



## JEE Main Online Exam 2025

Questions & Solution  
29<sup>th</sup> January 2025 | Morning

### MATHEMATICS

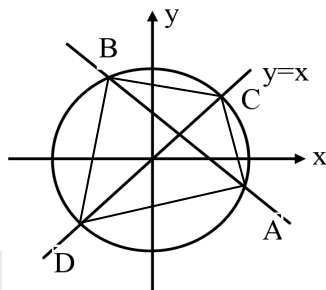
**Section-A:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct..

**Q.1** Let the line  $x + y = 1$  meet the circle  $x^2 + y^2 = 4$  at the points A and B. If the line perpendicular to AB and passing through the mid point of the chord AB intersects the circle at C and D, then the area of the quadrilateral ADCB is equal to :

- (1)  $3\sqrt{7}$                       (2)  $2\sqrt{14}$                       (3)  $5\sqrt{7}$                       (4)  $\sqrt{14}$

**Ans.** [2]

**Sol.**



By solving  $x = y$  with circle

We get

$$C(\sqrt{2}, \sqrt{2})$$

$$D(-\sqrt{2}, -\sqrt{2})$$

By solving  $x + y = 1$  with circle  $x^2 + y^2 = 4$

we get

$$A\left(\frac{1+\sqrt{7}}{2}, \frac{1-\sqrt{7}}{2}\right)$$

$$\& B\left(\frac{1-\sqrt{7}}{2}, \frac{1+\sqrt{7}}{2}\right)$$

$\therefore$  Area of Quadrilateral ACBD

$$= 2 \times \text{Area of } \triangle BCD$$

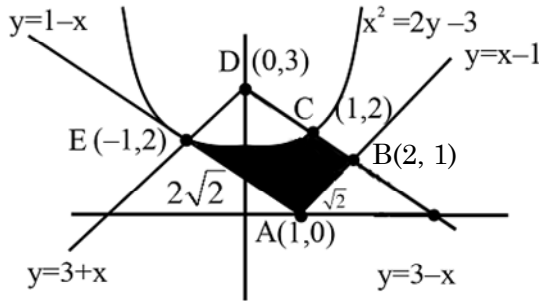
$$= 2 \times \frac{1}{2} \begin{vmatrix} \sqrt{2} & \sqrt{2} & 1 \\ \frac{1-\sqrt{7}}{2} & \frac{1+\sqrt{7}}{2} & 1 \\ -\sqrt{2} & -\sqrt{2} & 1 \end{vmatrix} = 2\sqrt{14}$$







- Q.7** Let the area of the region  $\{(x, y) : 2y \leq x^2 + 3, y + |x| \leq 3, y \geq |x - 1|\}$  be A. Then 6A is equal to :  
 (1) 16 (2) 12 (3) 18 (4) 14
- Ans.** [4]  
**Sol.**



$A \Rightarrow$  Rectangle ABDE – Area of region EDC

$$A \Rightarrow 4 - 2 \int_0^1 (3-x) - \left( \frac{x^2+3}{2} \right) dx$$

$$A \Rightarrow 4 - 2 \left\{ 3x - \frac{x^2}{2} - \frac{x^3}{6} - \frac{3}{2}x \right\}_0^1$$

$$A \Rightarrow 4 - 2 \left\{ 3 - \frac{1}{2} - \frac{1}{6} - \frac{3}{2} \right\} = \frac{7}{3}$$

So  $6A = 14$

- Q.8** The least value of n for which the number of integral terms in the Binomial expansion of  $(\sqrt[3]{7} + \sqrt[12]{11})^n$  is 183, is :  
 (1) 2184 (2) 2148 (3) 2172 (4) 2196

**Ans.** [1]  
**Sol.**

General term =  ${}^n C_r \{7^{1/3}\}^{n-r} \{11^{1/12}\}^r$

$$= {}^n C_r \{7\}^{\frac{n-r}{3}} \{11\}^{r/12}$$

For integral terms, r must be multiple of 12

$$\therefore r = 12k, k \in W$$

Total values of r = 183

$$\text{Hence max } r = 12(182) = 2184$$

Min value of n = 2184

- Q.9** The number of solutions of the equation  $\left(\frac{9}{x} - \frac{9}{\sqrt{x}} + 2\right) \left(\frac{2}{x} - \frac{7}{\sqrt{x}} + 3\right) = 0$  is :  
 (1) 2 (2) 4 (3) 1 (4) 3

**Ans.** [2]

**Sol.** Consider  $\frac{1}{\sqrt{x}} = \alpha$   $\boxed{x > 0}$

$$\{9\alpha^2 - 9\alpha + 2\} \{2\alpha^2 - 7\alpha + 3\} = 0$$

$$(3\alpha - 2)(3\alpha - 1)(\alpha - 3)(2\alpha - 1) = 0$$

$$\alpha = \frac{1}{3}, \frac{1}{2}, \frac{2}{3}, 3$$

$$x = 9, 4, \frac{9}{4}, \frac{1}{9}$$

So, no. of solutions = 4

**Q.10** Let  $y = y(x)$  be the solution of the differential equation  $\cos x (\log_e(\cos x))^2 dy + (\sin x - 3y \sin x \log_e(\cos x)) dx = 0$ ,

$x \in \left(0, \frac{\pi}{2}\right)$ . If  $y\left(\frac{\pi}{4}\right) = \frac{-1}{\log_e 2}$ , then  $y\left(\frac{\pi}{6}\right)$  is :

(1)  $\frac{2}{\log_e(3) - \log_e(4)}$

(2)  $\frac{1}{\log_e(4) - \log_e(3)}$

(3)  $-\frac{1}{\log_e(4)}$

(4)  $\frac{1}{\log_e(3) - \log_e(4)}$

**Ans.** [4]

**Sol.**  $\cos x (\ln(\cos x))^2 dy + (\sin x - 3y (\sin x) \ln(\cos x)) dx = 0$

$$\cos x (\ln(\cos x))^2 \frac{dy}{dx} - 3 \sin x \cdot \ln(\cos x) y = -\sin x$$

$$\frac{dy}{dx} - \frac{3 \tan x}{\ln(\cos x)} y = \frac{-\tan x}{(\ln(\cos x))^2}$$

$$\frac{dy}{dx} + \frac{3 \tan x}{\ln(\sec x)} y = \frac{-\tan x}{(\ln(\sec x))^2}$$

$$\text{I.F.} = e^{\int \frac{3 \tan x}{\ln(\sec x)} dx} = (\ln(\sec x))^3$$

$$y \times (\ln(\sec x))^3 = - \int \frac{\tan x}{(\ln(\sec x))^2} (\ln(\sec x))^3 dx + C$$

$$y \times (\ln(\sec x))^3 = -\frac{1}{2} (\ln(\sec x))^2 + C$$

Given :  $x = \frac{\pi}{4}, y = -\frac{1}{\ln 2}$

$$\frac{-1}{\ln 2} \times (\ln \sqrt{2})^3 = -\frac{1}{2} \times (\ln \sqrt{2})^2 + C$$

$$\Rightarrow \frac{-1}{8 \ln 2} \times (\ln 2)^3 = \frac{-1}{2} \times \frac{1}{4} (\ln 2)^2 + C$$

$$-\frac{1}{8} (\ln 2)^2 = \frac{-1}{8} (\ln 2)^2 + C$$

$$\Rightarrow C = 0$$

$$\therefore y (\ln(\sec x))^3 = \frac{-1}{2} (\ln(\sec x))^2 + 0$$

$$y = \frac{-1}{2 \ln(\sec x)}$$

$$y = \frac{1}{2 \ln(\cos x)}$$

$$\therefore y\left(\frac{\pi}{6}\right) = \frac{1}{2 \ln\left(\cos \frac{\pi}{6}\right)} = \frac{1}{2 \ln\left(\frac{\sqrt{3}}{2}\right)}$$

$$= \frac{1}{2\left(\frac{1}{2} \ln 3 - \ln 2\right)} = \frac{1}{\ln 3 - \ln 4} \quad \text{Option (4)}$$

**Q.11** Define a relation R on the interval  $\left[0, \frac{\pi}{2}\right)$  by  $x R y$  if and only if  $\sec^2 x - \tan^2 y = 1$ . Then R is :

- (1) an equivalence relation
- (2) both reflexive and transitive but not symmetric
- (3) both reflexive and symmetric but not transitive
- (4) reflexive but neither symmetric nor transitive

**Ans.** [1]

**Sol.**  $\sec^2 x - \tan^2 x = 1$  (on replacing y with x)

$\Rightarrow$  Reflexive

$$\sec^2 x - \tan^2 y = 1$$

$$\Rightarrow 1 + \tan^2 x + 1 - \sec^2 y = 1$$

$$\Rightarrow \sec^2 y - \tan^2 x = 1$$

$\Rightarrow$  symmetric

$$\sec^2 x - \tan^2 y = 1,$$

$$\sec^2 y - \tan^2 z = 1$$

Adding both

$$\Rightarrow \sec^2 x - \tan^2 y + \sec^2 y - \tan^2 z = 1 + 1$$

$$\sec^2 x + 1 - \tan^2 z = 2$$

$$\sec^2 x - \tan^2 z = 1$$

$\Rightarrow$  Transitive

hence equivalence relation

**Option (1)**

**Q.12** Let the ellipse,  $E_1 : \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ ,  $a > b$  and  $E_2 : \frac{x^2}{A^2} + \frac{y^2}{B^2} = 1$ ,  $A < B$  have same eccentricity  $\frac{1}{\sqrt{3}}$ . Let the

product of their lengths of latus rectums be  $\frac{32}{\sqrt{3}}$ , and the distance between the foci of  $E_1$  be 4. If  $E_1$  and  $E_2$

meet at A, B, C and D, then the area of the quadrilateral ABCD equals :

- (1)  $6\sqrt{6}$                       (2)  $\frac{18\sqrt{6}}{5}$                       (3)  $\frac{12\sqrt{6}}{5}$                       (4)  $\frac{24\sqrt{6}}{5}$

**Ans.** [4]

**Sol.**

$$2ae = 4$$

$$2a \left( \frac{1}{\sqrt{3}} \right) = 4$$

$$\Rightarrow a = 2\sqrt{3}$$

$$\Rightarrow 1 - \frac{b^2}{12} = \frac{1}{3} \Rightarrow b^2 = 8$$

$$\text{Now } \frac{2b^2}{a} \cdot \frac{2A^2}{B} = \frac{32}{\sqrt{3}} \Rightarrow 2 \left( \frac{8}{2\sqrt{3}} \right) \frac{2A^2}{B} = \frac{32}{\sqrt{3}}$$

$$\Rightarrow A^2 = 2B$$

$$1 - \frac{A^2}{B^2} = \frac{1}{3} \Rightarrow 1 - \frac{2B}{B^2} = \frac{1}{3} \Rightarrow B = 3$$

$$\Rightarrow A^2 = 6$$

$$\frac{x^2}{12} + \frac{y^2}{8} = 1 \quad \dots(1)$$

$$\frac{x^2}{6} + \frac{y^2}{9} = 1 \quad \dots(2)$$

On solving (1) & (2) we get

$$(x, y) \equiv \left( \frac{\sqrt{6}}{\sqrt{5}}, \frac{6}{\sqrt{5}} \right), \left( \frac{-\sqrt{6}}{\sqrt{5}}, \frac{6}{\sqrt{5}} \right), \left( \frac{\sqrt{6}}{\sqrt{5}}, \frac{-6}{\sqrt{5}} \right), \left( \frac{-\sqrt{6}}{\sqrt{5}}, \frac{-6}{\sqrt{5}} \right)$$

The four points are vertices of rectangle and its area =  $\frac{24\sqrt{6}}{5}$

**Q.13** Consider an A.P. of positive integers, whose sum of the first three terms is 54 and the sum of the first twenty terms lies between 1600 and 1800. Then its 11<sup>th</sup> term is :

- (1) 84                                      (2) 122                                      (3) 90                                      (4) 108

**Ans.** [3]

**Sol.**  $S_3 = 3a + 3d = 54$

$$\Rightarrow a + d = 18$$

$$S_{20} = 10(2a + 19d)$$

$$\Rightarrow 10(36 + 17d)$$

$$\Rightarrow 1600 < 10(36 + 17d) < 1800$$

$$\Rightarrow 160 < 36 + 17d < 180$$

$$\Rightarrow 124 < 17d < 144$$

$$\Rightarrow 7\frac{5}{17} < d < 8\frac{8}{17}$$

Common difference will be natural number

$$\Rightarrow d = 8 \Rightarrow a = 10$$

$$\Rightarrow a_{11} = 10 + 10 \times 8 = 90$$

**Q.14** Let  $\vec{a} = \hat{i} + 2\hat{j} + \hat{k}$  and  $\vec{b} = 2\hat{i} + 7\hat{j} + 3\hat{k}$ . Let  $L_1: \vec{r} = (-\hat{i} + 2\hat{j} + \hat{k}) + \lambda \vec{a}$ ,  $\lambda \in \mathbb{R}$  and  $L_2: \vec{r} = (\hat{j} + \hat{k}) + \mu \vec{b}$ ,  $\mu \in \mathbb{R}$  be two lines. If the line  $L_3$  passes through the point of intersection of  $L_1$  and  $L_2$ , and is parallel to  $\vec{a} + \vec{b}$  then  $L_3$  passes through the point :

- (1) (8, 26, 12)                              (2) (2, 8, 5)                              (3) (-1, -1, 1)                              (4) (5, 17, 4)

**Ans.** [1]

**Sol.**  $L_1: \vec{r} = (-\hat{i} + 2\hat{j} + \hat{k}) + \lambda (\hat{i} + 2\hat{j} + \hat{k})$

$$\Rightarrow \vec{r} = (\lambda - 1) \hat{i} + 2(\lambda + 1) \hat{j} + (\lambda + 1) \hat{k}$$

$$L_2: \vec{r} = (\hat{j} + \hat{k}) + \mu(2\hat{i} + 7\hat{j} + 3\hat{k})$$

$$\Rightarrow \vec{r} = 2\mu \hat{i} + (1 + 7\mu) \hat{j} + (1 + 3\mu) \hat{k}$$

For point of intersection equating respective components

$$\Rightarrow \lambda - 1 = 2\mu \quad \dots(1)$$

$$2(\lambda + 1) = 1 + 7\mu \quad \dots(2)$$

$$\lambda + 1 = 1 + 3\mu \quad \dots(3)$$



We get

$$\Rightarrow \lambda = 3 \text{ and } \mu = 1$$

$$\Rightarrow \vec{a} + \vec{b} = 3\hat{i} + 9\hat{j} + 4\hat{k}$$

$$L_3 : \vec{r} = 2\hat{i} + 8\hat{j} + 4\hat{k} + \alpha(3\hat{i} + 9\hat{j} + 4\hat{k})$$

$$\text{For } \alpha = 2, \vec{r} = 8\hat{i} + 26\hat{j} + 12\hat{k}$$

**Q.15** The value of  $\lim_{n \rightarrow \infty} \left( \sum_{k=1}^n \frac{k^3 + 6k^2 + 11k + 5}{(k+3)!} \right)$  is :

(1)  $\frac{4}{3}$

(2) 2

(3)  $\frac{7}{3}$

(4)  $\frac{5}{3}$

**Ans.** [4]

**Sol.**

$$\begin{aligned} \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{k^3 + 6k^2 + 11k + 5}{(k+3)!} &= \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{k^3 + 6k^2 + 11k + 6 - 1}{(k+3)!} \\ &= \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{(k+1)(k+2)(k+3) - 1}{(k+3)!} \\ &= \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{(k+1)(k+2)(k+3)}{(k+3)!} - \frac{1}{(k+3)!} \\ &= \lim_{k=1}^n \left( \frac{1}{k!} - \frac{1}{(k+3)!} \right) \\ &= \lim_{k=1} \left( \frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \frac{1}{4!} \dots + \frac{1}{n!} - \frac{1}{4!} - \frac{1}{5!} - \frac{1}{6!} \dots - \frac{1}{(n+3)!} \right) \\ &= \frac{1}{1} + \frac{1}{2} + \frac{1}{6} = \frac{10}{6} = \frac{5}{3} \end{aligned}$$

**Q.16** The integral  $80 \int_0^{\frac{\pi}{4}} \left( \frac{\sin \theta + \cos \theta}{9 + 16 \sin 2\theta} \right) d\theta$  is equal to :

(1)  $3 \log_e 4$

(2)  $6 \log_e 4$

(3)  $4 \log_e 3$

(4)  $2 \log_e 3$

**Ans.** [3]

**Sol.**

$$\begin{aligned} I &= 80 \int_0^{\frac{\pi}{4}} \left( \frac{\sin \theta + \cos \theta}{9 + 16(2 \sin \theta \cdot \cos \theta)} \right) d\theta \\ &= 80 \int_0^{\frac{\pi}{4}} \frac{\sin \theta + \cos \theta}{9 - 16(1 - 2 \sin \theta \cdot \cos \theta - 1)} d\theta \\ &= 80 \int_0^{\frac{\pi}{4}} \frac{\sin \theta + \cos \theta}{9 + 16 - 16(\sin \theta - \cos \theta)^2} d\theta \end{aligned}$$





**Sol.**  $|A| = \frac{11}{2}$

$$C_{11} = \sum_{k=1}^2 a_{1k} \cdot A_{1k} = a_{11}A_{11} + a_{12}A_{12} = |A| = \frac{11}{2}$$
$$C_{12} = \sum_{k=1}^2 a_{1k} \cdot A_{2k} = 0$$
$$C_{21} = \sum_{k=1}^2 a_{2k} \cdot A_{1k} = 0$$
$$C_{22} = \sum_{k=1}^2 a_{2k} \cdot A_{2k} = |A| = \frac{11}{2}$$
$$C = \begin{bmatrix} 11/2 & 0 \\ 0 & 11/2 \end{bmatrix}$$
$$|C| = \frac{121}{4}$$
$$8|C| = 242$$

**Section-B: Numerical Value Type Questions:** This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

**Q.21** Let  $f : (0, \infty) \rightarrow \mathbb{R}$  be a twice differentiable function. If for some  $a \neq 0$ ,  $\int_0^1 f(\lambda x) d\lambda = af(x)$ ,  $f(1) = 1$  and  $f(16) = \frac{1}{8}$ , then  $16 - f' \left( \frac{1}{16} \right)$  is equal to .....

**Ans.** [112]

**Sol.**  $\int_0^1 f(\lambda x) d\lambda = af(x)$

$$\lambda x = t$$

$$d\lambda = \frac{1}{x} dt$$

$$\frac{1}{x} \int_0^x f(t) dt = af(x)$$

$$\int_0^x f(t) dt = axf(x)$$

differentiating both sides

$$f(x) = a(xf'(x) + f(x))$$

$$(1 - a) f(x) = a \cdot x f'(x)$$

$$\frac{f'(x)}{f(x)} = \frac{(1-a)}{a} \cdot \frac{1}{x}$$

$$\ln f(x) = \frac{1-a}{a} \ln x + c$$

$$x = 1, f(1) = 1 \Rightarrow c = 0$$

$$x = 16, f(16) = \frac{1}{8}$$

$$\frac{1}{8} = (16)^{\frac{1-a}{a}} \Rightarrow -3 = \frac{4-4a}{a} \Rightarrow a = 4$$

$$f(x) = x^{-\frac{3}{4}}$$

$$f'(x) = -\frac{3}{4}x^{-\frac{7}{4}}$$

$$\therefore 16 - f'\left(\frac{1}{16}\right)$$

$$= 16 - \left(-\frac{3}{4}(2^{-4})^{-7/4}\right)$$

$$= 16 + 96 = 112$$

**Q.22** Let  $S = \{m \in \mathbb{Z} : A^{m^2} + A^m = 3I - A^{-6}\}$ , where  $A = \begin{bmatrix} 2 & -1 \\ 1 & 0 \end{bmatrix}$ . Then  $n(S)$  is equal to .....

**Ans.** [2]

**Sol.**  $A = \begin{bmatrix} 2 & -1 \\ 1 & 0 \end{bmatrix}$

$$A^2 = \begin{bmatrix} 3 & -2 \\ 2 & -1 \end{bmatrix}, A^3 = \begin{bmatrix} 4 & -3 \\ 3 & -2 \end{bmatrix}, A^4 = \begin{bmatrix} 5 & -4 \\ 4 & -3 \end{bmatrix}$$

and so on

$$A^6 = \begin{bmatrix} 7 & -6 \\ 6 & -5 \end{bmatrix}$$

$$A^m = \begin{bmatrix} m+1 & -m \\ m & -(m-1) \end{bmatrix},$$

$$A^{m^2} = \begin{bmatrix} m^2+1 & -m^2 \\ m^2 & -(m^2-1) \end{bmatrix}$$

$$A^{m^2} + A^m = 3I - A^{-6}$$

$$\begin{bmatrix} m^2+1 & -m^2 \\ m^2 & -(m^2-1) \end{bmatrix} + \begin{bmatrix} m+1 & -m \\ m & -(m-1) \end{bmatrix}$$

$$= 3 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} -5 & 6 \\ -6 & 7 \end{bmatrix}$$

$$= \begin{bmatrix} 8 & -6 \\ 6 & -4 \end{bmatrix}$$

$$= m^2 + 1 + m + 1 = 8$$

$$= m^2 + m - 6 = 0 \Rightarrow m = -3, 2$$

$$n(s) = 2$$

**Q.23** Let  $[t]$  be the greatest integer less than or equal to  $t$ . Then the least value of  $p \in \mathbb{N}$  for which

$$\lim_{x \rightarrow 0^+} \left( x \left( \left[ \frac{1}{x} \right] + \left[ \frac{2}{x} \right] + \dots + \left[ \frac{p}{x} \right] \right) - x^2 \left( \left[ \frac{1}{x^2} \right] + \left[ \frac{2^2}{x^2} \right] + \dots + \left[ \frac{9^2}{x^2} \right] \right) \right) \geq 1$$

is equal to \_\_\_\_.

**Ans.** [24]

**Sol.** 
$$\lim_{x \rightarrow 0^+} \left( x \left( \left[ \frac{1}{x} \right] + \left[ \frac{2}{x} \right] + \dots + \left[ \frac{p}{x} \right] \right) - x^2 \left( \left[ \frac{1}{x^2} \right] + \left[ \frac{2^2}{x^2} \right] + \dots + \left[ \frac{9^2}{x^2} \right] \right) \right) \geq 1$$

$$(1 + 2 + \dots + p) - (1^2 + 2^2 + \dots + 9^2) \geq 1$$

$$\frac{p(p+1)}{2} - \frac{9 \cdot 10 \cdot 19}{6} \geq 1$$

$$P(p+1) \geq 572$$

Least natural value of  $p$  is 24

**Q.24** The number of 6-letter words, with or without meaning, that can be formed using the letters of the word 'MATHS' such that any letter that appears in the word must appear at least twice, is \_\_\_\_.

**Ans.** [1405]

**Sol.** (i) Single letter is used, then no. of words = 5

(ii) Two distinct letters are used, then no. of words

$${}^5C_2 \times \left( \frac{6!}{2!4!} \times 2 + \frac{6!}{3!3!} \right) = 10(30 + 20) = 500$$

(iii) Three distinct letters are used, then no. of words

$${}^5C_3 \times \frac{6!}{2!2!2!} = 900$$

Total no. of words = 1405

**Q.25** Let  $S = \{x : \cos^{-1}x = \pi + \sin^{-1}x + \sin^{-1}(2x+1)\}$ . Then  $\sum_{x \in S} (2x-1)^2$  is equal to .....

**Ans.** [5]

**Sol.**  $\cos^{-1}x = \pi + \sin^{-1}x + \sin^{-1}(2x+1)$

$$2\cos^{-1}x - \sin^{-1}(2x+1) = \frac{3\pi}{2}$$

$$2\alpha - \beta = \frac{3\pi}{2} \text{ where } \cos^{-1}x = \alpha, \sin^{-1}(2x+1) = \beta$$

$$2\alpha = \frac{3\pi}{2} + \beta$$

$$\cos 2\alpha = \sin \beta$$

$$2 \cos^2 \alpha - 1 = \sin \beta$$

$$2x^2 - 1 = 2x + 1$$

$$x^2 - x - 1 = 0$$

$$\Rightarrow n = \frac{1 \pm \sqrt{5}}{2} = \begin{cases} n = \frac{1 + \sqrt{5}}{2} \text{ rejected} \\ n = \frac{1 - \sqrt{5}}{2} \end{cases}$$

$$\therefore \begin{aligned} 4x^3 - 4x &= 4 \\ (2x-1)^2 &= 5 \end{aligned}$$

## PHYSICS

**Section-A:** This section contains 20 multiple choice questions. Each question has 4 choices(1), (2), (3) and (4), out of which **ONLY ONE** is correct..

**Q.26** Given below are two statements : one is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.  
**Assertion (A) :** Choke coil is simply a coil having a large inductance but a small resistance. Choke coils are used with fluorescent mercury-tube fittings. If household electric power is directly connected to a mercury tube, the tube will be damaged.

**Reason (R) :** By using the choke coil, the voltage across the tube is reduced by a factor  $(R/\sqrt{R^2 + \omega^2 L^2})$ , where  $\omega$  is frequency of the supply across resistor R and inductor L. If the choke coil were not used, the voltage across the resistor would be the same as the applied voltage.

In the light of the above statements, choose the **most appropriate answer** from the options given below :

- (1) Both (A) and (R) are true but (R) is not the correct explanation of (A).  
(2) (A) is false but (R) is true.  
(3) Both (A) and (R) are true and (R) is the correct explanation of (A).  
(4) (A) is true but (R) is false.

**Ans.** [3]

**Sol.** A: Correct

B : Correct with correct explanation

**Q.27** Two projectiles are fired with same initial speed from same point on ground at angles of  $(45^\circ - \alpha)$  and  $(45^\circ + \alpha)$ , respectively, with the horizontal direction. The ratio of their maximum heights attained is :

- (1)  $\frac{1 - \tan \alpha}{1 + \tan \alpha}$                       (2)  $\frac{1 + \sin \alpha}{1 - \sin \alpha}$                       (3)  $\frac{1 - \sin 2\alpha}{1 + \sin 2\alpha}$                       (4)  $\frac{1 + \sin 2\alpha}{1 - \sin 2\alpha}$

**Ans.** [3]

**Sol.**  $H_{\max} = \frac{(u \sin \theta)^2}{2g}$

$$\frac{(H_{\max})_1}{(H_{\max})_2} = \frac{u^2 \sin^2(45 - \alpha)}{u^2 \sin^2(45 + \alpha)}$$

$$= \frac{\left(\frac{1}{\sqrt{2}} \cos \alpha - \frac{1}{\sqrt{2}} \sin \alpha\right)^2}{\left(\frac{1}{\sqrt{2}} \cos \alpha + \frac{1}{\sqrt{2}} \sin \alpha\right)^2}$$

$$= \frac{1 - \sin 2\alpha}{1 + \sin 2\alpha}$$

**Q.28** An electric dipole of mass m, charge q, and length  $\ell$  is placed in a uniform electric field  $\vec{E} = E_0 \hat{i}$ . When the dipole is rotated slightly from its equilibrium position and released, the time period of its oscillations will be :

- (1)  $\frac{1}{2\pi} \sqrt{\frac{2m\ell}{qE_0}}$                       (2)  $2\pi \sqrt{\frac{m\ell}{qE_0}}$                       (3)  $\frac{1}{2\pi} \sqrt{\frac{m\ell}{2qE_0}}$                       (4)  $2\pi \sqrt{\frac{m\ell}{2qE_0}}$

**Ans.** [4]

**Sol.**  $I\omega^2\theta = q\ell E_0\theta$

$$2m\left(\frac{\ell}{2}\right)^2 \omega^2 = q\ell E_0$$

$$\omega^2 = \frac{2qE_0}{m\ell}$$

$$T = 2\pi \sqrt{\frac{m\ell}{2qE_0}}$$

**Q.29** The pair of physical quantities not having same dimensions is :

- (1) Torque and energy
- (2) Surface tension and impulse
- (3) Angular momentum and Planck's constant
- (4) Pressure and Young's modulus

**Ans.** [2]

**Sol.**  $[\tau] = [E]$

$[\sigma] \neq [I]$

$[L] = [h]$

$[P] = [Y]$

**Q.30** Given below are two statements : one is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.  
**Assertion (A)** : Time period of a simple pendulum is longer at the top of a mountain than that at the base of the mountain.

**Reason (R)** : Time period of a simple pendulum decreases with increasing value of acceleration due to gravity and vice-versa.

In the light of the above statements, choose the **most appropriate answer** from the options given below :

- (1) Both (A) and (R) are true but (R) is not the correct explanation of (A).
- (2) Both (A) and (R) are true and (R) is the correct explanation of (A).
- (3) (A) is true but (R) is false.
- (4) (A) is false but (R) is true.

**Ans.** [2]

**Sol.** As h increases, g decreases, T increases

$$T = 2\pi \sqrt{\frac{\ell}{g}}$$

$$g = \frac{g_0 R^2}{(R+h)^2}$$

**Q.31** The expression given below shows the variation of velocity (v) with time (t),  $v = At^2 + \frac{Bt}{C+t}$ . The dimension of ABC is :

- (1)  $[M^0L^2T^{-3}]$                       (2)  $[M^0L^1T^{-3}]$                       (3)  $[M^0L^1T^{-2}]$                       (4)  $[M^0L^2T^{-2}]$

**Ans.** [1]

**Sol.**  $[LT^{-1}] = [A] [T^2] = \frac{[B][T]}{[C]+[T]}$

$[C] = [T]$

$[A] = [LT^{-3}]$

$[B] = [LT^{-1}]$

$[ABC] = [L^2T^{-3}]$



**Q.32** Consider  $I_1$  and  $I_2$  are the currents flowing simultaneously in two nearby coils 1 & 2, respectively. If  $L_1$  = self inductance of coil 1,  $M_{12}$  = mutual inductance of coil 1 with respect to coil 2, then the value of induced emf in coil 1 will be :

$$(1) \varepsilon_1 = -L_1 \frac{dI_1}{dt} + M_{12} \frac{dI_2}{dt}$$

$$(2) \varepsilon_1 = -L_1 \frac{dI_1}{dt} - M_{12} \frac{dI_1}{dt}$$

$$(3) \varepsilon_1 = -L_1 \frac{dI_1}{dt} - M_{12} \frac{dI_2}{dt}$$

$$(4) \varepsilon_1 = -L_1 \frac{dI_2}{dt} - M_{12} \frac{dI_1}{dt}$$

**Ans.** [3]

**Sol.**  $\phi_1 = L_1 I_1 + M_{12} I_2$

$$\varepsilon_1 = -\frac{d\phi_1}{dt} = -L_1 \frac{dI_1}{dt} - M_{12} \frac{dI_2}{dt}$$

**Q.33** At the interface between two materials having refractive indices  $n_1$  and  $n_2$ , the critical angle for reflection of an em wave is  $\theta_{1C}$ . The  $n_2$  material is replaced by another material having refractive index  $n_3$ , such that the critical angle at the interface between  $n_1$  and  $n_3$  materials is  $\theta_{2C}$ . If  $n_3 > n_2 > n_1$ ;  $\frac{n_2}{n_3} = \frac{2}{5}$  and  $\sin\theta_{2C} - \sin\theta_{1C} = \frac{1}{2}$ ,

then  $\theta_{1C}$  is :

$$(1) \sin^{-1}\left(\frac{1}{6n_1}\right)$$

$$(2) \sin^{-1}\left(\frac{2}{3n_1}\right)$$

$$(3) \sin^{-1}\left(\frac{5}{6n_1}\right)$$

$$(4) \sin^{-1}\left(\frac{1}{3n_1}\right)$$

**Ans.** [Bonus]

**Sol.**  $\sin\theta_{1C} = \frac{n_1}{n_2}$

$$\sin\theta_{2C} = \frac{n_1}{n_3}$$

$$\sin\theta_{2C} - \sin\theta_{1C} = \frac{1}{2}$$

$$n_1 \frac{n_2}{n_3} - n_1 = \frac{n_2}{2}$$

$$n_1 \left(\frac{2}{5} - 1\right) = \frac{n_2}{2}$$

$$\frac{n_1}{n_2} = \frac{-5}{6}$$

$$= \sin^{-1}\left(\frac{-5}{6}\right)$$

**Q.34** Consider a long straight wire of a circular cross-section (radius  $a$ ) carrying a steady current  $I$ . The current is uniformly distributed across this cross-section. The distances from the centre of the wire's cross-section at which the magnetic field [inside the wire, outside the wire] is half of the maximum possible magnetic field, any where due to the wire, will be :

$$(1) [a/4, 3a/2]$$

$$(2) [a/2, 2a]$$

$$(3) [a/2, 3a]$$

$$(4) [a/4, 2a]$$

**Ans.** [2]

**Sol.** Maximum possible magnetic field is at the surface

$$B_{\max} = \frac{\mu_0 I}{2\pi a}$$

$$\frac{B_{\max}}{2} = \frac{\mu_0 I}{4\pi a}$$

It can be obtained inside as well as outside the wire

For inside,

$$\frac{\mu_0 I}{4\pi a} = \frac{\mu_0 I r}{2\pi a^2}$$

$$\Rightarrow r = \frac{a}{2}$$

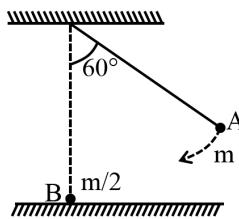
For outside

$$\frac{\mu_0 I}{4\pi a} = \frac{\mu_0 I}{2\pi r}$$

$$\Rightarrow r = 2a$$

Correct answer  $\left[ \frac{a}{2}, 2a \right]$

**Q.35** As shown below, bob A of a pendulum having massless string of length 'R' is released from  $60^\circ$  to the vertical. It hits another bob B of half the mass that is at rest on a friction less table in the centre. Assuming elastic collision, the magnitude of the velocity of bob A after the collision will be (take g as acceleration due to gravity)



(1)  $\frac{1}{3} \sqrt{Rg}$

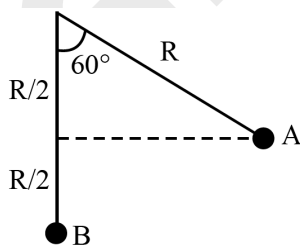
(2)  $\sqrt{Rg}$

(3)  $\frac{4}{3} \sqrt{Rg}$

(4)  $\frac{2}{3} \sqrt{Rg}$

**Ans.** [1]

**Sol.**



Velocity of a just before hitting :

$$u = \sqrt{2g \frac{R}{2}} = \sqrt{gR}$$

Just after collision, let velocity of A and B are  $v_1$  and  $v_2$  respectively

∴ by COM :

$$mu = mv_1 + \frac{m}{2}v_2$$

$$2v_1 + v_2 = 2u \quad \dots(i)$$

$$e = 1 = \frac{v_2 - v_1}{u}$$

$$\Rightarrow v_2 - v_1 = u \quad \dots(ii)$$

From (i) –(ii)

$$\Rightarrow 3v_1 = u \Rightarrow v_1 = \frac{u}{3} = \frac{1}{3}\sqrt{gR}$$

**Q.36** Given below are two statements : one is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.  
**Assertion (A)** : Emission of electrons in photoelectric effect can be suppressed by applying a sufficiently negative electron potential to the photoemissive substance.

**Reason (R)** : A negative electric potential, which stops the emission of electrons from the surface of a photoemissive substance, varies linearly with frequency of incident radiation.

In the light of the above statements, choose the **most appropriate answer** from the options given below:

- (1) (A) is false but (R) is true.
- (2) (A) is true but (R) is false.
- (3) Both (A) and (R) are true and (R) is the correct explanation of (A).
- (4) Both (A) and (R) are true but (R) is not the correct explanation of (A).

**Ans.** [4]

**Sol.** (A) : True

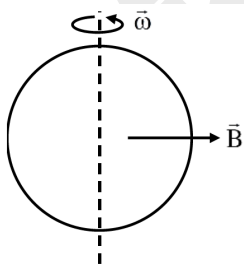
(B) : True but not correct explanation

**Q.37** A coil of area A and N turns is rotating with angular velocity  $\omega$  in a uniform magnetic field  $\vec{B}$  about an axis perpendicular to  $\vec{B}$ . Magnetic flux  $\phi$  and induced emf  $\varepsilon$  across it, at an instant when B is parallel to the plane of coil, are :

- |                                  |  |
|----------------------------------|--|
| (1) $\phi = AB, \varepsilon = 0$ | (2) $\phi = 0, \varepsilon = NAB\omega$  |
| (3) $\phi = 0, \varepsilon = 0$  | (4) $\phi = AB, \varepsilon = NAB\omega$ |

**Ans.** [2]

**Sol.**



$$\phi = BAN \cdot \cos(\omega t)$$

$$\varepsilon = \frac{-d\phi}{dt} = BA\omega N \cdot \sin(\omega t)$$

When B is parallel to plane,  $\omega t = \frac{\pi}{2}$

$$\Rightarrow \phi = 0, \varepsilon = BA\omega N$$



**Q.41** A body of mass 'm' connected to a massless and unstretchable string goes in verticle circle of radius 'R' under gravity g. The other end of the string is fixed at the center of circle. If velocity at top of circular path is  $n\sqrt{gR}$ , where,  $n \geq 1$ , then ratio of kinetic energy of the body at bottom to that at top of the circle is :

- (1)  $\frac{n}{n+4}$                       (2)  $\frac{n+4}{n}$                       (3)  $\frac{n^2}{n^2+4}$                       (4)  $\frac{n^2+4}{n^2}$

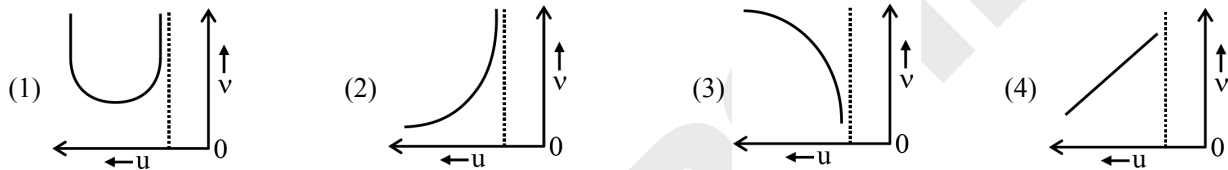
**Ans.** [4]

**Sol.**  $V_{\text{Top}} = \sqrt{n^2 gR}$

$V_{\text{Bottom}} = \sqrt{n^2 gR + 4gR}$

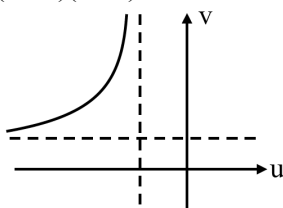
Ratio =  $\frac{n^2 + 4}{n^2}$

**Q.42** Let u and v be the distances of the object and the image from a lens of focal length f. The correct graphical representation of u and v for a convex lens when  $|u| > f$ , is :



**Ans.** [2]

**Sol.**  $(u + f)(v - f) = f^2$



**Q.43** Match List-I with List-II.

List-I		List-II	
(A)	Electric field inside (distance $r > 0$ from center) of a uniformly charged spherical shell with surface charge density $\sigma$ , and radius R.	(I)	$\sigma / \epsilon_0$
(B)	Electric field at distance $r > 0$ from a uniformly charged infinite plane sheet with surface charge density $\sigma$ .	(II)	$\sigma / 2\epsilon_0$
(C)	Electric field outside (distance $r > 0$ from center) of a uniformly charged spherical shell with surface charge density $\sigma$ , and radius R	(III)	0
(D)	Electric field between 2 oppositely charged infinite plane parallel sheets with uniform surface charge density $\sigma$ .	(IV)	$\frac{\sigma}{\epsilon_0 r^2}$

Choose the correct answer from the options given below :

- (1) (A)-(IV), (B)-(I), (C)-(III), (D)-(II)                      (2) (A)-(IV), (B)-(II), (C)-(III), (D)-(I)  
 (3) (A)-(II), (B)-(I), (C)-(IV), (D)-(III)                      (4) (A)-(III), (B)-(II), (C)-(IV), (D)-(I)

**Ans.** [Bonus]

- Sol. (A)  $\rightarrow 0$  (III)  
(B)  $\rightarrow \frac{\sigma}{2\epsilon_0}$  (II)  
(C)  $\rightarrow \frac{\sigma R^2}{\epsilon_0 r^2}$  (No row matching)  
(D)  $\rightarrow \frac{\sigma}{\epsilon_0}$  (I)

- Q.44 The workdone in an adiabatic change in an ideal gas depends upon only :  
(1) change in its pressure (2) change in its specific heat  
(3) change in its volume (4) change in its temperature

Ans. [4]

Sol.  $\Delta W = -\Delta U = -nC_V\Delta T$

- Q.45 Given below are two statements : one is labelled as **Assertion (A)** and other is labelled as **Reason (R)**.

**Assertion (A)** : Electromagnetic waves carry energy but not momentum.

**Reason (R)** : Mass of a photon is zero.

In the light of the above statements, choose the **most appropriate answer** from the options given below :

- (1) (A) is true but (R) is false.  
(2) (A) is false but (R) is true.  
(3) Both (A) and (R) are true but (R) is not the correct explanation of (A).  
(4) Both (A) and (R) are true and (R) is the correct explanation of (A).

Ans. [2]

Sol. Assertion is false because em waves have momentum.

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**Section-B: Numerical Value Type Questions:** This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

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- Q.46 The coordinates of a particle with respect to origin in a given reference frame is (1, 1, 1) meters. If a force of  $\vec{F} = \hat{i} - \hat{j} + \hat{k}$  acts on the particle, then the magnitude of torque (with respect to origin) in z-direction is

Ans. [2]

Sol.  $\vec{\tau} = \vec{r} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 1 & 1 \\ 1 & -1 & 1 \end{vmatrix}$

$$\vec{\tau} = \hat{k}(-1 - 1) = -2\hat{k}$$

$$|\vec{\tau}| = 2 \text{ Nm}$$

- Q.47 A container of fixed volume contains a gas at 27°C. To double the pressure of the gas, the temperature of gas should be raised to \_\_\_\_\_ °C.

Ans. [327]

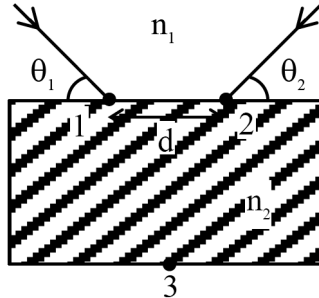
Sol.  $\frac{P_1}{T_1} = \frac{P_2}{T_2}$

$$\frac{P}{300} = \frac{2P}{T_2}$$

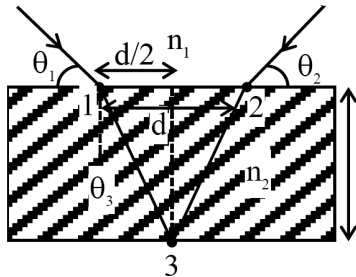
$$T_2 = 6000 \text{ K}$$

$$T_2 = 327^\circ\text{C}$$

- Q.48** Two light beams fall on a transparent material block at point 1 and 2 with angle  $\theta_1$  and  $\theta_2$ , respectively, as shown in figure. After refraction, the beams intersect at point 3 which is exactly on the interface at other end of the block. Given : the distance between 1 and 2,  $d = 4\sqrt{3}$  cm and  $\theta_1 = \theta_2 \cos^{-1} \left( \frac{n_2}{2n_1} \right)$ , where refractive index of the block  $n_2 >$  refractive index of the outside medium  $n_1$ , then the thickness of the block is \_\_\_\_\_ cm.



**Ans.** [6]  
**Sol.**



$$n_1 \sin(90 - \theta_1) = n_2 \sin \theta_3$$

$$n_1 \cos \theta_1 = n_2 \sin \theta_3$$

$$n_1 \frac{n_2}{2n_1} = n_2 \sin \theta_3$$

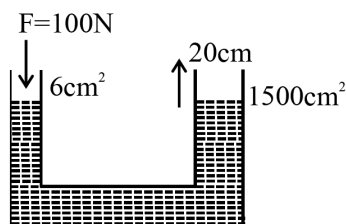
$$\frac{1}{2} = \sin \theta_3, \theta_3 = 30$$

$$\tan 30 = \frac{d}{2(t)}$$

$$t = \frac{d\sqrt{3}}{2} = \frac{4\sqrt{3} \times \sqrt{3}}{2} \text{ cm} = 6 \text{ cm}$$

- Q.49** In a hydraulic lift, the surface area of the input piston is  $6 \text{ cm}^2$  and that of the output piston is  $1500 \text{ cm}^2$ . If  $100 \text{ N}$  force is applied to the input piston to raise the output piston by  $20 \text{ cm}$ , then the work done is \_\_\_\_\_ kJ.

**Ans.** [5]  
**Sol.**



$$\frac{F_1}{A_1} = \frac{F_2}{A_2}, \frac{100}{6} = \frac{F}{1500}, F = \frac{50}{3} \times 1500$$

$$F = 50 \times 500 = 25 \times 10^3 \text{ N}$$

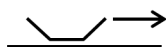
$$\omega = \vec{F} \cdot \vec{S} = 25 \times 10^3 \times \frac{20}{100}$$

$$= 5 \times 10^3 = 5 \text{ kJ}$$

**Q.50** The maximum speed of a boat in still water is 27 km/h. Now this boat is moving downstream in a river flowing at 9 km/h. A man in the boat throws a ball vertically upwards with speed of 10 m/s. Range of the ball as observed by an observer at rest on the river bank, is \_\_\_\_\_ cm.  
(Take  $g = 10 \text{ m/s}^2$ )

**Ans. [2000]**

**Sol.**  $\vec{v}_b = 9 + 27 = 36 \text{ km/hr}$



$$\vec{v}_b = 36 \times \frac{1000}{36000} = 10 \text{ m/sec}$$

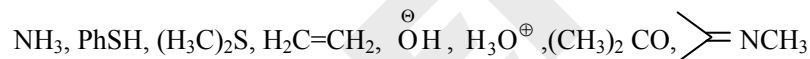
$$\text{Time of flight} = \frac{2 \times 10}{10} = 2 \text{ sec}$$

$$\text{Range} = 10 \times 2 = 20 \text{ m} = 2000 \text{ cm}$$

## CHEMISTRY

**Section-A:** This section contains 20 multiple choice questions. Each question has 4 choices(1), (2), (3) and (4), out of which **ONLY ONE** is correct..

**Q.51** Total number of nucleophiles from the following is :-



(1) 5

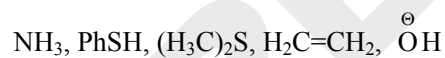
(2) 4

(3) 7

(4) 6

**Ans. [1]**

**Sol.** Total five nucleophiles are present



**Q.52** The standard reduction potential values of some of the p-block ions are given below. Predict the one with the strongest oxidising capacity.

(1)  $E_{\text{Sn}^{4+}/\text{Sn}^{2+}}^{\ominus} = +1.15\text{V}$

(2)  $E_{\text{Tl}^{3+}/\text{Tl}}^{\ominus} = +1.26\text{V}$

(3)  $E_{\text{Al}^{3+}/\text{Al}}^{\ominus} = -1.66\text{V}$

(4)  $E_{\text{Pb}^{4+}/\text{Pb}^{2+}}^{\ominus} = +1.67\text{V}$

**Ans. [4]**

**Sol.** Standard reduction potential value (+ve) increases oxidising capacity increases.

**Q.53** The molar conductivity of a weak electrolyte when plotted against the square root of its concentration, which of the following is expected to be observed ?

(1) A small decrease in molar conductivity is observed at infinite dilution.

(2) A small increase in molar conductivity is observed at infinite dilution.

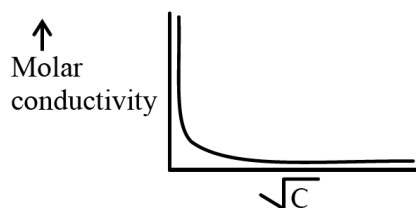
(3) Molar conductivity increases sharply with increase in concentration.

(4) Molar conductivity decreases sharply with increase in concentration.



Ans. [4]

Sol.



**Q.54** At temperature T, compound  $AB_{2(g)}$  dissociates as  $AB_{2(g)} \rightleftharpoons AB_{(g)} + \frac{1}{2}B_{2(g)}$  having degree of dissociation  $x$  (small compared to unity). The correct expression for  $x$  in terms of  $K_p$  and  $p$  is

- (1)  $\sqrt[3]{\frac{2K_p}{p}}$                       (2)  $\sqrt[4]{\frac{2K_p}{p}}$                       (3)  $\sqrt[3]{\frac{2K_p^2}{p}}$                       (4)  $\sqrt{K_p}$

Ans. [3]

 Sol.  $AB_{2(g)} \rightleftharpoons AB_{(g)} + \frac{1}{2}B_{2(g)}$ 

$$t_{eq} \cdot \frac{(1-x)p}{1+\frac{x}{2}} \cdot \frac{xP}{1+\frac{x}{2}} \cdot \left(\frac{x}{2}\right)^{\frac{1}{2}} P$$

$$\Rightarrow x \ll 1 \Rightarrow 1 + \frac{x}{2} \approx 1 \text{ and } 1 - x \approx 1$$

$$\Rightarrow k_p = \frac{(xp) \cdot \left(\frac{xp}{2}\right)^{\frac{1}{2}}}{P}$$

$$\Rightarrow k_p^2 = x^2 \cdot \frac{xP}{2}$$

$$x = \sqrt[3]{\frac{2k_p^2}{P}}$$

**Q.55** Match List-I with List-II.

	<b>List-I (Structure)</b>		<b>List-II (IUPAC Name)</b>
(A)	$\begin{array}{ccccccc} \text{CH}_3 & -\text{CH}_2 & -\text{CH} & -\text{CH}_2 & -\text{CH} & -\text{C}_2\text{H}_5 \\ & &   & &   & \\ & & \text{C}_2\text{H}_5 & & \text{CH}_3 & \end{array}$	(I)	4-Methylpent-1-ene
(B)	$(\text{CH}_3)_2\text{C}(\text{C}_3\text{H}_7)_2$	(II)	3-Ethyl-5-methylheptane
(C)		(III)	4,4-Dimethylheptane
(D)		(IV)	2-Methyl-1,3-pentadiene

Choose the correct answer from the options given below:

- (1) (A)-(III), (B)-(II), (C)-(IV), (D)-(I)                      (2) (A)-(III), (B)-(II), (C)-(I), (D)-(IV)  
 (3) (A)-(II), (B)-(III), (C)-(IV), (D)-(I)                      (4) (A)-(II), (B)-(III), (C)-(I), (D)-(IV)

Ans. [3]

- Sol. (A) 
$$\begin{array}{cccccccc} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \text{CH}_3 & -\text{CH}_2 & -\text{CH} & -\text{CH}_2 & -\text{CH} & -\text{CH}_2 & -\text{CH}_3 \\ & & | & & | & & \\ & & \text{CH}_2-\text{CH}_3 & & \text{CH}_3 & & \end{array}$$
  
 3-Ethyl-5-Methylheptane  
 $(\text{CH}_3)_2\text{C}(\text{C}_3\text{H}_7)_2$
- (B) 
$$\begin{array}{ccccccc} & & \text{CH}_3 & & & & \\ & & | & & & & \\ \text{CH}_3 & -\text{C} & -\text{CH}_2 & -\text{CH}_2 & -\text{CH}_3 & & \\ & | & & & & & \\ & \text{CH}_2 & -\text{CH}_2 & -\text{CH}_3 & & & \end{array}$$
 4,4-Dimethylheptane
- (C) 
$$\begin{array}{ccccccc} & & 2 & & 4 & & \\ & & | & & | & & \\ 1 & = & \text{C} & - & \text{C} & = & 5 \\ & & & & & & \end{array}$$
 2-Methyl-1, 3-pentadiene
- (D) 
$$\begin{array}{ccccccc} & & 2 & & 4 & & \\ & & | & & | & & \\ 1 & = & \text{C} & - & \text{C} & - & \text{C} & - & \text{C} & - & \text{C} \\ & & & & & & | & & & & \\ & & & & & & \text{CH}_3 & & & & \end{array}$$
 4-Methylpent-1-ene

**Q.56** Choose the correct statements.

- (A) Weight of a substance is the amount of matter present in it.  
 (B) Mass is the force exerted by gravity on an object.  
 (C) Volume is the amount of space occupied by a substance.  
 (D) Temperatures below  $0^\circ\text{C}$  are possible in Celsius scale, but in Kelvin scale negative temperature is not possible.  
 (E) Precision refers to the closeness of various measurements for the same quantity.
- (1) (B), (C) and (D) Only  
 (2) (A), (B) and (C) Only  
 (3) (A), (D) and (E) Only  
 (4) (C), (D) and (E) Only

**Ans.** [4]

**Sol.** Mass of substance is amount of matter present in it. Weight is force exerted by gravity on object.

**Q.57** The correct increasing order of stability of the complexes based on  $\Delta_o$  value is :

- (I)  $[\text{Mn}(\text{CN})_6]^{3-}$                       (II)  $[\text{Co}(\text{CN})_6]^{4-}$   
 (III)  $[\text{Fe}(\text{CN})_6]^{4-}$                       (IV)  $[\text{Fe}(\text{CN})_6]^{3-}$
- (1) II < III < I < IV  
 (2) IV < III < II < I  
 (3) I < II < IV < III  
 (4) III < II < IV < I

**Ans.** [3]

- Sol.** (I)  $[\text{Mn}(\text{CN})_6]^{3-}$                        $-1.6 \Delta_o$   
 (II)  $[\text{Co}(\text{CN})_6]^{4-}$                        $-1.8 \Delta_o$   
 (III)  $[\text{Fe}(\text{CN})_6]^{4-}$                        $-2.4 \Delta_o$   
 (IV)  $[\text{Fe}(\text{CN})_6]^{3-}$                        $-2.0 \Delta_o$
- I < II < IV < III

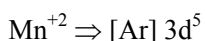
**Q.58** Match List-I with List-II.

List-I (Complex)		List-II (Hybridisation & Magnetic characters)	
(A)	$[\text{MnBr}_4]^{2-}$	(I)	$d^2 sp^3$ & diamagnetic
(B)	$[\text{FeF}_6]^{3-}$	(II)	$sp^3 d^2$ & paramagnetic
(C)	$[\text{Co}(\text{C}_2\text{O}_4)_3]^{3-}$	(III)	$sp^3$ & diamagnetic
(D)	$[\text{Ni}(\text{CO})_4]$	(IV)	$sp^3$ & paramagnetic

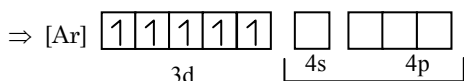
Choose the correct answer from the options given below :

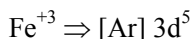
- (1) (A)-(III), (B)-(II), (C)-(I), (D)-(IV)
- (2) (A)-(III), (B)-(I), (C)-(II), (D)-(IV)
- (3) (A)-(IV), (B)-(I), (C)-(II), (D)-(III)
- (4) (A)-(IV), (B)-(II), (C)-(I), (D)-(III)

**Ans.** [4]

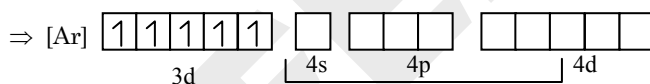
**Sol.** (A)  $[\text{MnBr}_4]^{2-}$ 


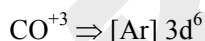
In presence of ligand field


 $\Rightarrow sp^3$  hybridization, paramagnetic in nature

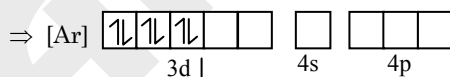
**(B)**  $[\text{FeF}_6]^{3-}$ 


In presence of ligand field


 $sp^3 d^2$  hybridization, paramagnetic in nature

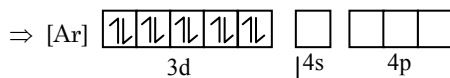
**(C)**  $[\text{Co}(\text{C}_2\text{O}_4)_3]^{3-}$ 


In presence of ligand field

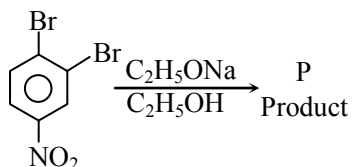

 $\Rightarrow d^2 sp^3$  hybridization, diamagnetic in nature

**(C)**  $[\text{Ni}(\text{CO})_4]$ 

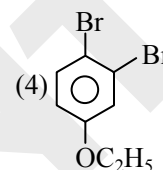
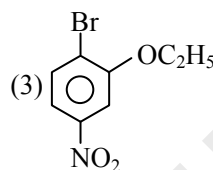
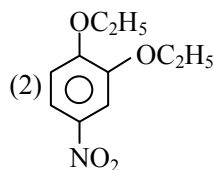
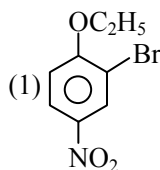

In presence of ligand field


 $\Rightarrow sp^3$  hybridization, diamagnetic in nature

**Q.59** In the following substitution reaction :

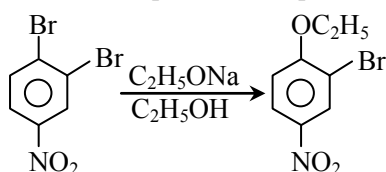


Product 'P' formed is :



**Ans.** [1]

**Sol.** It is an example of nucleophilic Aromatic substitution reaction.



**Q.60** For a  $\text{Mg} | \text{Mg}^{2+}(\text{aq}) || \text{Ag}^+(\text{aq}) | \text{Ag}$  the correct Nernst Equation is :

(1)  $E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{RT}{2F} \ln \frac{[\text{Ag}^+]}{[\text{Mg}^{2+}]}$

(2)  $E_{\text{cell}} = E_{\text{cell}}^{\circ} + \frac{RT}{2F} \ln \frac{[\text{Ag}^+]^2}{[\text{Mg}^{2+}]}$

(3)  $E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{RT}{2F} \ln \frac{[\text{Mg}^{2+}]}{[\text{Ag}^+]}$

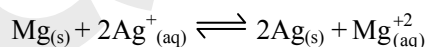
(4)  $E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{RT}{2F} \ln \frac{[\text{Ag}^+]^2}{[\text{Mg}^{2+}]}$

**Ans.** [2]

**Sol.** According to Nernst equation :-

$$E = E^{\circ} - \frac{RT}{nF} \ln Q.$$

Cell reaction :-



$$\Rightarrow Q = \frac{[\text{Mg}^{2+}]}{[\text{Ag}^+]^2}$$

$$\Rightarrow E = E_{\text{Cell}}^{\circ} - \frac{RT}{2F} \ln \left[ \frac{[\text{Mg}^{2+}]}{[\text{Ag}^+]^2} \right]$$

**Q.61** The correct option with order of melting points of the pairs (Mn, Fe), (Tc, Ru) and (Re, Os) is :

- (1) Fe < Mn, Ru < Tc and Re < Os
- (2) Mn < Fe, Tc < Ru and Re < Os
- (3) Mn < Fe, Tc < Ru and Os < Re
- (4) Fe < Mn, Ru < Tc and Os < Re

**Ans.** [3]

**Sol.** M.P.  $\Rightarrow$  Mn < Fe, Tc < Ru, Os < Re  
NCERT based

**Q.62** 1.24 g of AX<sub>2</sub> (molar mass 124 g mol<sup>-1</sup>) is dissolved in 1 kg of water to form a solution with boiling point of 100.0156°C, while 25.4 g of AY<sub>2</sub> (molar mass 250 g mol<sup>-1</sup>) in 2 kg of water constitutes a solution with a boiling point of 100.0260°C.

$$K_b(\text{H}_2\text{O}) = 0.52 \text{ K kg mol}^{-1}$$

Which of the following is correct ?

- (1) AX<sub>2</sub> and AY<sub>2</sub> (both) are completely unionised.
- (2) AX<sub>2</sub> and AY<sub>2</sub> (both) are fully ionised.
- (3) AX<sub>2</sub> is completely unionised while AY<sub>2</sub> is fully ionised.
- (4) AX<sub>2</sub> is fully ionised while AY<sub>2</sub> is completely unionised.

**Ans.** [4]

**Sol.** For AX<sub>2</sub> :-  $\Delta T_b = k_b \times m \times i$

$$0.0156 = 0.52 \times \frac{0.01}{1} \times i_{\text{AX}_2}$$

$$\Rightarrow i_{\text{AX}_2} = 3 \Rightarrow \text{complete ionisation}$$

For AY<sub>2</sub> :  $\Delta T_b = K_b \times m \times i$

$$0.026 = 0.52 \times 0.0508 \times i_{\text{AY}_2}$$

$$\Rightarrow i_{\text{AY}_2} \sim 1 \therefore \text{complete unionisation}$$

**Q.63** 500 J of energy is transferred as heat to 0.5 mol of Argon gas at 298 K and 1.00 atm. The final temperature and the change in internal energy respectively are :

Given : R = 8.3 J K<sup>-1</sup> mol<sup>-1</sup>

- |                     |                     |
|---------------------|---------------------|
| (1) 348 K and 300 J | (2) 378 K and 300 J |
| (3) 368 K and 500 J | (4) 378 K and 500 J |

**Ans.** [1]

**Sol.**  $q_p = n \times c_p \times \Delta T$

$$\Rightarrow 500 = 0.5 \times \frac{5}{2} \times 8.3 (T_f - 298)$$

$$\Rightarrow T_f \approx 346.2 \text{ K}$$

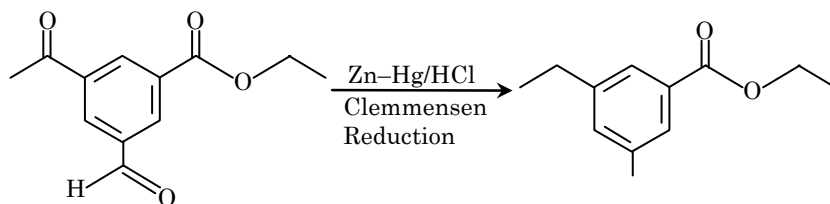
$$\frac{\Delta H}{\Delta U} = \frac{C_p}{C_v} = \left(\frac{5}{3}\right)$$

$$\Rightarrow \Delta U = \frac{3}{5} \times 500 = 300 \text{ J}$$



Ans. [3]

Sol.



**Q.67** An element 'E' has the ionisation enthalpy value of  $374 \text{ kJ mol}^{-1}$ . 'E' reacts with elements A, B, C and D with electron gain enthalpy values of  $-328$ ,  $-349$ ,  $-325$  and  $-295 \text{ kJ mol}^{-1}$ , respectively. The correct order of the products EA, EB, EC and ED in terms of ionic character is :

- (1)  $EB > EA > EC > ED$  (2)  $ED > EC > EA > EB$   
 (3)  $EA > EB > EC > ED$  (4)  $ED > EC > EB > EA$

Ans. [1]

Sol. Difference between I.E. & E.G.E increases, ionic character increases.

**Q.68** Match List – I with List – II.

List – I (Carbohydrate)		List – II (Linkage source)	
(A)	Amylose	(I)	$\beta$ -C <sub>1</sub> -C <sub>4</sub> , plant
(B)	Cellulose	(II)	$\alpha$ -C <sub>1</sub> -C <sub>4</sub> , animal
(C)	Glycogen	(III)	$\alpha$ -C <sub>1</sub> -C <sub>4</sub> , $\alpha$ -C <sub>1</sub> -C <sub>6</sub> , plant
(D)	Amylopectin	(IV)	$\alpha$ -C <sub>1</sub> -C <sub>4</sub> , plant

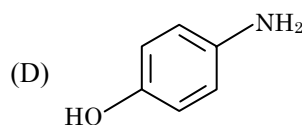
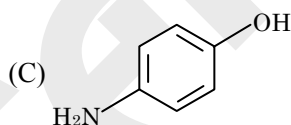
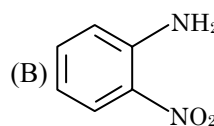
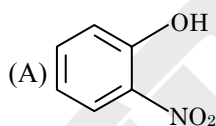
Choose the correct answer form the options given below :

- (1) (A)-(III), (B)-(II), (C)-(I), (D)-(IV) (2) (A)-(IV), (B)-(I), (C)-(II), (D)-(III)  
 (3) (A)-(II), (B)-(III), (C)-(I), (D)-(IV) (4) (A)-(IV), (B)-(I), (C)-(III), (D)-(II)

Ans. [2]

Sol. Informative

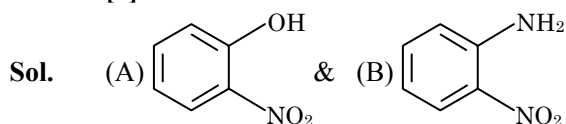
**Q.69** The steam volatile compounds among the following are :



Choose the correct answer from the options given below :

- (1) (B) and (D) only (2) (A) and (C) only  
 (3) (A) and (B) only (4) (A), (B) and (C) only

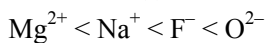
Ans. [3]



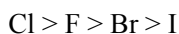
are steam volatile due to intramolecular hydrogen bonding.

**Q.70** Given below are two statements :

**Statement (I) :** The radii of isoelectronic species increases in the order.



**Statement (II) :** The magnitude of electron gain enthalpy of halogen decreases in the order.



In the light of the above statements, choose the most appropriate answer from the options given below :

- (1) Statement I is incorrect but Statement II is correct
- (2) Both Statement I and Statement II are incorrect
- (3) Statement I is correct but Statement II is incorrect
- (4) Both Statement I and Statement II are correct

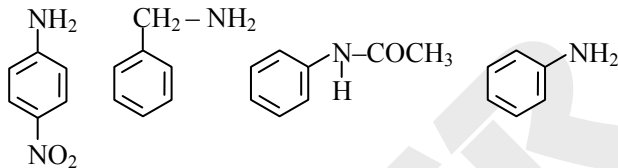
**Ans.** [4]

**Sol.** (i) For isoelectronic species –ve charge increases, radii increases.

(ii) Magnitude of E.G.E :  $\text{Cl} > \text{F} > \text{Br} > \text{I}$

**Section-B: Numerical Value Type Questions:** This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

**Q.71** Given below are some nitrogen containing compounds.

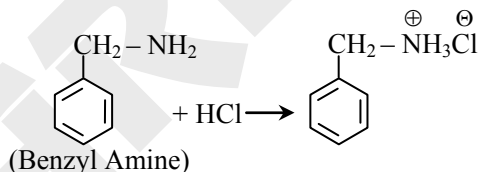


Each of them is treated with HCl separately. 1.0 g of the most basic compound will consume \_\_\_\_\_ mg of HCl.

(Given molar mass in  $\text{g mol}^{-1}$  C:12, H : 1, O : 16, Cl : 35.5)

**Ans.** [341]

**Sol.** Benzyl Amine is most basic due to localised lone pair.



$$\text{Mole of benzyl Amine} \Rightarrow \frac{1}{107} = 0.00934 \text{ mole}$$

1 Mole of Benzyl amine consumed 1 mole of HCl

So, Mole of HCl consumed  $\rightarrow 0.00934$  mole

Mass of HCl consumed  $\rightarrow 0.00934 \times \text{molar mass of HCl}$

$$= 0.00934 \times 36.5$$

$$= 0.341 \text{ gm}$$

$$= 341 \text{ mg}$$



**Q.72** The molar mass of the water insoluble product formed from the fusion of chromite ore ( $\text{FeCr}_2\text{O}_4$ ) with  $\text{Na}_2\text{CO}_3$  in presence of  $\text{O}_2$  is \_\_\_\_\_  $\text{g mol}^{-1}$ .

**Ans.** [160]

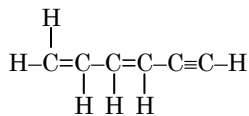
**Sol.**  $4\text{FeCr}_2\text{O}_4 + 8\text{Na}_2\text{CO}_3 + 7\text{O}_2 \rightarrow 8\text{Na}_2\text{CrO}_4 + 2\text{Fe}_2\text{O}_3 + 8\text{CO}_2$

$\text{Fe}_2\text{O}_3$  is water insoluble, so its molar mass

$$\Rightarrow [2 \times 56 + 3 \times 16] \Rightarrow 160 \text{ g/mol}$$

**Q.73** The sum of sigma ( $\sigma$ ) and pi ( $\pi$ ) bonds in Hex-1,3-dien-5-yne is \_\_\_\_\_.

**Ans.** [15]



**Sol.**

Number of  $\sigma$  bond = 11

Number of  $\pi$  bond = 4

$$\sigma + \pi = 11 + 4 = 15$$

**Q.74** If  $\text{A}_2\text{B}$  is 30% ionised in an aqueous solution, then the value of van't Hoff factor ( $i$ ) is \_\_\_\_\_  $\times 10^{-1}$ .

**Ans.** [16]

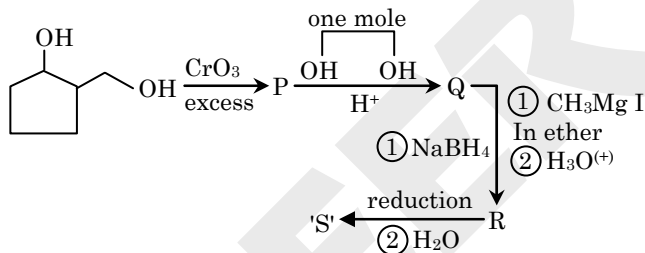
**Sol.**  $\text{A}_2\text{B} \rightarrow 2\text{A}^+ + \text{B}^{2-}$ ;  $y = 3$

$$\alpha = 0.3$$

$$i = 1 + (y - 1)\alpha$$

$$= 1 + (3 - 1)(0.3) = 1.6 = 16 \times 10^{-1}$$

**Q.75**

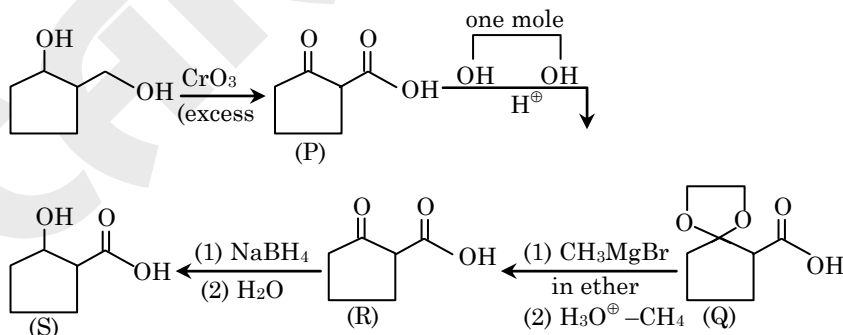


0.1 mole of compound 'S' will weight \_\_\_\_\_ g.

(Given molar mass in  $\text{g mol}^{-1}$  C : 12, H : 1, O : 16)

**Ans.** [13]

**Sol.**



0.1 mole of compound (S) weight in gm

$$= 0.1 \times \text{molar mass of compound (S)}$$

$$= 0.1 \times 130 = 13 \text{ gm}$$