given : Molar mass in $g\ mol^{-1}$ H : 1, C : 12, O : 16, Br : 80)

Ans.[66]



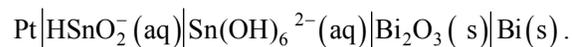
$$12 \times 6 + 10 + 160$$

$$72 + 10 + 160 = 242$$

$$\% \text{ of Br} = \frac{160}{242} \times 100$$

$$\% \text{ of Br} = 66.11\% \approx 66\%$$

72. Consider the following electrochemical cell at 298 K



If the reaction quotient at a given time is 10^6 , then the cell EMF (E_{cell}) is $\text{_____} \times 10^{-1}$ V (Nearest integer).

Given the standard half-cell reduction potential as

$$E_{\text{Bi}_2\text{O}_3/\text{Bi,OH}^-}^0 = -0.44 \text{ V and}$$

$$E_{\text{Sn}(\text{OH})_6^{2-}/\text{HSnO}_2^-,\text{OH}}^0 = -0.90 \text{ V}$$

Ans.[4]

Sol. $E_{\text{cell}}^0 = -0.44 - (-0.90)$
 $= +0.46 \text{ V}$

Applying Nernst equation :-

$$E_{\text{cell}} = E_{\text{cell}}^0 - \frac{0.06}{n} \log Q$$

$$E_{\text{cell}} = 0.46 - \frac{0.06}{6} \log 10^6$$

$$E_{\text{cell}} = 4 \times 10^{-1}$$

$$x = 4$$

73. The temperature at which the rate constants of the given below two gaseous reactions become equal is _____ K. (Nearest integer).



Given : $\ln 10 = 2.303$

Ans.[1303]

Sol. $10^4 e^{\frac{-24000}{T}} = 10^6 e^{\frac{-30000}{T}}$

$$e^{\frac{6000}{T}} = 100$$

$$\frac{6000}{T} = 2 \ln 10$$

$$T = \frac{6000}{2 \times 2.303}$$

$$T = 1302.64 \text{ K}$$

$$T \approx 1303 \text{ K}$$

74. Sodium fusion extract of an organic compound (Y) with CHCl_3 and chlorine water gives violet color to the CHCl_3 layer. 0.15 g of (Y) gave 0.12 g of the silver halide precipitate in Carius method. Percentage of halogen in the compound (Y) is _____. (Nearest integer).
(Given : molar mass g mol^{-1} C : 12, H : 1, Cl : 35.5, Br : 80, I = 127)

Ans.[43]

Sol. Iodine gives violet colour

$$\% \text{ of I} = \frac{\text{Atomic weight of I}}{\text{Molecular weight of AgI}} \times \frac{m}{W} \times 100$$

$$= \frac{127}{235} \times \frac{0.12}{0.15} \times 100$$

$$\% \text{ of I} = 43.23 \% \approx 43\%$$

75. Dissociation of a gas A_2 takes place according to the following chemical reactions. At equilibrium, the total pressure is 1 bar at 300 K .



The standard Gibbs energy of formation of the involved substances has been provided below:

Substance	$\Delta G_f^\circ / \text{kJmol}^{-1}$
A_2	-100.00
A	-50.832

The degree of dissociation of A_2 (g) is given by $(x \times 10^{-2})^{1/2}$ where $x =$ _____. (Nearest integer).

[Given : $R = 8 \text{ J mol}^{-1} \text{ K}^{-1}$, $\log 2 = 0.3010$, $\log 3 = 0.48$]

Ans.[33]

Sol. $-1.664 \times 10^3 = -8.3 \times 300 \ln K_p$

$$\ln K_p = 0.693$$

$$K_p = 2$$

$$2 = \frac{4\alpha^2 P_0}{1 - \alpha^2}$$

$$\alpha = \frac{1}{\sqrt{3}}$$

$$\alpha = \left(\frac{100}{3} \times 10^{-2} \right)^{1/2}$$

$$= (33.33 \times 10^{-2})^{1/2}$$