



JEE Main Online Exam 2023

Questions & Solution

15th April 2023 | Morning

MATHEMATICS

Section-A: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Q.1 Let S be the set of all (λ, μ) for which the vectors $\lambda\hat{i} - \hat{j} + \hat{k}$, $\hat{i} + 2\hat{j} + \mu\hat{k}$ and $3\hat{i} - 4\hat{j} + 5\hat{k}$, where $\lambda - \mu = 5$, are coplanar, then $\sum_{(\lambda, \mu) \in S} 80(\lambda^2 + \mu^2)$ is equal to-

(1) 2210

(2) 2130

(3) 2290

(4) 2370

Ans. [3]

Sol. $\therefore \begin{vmatrix} \lambda & -1 & 1 \\ 1 & 2 & \mu \\ 3 & -4 & 5 \end{vmatrix} = 0$

$$\Rightarrow \lambda[10 + 4\mu] + 1[5 - 3\mu] + 1[-10] = 0$$

$$\Rightarrow 4\lambda\mu + 10\lambda - 3\mu = 5 \quad \dots(i)$$

And $\lambda - \mu = 5$

So, by (i)

$$4(5 + \mu)\mu + 10(5 + \mu) - 3\mu = 5$$

$$\Rightarrow 4\mu^2 + 27\mu + 45 = 0$$

$$\Rightarrow 4\mu^2 + 15\mu + 12\mu + 45 = 0$$

$$\Rightarrow (4\mu + 15) - (\mu + 3) = 0$$

$$\therefore \mu = -3, \frac{-15}{4}$$

$$= 2, \frac{5}{4}$$

$$\therefore \sum_{\lambda, \mu \in S} 80(\lambda^2 + \mu^2) = 80 \left[(9 + 4) + \frac{225}{16} + \frac{25}{16} \right]$$

$$= 80 \left[13 + \frac{125}{8} \right] = 10 \times 229$$

$$= 2290$$

Q.2 Let the determinant of a square matrix A of order m be $m - n$, where m and n satisfy $4m + n = 22$ and $17m + 4n = 93$. If $\det(n \operatorname{adj}(\operatorname{adj}(mA))) = 3^a 5^b 6^c$, then $a + b + c$ is equal to

(1) 84

(2) 96

(3) 101

(4) 109

Ans. [2]

Sol. $|A| = m - n$, where $4m + n = 22 \quad \dots(i)$

and $17m + 4n = 93 \quad \dots(ii)$

Solving (i) and (ii)

$$m = 5, n = 2$$

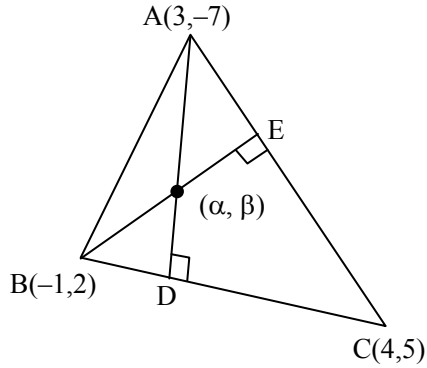
$$\text{Order} = 5$$

$$|A| = 3$$

$$\begin{aligned}
 &\therefore \det (n \operatorname{adj} (\operatorname{adj}(mA))) \\
 &= |2 \operatorname{adj} (\operatorname{adj} (5A))| \\
 &= 2^5 |5A|^{16} \\
 &= 2^5 5^{80} |A|^{16} = 2^5 \cdot 3^{16} \cdot 5^{80} \\
 &= 3^{11} 5^{80} 6^5 \\
 &\text{So, } a + b + c = 96
 \end{aligned}$$

- Q.3** If (α, β) is the orthocenter of the triangle ABC with vertices $A(3, -7)$, $B(-1, 2)$ and $C(4, 5)$, then $9\alpha - 6\beta + 60$ is equal to
 (1) 25 (2) 35 (3) 30 (4) 40

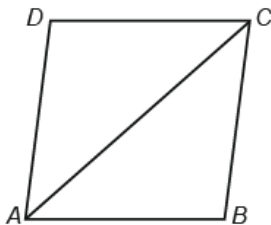
Ans. [1]
Sol.



$$\begin{aligned}
 AD : y + 7 &= \frac{-5}{3}(x - 3) \\
 \Rightarrow 3y + 21 &= -5x + 15 \\
 5x + 3y + 6 &= 0 \quad \dots(i) \\
 BE : y - 2 &= \frac{-1}{12}(x + 1) \\
 \Rightarrow 12y - 24 &= -x - 1 \\
 \Rightarrow x &= 23 - 12y \\
 \text{by (ii) } 115 - 60y + 3y + 6 &= 0 \\
 57y &= 121 \\
 y &= \frac{121}{57}, x = 23 - 12 \times \frac{121}{57} \\
 \therefore 9\alpha - 6\beta + 60 &= 9 \times 23 - 108 \times \frac{121}{57} - 6 \times \frac{121}{57} + 60 \\
 &= 207 - 242 + 60 = 25
 \end{aligned}$$

- Q.4** Let ABCD be a quadrilateral. If E and F are the mid points of the diagonals AC and BD respectively and $(\vec{AB} - \vec{BC}) + (\vec{AD} - \vec{DC}) = k \vec{FE}$, then k is equal to-
 (1) 4 (2) -2 (3) 2 (4) -4

Ans. [4]
Sol.



Let position vector of A, B, C and D are \vec{a} , \vec{b} , \vec{c} and \vec{d} respectively

$$\therefore \text{Position vector of E} = \frac{\vec{OC} + \vec{OA}}{2} = \frac{\vec{c} + \vec{a}}{2}$$

$$\text{Position vector of F} = \frac{\vec{b} + \vec{d}}{2}$$

Now, $(\vec{AB} - \vec{BC}) + \vec{AD} - \vec{DC}$

$$\Rightarrow \vec{b} - \vec{a} - (\vec{c} - \vec{b}) + \vec{d} - \vec{a} - (\vec{c} - \vec{d})$$

$$\Rightarrow 2\vec{b} - 2\vec{a} - 2\vec{c} + 2\vec{d}$$

$$\Rightarrow 2(\vec{b} + \vec{d}) - 2(\vec{a} + \vec{c})$$

$$\Rightarrow 4 \left[\frac{\vec{b} + \vec{d}}{4} - \frac{\vec{a} + \vec{c}}{2} \right] = 4[\vec{OF} - \vec{OE}]$$

$$\Rightarrow 4\vec{EF} = -4\vec{FE}$$

$$\therefore k = -4$$

Q.5 Let the foot of perpendicular of the point P(3, -2, -9) on the plane passing through the points (-1, -2, -3), (9, 3, 4), (9, -2, 1) be Q(α , β , γ). Then the distance Q from the origin is

(1) $\sqrt{42}$

(2) $\sqrt{38}$

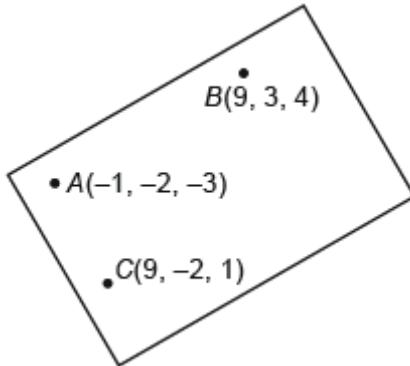
(3) $\sqrt{35}$

(4) $\sqrt{29}$

Ans.

[1]

Sol.



$$\vec{AC} = 10\hat{i} + 4\hat{k}$$

$$\vec{AB} = 10\hat{i} + 5\hat{j} + 7\hat{k}$$

$$\vec{AC} \times \vec{AB} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 10 & 0 & 4 \\ 10 & 5 & 7 \end{vmatrix}$$

$$= -20\hat{i} - 30\hat{j} + 50\hat{k}$$

Equation of plane

$$2x + 3y - 5z = d$$

Put (-1, -2, -3)

$$-2 - 6 + 15 = d$$

$$d = 7$$

$$\therefore 2x + 3y - 5z = 7$$

Foot of perpendicular

$$\frac{x-3}{2} = \frac{y+2}{3} = \frac{z+9}{-5} = -\left(\frac{38}{38}\right)$$

$$x = 1, y = -5, z = -4$$

$$Q(1, -5, -4)$$

$$\begin{aligned} \text{Distance from origin} &= \sqrt{1+25+16} \\ &= \sqrt{42} \end{aligned}$$

Q.6 The number of common tangents, to the circles $x^2 + y^2 - 18x - 15y + 131 = 0$ and $x^2 + y^2 - 6x - 6y - 7 = 0$, is

(1) 3 (2) 1 (3) 4 (4) 2

Ans. [1]

Sol. $x^2 + y^2 - 18x - 15y + 131 = 0$

$$C_1\left(9, \frac{15}{2}\right), r_1 = \sqrt{81 + \frac{225}{4} - 131} = \frac{5}{2}$$

$$x^2 + y^2 - 6x - 6y - 7 = 0$$

$$C_2(3, 3), r_2 = \sqrt{9 + 9 + 7} = 5$$

$$d = C_1C_2 = \sqrt{(9-3)^2 + \left(\frac{15}{2}-3\right)^2} = \sqrt{36 + \frac{81}{4}} = \frac{15}{2}$$

$$r_1 + r_2 = \frac{5}{2} + 5 = \frac{15}{2}$$

$$\Rightarrow C_1C_2 = r_1 + r_2$$

\therefore Circles touch each other externally, 3 common tangents.

Q.7 The total number of three-digit numbers, divisible by 3, which can be formed using the digits 1, 3, 5, 8, if repetition of digits is allowed, is

(1) 21 (2) 20 (3) 22 (4) 18

Ans. [3]

Sol. Sum of digits 3 : (1, 1, 1)
Sum of digits 9 : (1, 3, 5) or (3, 3, 3)
Sum of digits 12 : (1, 3, 8)
Sum of digits 15 : (5, 5, 5)
Sum of digits 18 : (5, 5, 8)
Sum of digits 21 : (5, 8, 8)
Sum of digits 24 : (8, 8, 8)
Possible numbers are

$$= 1 + 3! + 1 + 3! + 1 + \frac{3!}{2!} + \frac{3!}{2!} + 1$$

$$= 22$$

Q.8 If the set $\left\{ \operatorname{Re}\left(\frac{z - \bar{z} + z\bar{z}}{2 - 3z + 5\bar{z}}\right) : z \in \mathbb{C}, \operatorname{Re} z = 3 \right\}$ is equal to the interval $(\alpha, \beta]$, then $24(\beta - \alpha)$ is equal to-

(1) 36 (2) 27 (3) 30 (4) 42

Ans. [3]

Sol. $\operatorname{Re}\left(\frac{z - \bar{z} + z\bar{z}}{2 - 3z + 5\bar{z}}\right)$

$$\operatorname{Re}\left(\frac{x + iy - (x - iy) + x^2 + y^2}{2 - 3(x + iy) + 5(x - iy)}\right)$$

$$\operatorname{Re}\left(\frac{x^2 + y^2 + i(2y)}{2 + 2x - 8iy}\right)$$

$$\operatorname{Re}\left(\frac{(x^2 + y^2 + 2yi)(2(1+x) + 8iy)}{(2(1+x))^2 + (8y)^2}\right)$$

$$= \frac{2(x^2 + y^2)(1+x) - 16y^2}{4(1+x)^2 + (8y)^2}$$

Put $x = 3$

$$= \frac{8(9 + y^2) - 16y^2}{64 + 64y^2}$$

$$f(y) = \frac{1}{8} \frac{(9 - y^2)}{1 + y^2}$$

Range of $f(y) = (-0.125, 1.125]$

$$\alpha = -0.125$$

$$\beta = 1.125$$

$$\beta - \alpha = 1.25$$

$$24(\beta - \alpha) = 30$$

Q.9 Let $(a + bx + cx^2)^{10} = \sum_{i=0}^{20} p_i x^i$, $a, b, c \in \mathbb{N}$. If $p_1 = 20$ and $p_2 = 210$, then $2(a + b + c)$ is equal to-

(1) 6

(2) 15

(3) 12

(4) 8

Ans. [3]

Sol. General term : $\frac{10!}{r_1! r_2! r_3!} (a)^{r_1} (bx)^{r_2} (cx^2)^{r_3}$

For coeff. of x : $r_2 + 2r_3 = 1$

$$\begin{matrix} r_1 & r_2 & r_3 \\ 9 & 1 & 0 \end{matrix}$$

$$\therefore \text{coeff. of } x = \frac{10!}{9!} a^9 b^1 = 20$$

$$\Rightarrow a^9 \cdot b = 2 \quad \dots(i)$$

$$\text{Coeff. of } x^2 : \frac{10!}{8! 2! 0!} a^8 \cdot b^2 + \frac{10!}{9! 0! 1!} a^9 \cdot c = 210$$

$$\Rightarrow 45a^8 \cdot b^2 + 10 \cdot a^9 \cdot c = 210$$

$$\Rightarrow 9a^8 b^2 + 2a^9 \cdot c = 42$$

as $a, b, c \in \mathbb{N}$

$$\therefore a = 1, b = 2, c = 3$$

$$2(a + b + c) = 2(3 + 2 + 1) = 12$$

Q.10 The number of real roots of the equation $x|x| - 5|x + 2| + 6 = 0$, is-

(1) 5

(2) 4

(3) 6

(4) 3

Ans. [4]

Sol. $x|x| - 5|x + 2| + 6 = 0$

Case-I :

$$x < -2$$

$$-x^2 + 5(x + 2) + 6 = 0$$

$$\Rightarrow x^2 - 5x - 16 = 0$$

$$\Rightarrow x = \frac{5 \pm \sqrt{25 + 64}}{2}$$

$$\therefore x = \frac{5 - \sqrt{89}}{2} \text{ is accepted}$$

Case-II :

$$-2 \leq x < 0$$

$$-x^2 - 5(x + 2) + 6 = 0$$

$$\Rightarrow x^2 + 5x + 4 = 0$$

$$\Rightarrow (x + 1)(x + 4) = 0$$

$$x = -1 \text{ is accepted}$$

Case-III :

$$x \geq 0$$

$$x^2 - 5(x + 2) + 6 = 0$$

$$\Rightarrow x^2 - 5x - 4 = 0$$

$$x = \frac{5 \pm \sqrt{25 + 16}}{2}$$

$$= \frac{5 \pm \sqrt{41}}{2}$$

$$x = \frac{5 \pm \sqrt{41}}{2} \text{ is accepted}$$

\therefore 3 real roots are possible.

Option (4) is correct.

Q.11 Let A_1 and A_2 be two arithmetic means and G_1, G_2 and G_3 be three geometric means of two distinct positive numbers. Then $G_1^4 + G_2^4 + G_3^4 + G_1^2 G_3^2$ is equal to-

(1) $(A_1 + A_2)^2 G_1 G_3$

(2) $2(A_1 + A_2) G_1 G_3$

(3) $(A_1 + A_2) G_1^2 G_3^2$

(4) $2(A_1 + A_2) G_1^2 G_3^2$

Ans. [1]

Sol. Let the two numbers are a, b

$$A_1 = a + \frac{b-a}{3} = \frac{2a+b}{3}$$

$$A_2 = a + \frac{b-a}{3} \cdot 2 = \frac{a+2b}{3}$$

$$G_1 = a \left(\frac{b}{a} \right)^{\frac{1}{4}} ; G_2 = a \left(\frac{b}{a} \right)^{\frac{2}{4}} ; G_3 = a \left(\frac{b}{a} \right)^{\frac{3}{4}}$$

$$(G_1)^4 + (G_2)^4 + (G_3)^4 + (G_1)^2 \cdot (G_3)^2$$

$$\Rightarrow a^4 \cdot \frac{b}{a} + a^4 \cdot \frac{b^2}{a^2} + a^4 \cdot \frac{b^3}{a^3} + a^4 \cdot \frac{b^2}{a^2}$$

$$= ba^3 + b^2 a^2 + b^3 a + a^2 b^2$$

$$= ab(a^2 + b^2 + 2ab) = ab(a+b)^2$$

$$(A_1 + A_2)^2 \cdot G_1 G_3 = (a+b)^2 \cdot ab$$

\therefore Option (1) is correct.

Q.12 Let $[x]$ denote the greatest integer function and $f(x) = \max\{1+x+[x], 2+x, x+2[x]\}$, $0 \leq x \leq 2$. Let m be the number of points in $[0, 2]$, where f is not continuous and n be the number of points in $(0, 2)$, where f is not differentiable. Then $(m+n)^2 + 2$ is equal to

(1) 2

(2) 11

(3) 6

(4) 3

Ans. [4]

Sol.
$$f(x) = \begin{cases} \max\{x+1, x+2, x\} & 0 \leq x < 1 \\ \max\{x+2, x+2, x+2\} & 1 \leq x < 2 \\ \max\{5, 4, 6\} & x = 2 \end{cases}$$

$$\Rightarrow f(x) = \begin{cases} x+2 & 0 \leq x < 1 \\ x+2 & 1 \leq x < 2 \\ 6 & x = 2 \end{cases}$$

$$\Rightarrow f(x) = \begin{cases} x+2 & 0 \leq x < 1 \\ 6 & x = 2 \end{cases}$$

f is not continuous at $x = 2$

f is differentiable in $(0, 2)$

$$\therefore m = 1, n = 0$$

$$(m + n)^2 + 2 = 1 + 2 = 3$$

Option (4) is correct

Q.13 Let S be the set of all values of λ , for which the shortest distance between the lines

$$\frac{x-\lambda}{0} = \frac{y-3}{4} = \frac{z+6}{1} \text{ and } \frac{x+\lambda}{3} = \frac{y}{-4} = \frac{z-6}{0} \text{ is } 13. \text{ Then } 8 \left| \sum_{\lambda \in S} \lambda \right| \text{ is equal to-}$$

(1) 306

(2) 304

(3) 308

(4) 302

Ans. [1]

Sol. $\frac{x-\lambda}{0} = \frac{y-3}{4} = \frac{z+6}{1}$

$$\frac{x+\lambda}{3} = \frac{y}{-4} = \frac{z-6}{0}$$

$$d = \frac{|(\vec{a}_2 - \vec{a}_1) \cdot (\vec{n}_1 \times \vec{n}_2)|}{|\vec{n}_1 \times \vec{n}_2|} = 13$$

$$\vec{n}_1 \times \vec{n}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 4 & 1 \\ 3 & -4 & 0 \end{vmatrix} = 4\hat{i} + 3\hat{j} - 12\hat{k}$$

$$\frac{|(2\lambda\hat{i} + 3\hat{j} - 12\hat{k}) \cdot (4\hat{i} + 3\hat{j} - 12\hat{k})|}{\sqrt{16+9+144}} = 8$$

$$|8\lambda + 9 + 144| = 104$$

$$|8\lambda + 153| = 104$$

$$8\lambda = \pm 104 - 153$$

$$\lambda = \frac{-49}{8}, \frac{-257}{8}$$

$$8 \left| \sum_{\lambda \in S} \lambda \right| = 8 \left[\frac{49}{8} + \frac{257}{8} \right] = 306$$

Q.14 Negation of $p \wedge (q \wedge \sim (p \wedge q))$ is

(1) $(\sim (p \wedge q)) \vee p$

(2) $p \vee q$

(3) $\sim (p \vee q)$

(4) $(\sim (p \wedge q)) \wedge q$

Ans. [1]

Sol. $\sim [p \wedge (q \wedge \sim (p \wedge q))]$

$$\sim [p \wedge (q \wedge (\sim p \vee \sim q))]$$

$$\sim [p \wedge ((q \wedge \sim p) \vee (q \wedge \sim q))]$$

$$\sim [p \wedge (q \wedge \sim p)]$$

$$\sim p \vee \sim (q \wedge \sim p)$$

$$\sim p \vee (\sim q \vee p)$$

$$\sim p \vee (p \wedge q) \vee p$$

Q.15 Let the system of linear equations

$$\begin{aligned} -x + 2y - 9z &= 7 \\ -x + 3y + 7z &= 9 \\ -2x + y + 5z &= 8 \\ -3x + y + 13z &= \lambda \end{aligned}$$

has a unique solution $x = \alpha, y = \beta, z = \gamma$. Then the distance of the point (α, β, γ) from the plane $2x - 2y + z = \lambda$ is-

- (1) 11 (2) 7 (3) 9 (4) 13

Ans.

[2]

Sol.

$$\begin{aligned} -x + 2y - 9z &= 7 && \dots(i) \\ -x + 3y + 7z &= 9 && \dots(ii) \\ -2x + y + 5z &= 8 && \dots(iii) \\ -3x + y + 13z &= \lambda && \dots(iv) \end{aligned}$$

From (i), (ii), (iii)

$$x = -3, y = 2, z = 0$$

Substitute in (iv)

$$3 \times 3 + 2 = \lambda$$

$$\lambda = 11$$

Point: $(-3, 2, 0)$

Plane: $2x - 2y + z = 11$

$$d = \frac{|-6 - 4 - 11|}{\sqrt{2^2 + 2^2 + 1}} = \frac{21}{3} = 7$$

Q.16 A bag contains 6 white and 4 black balls. A die is rolled once and the number of balls equal to the number obtained on the die are drawn from the bag at random. The probability that all the balls drawn are white is

- (1) $\frac{1}{4}$ (2) $\frac{11}{50}$ (3) $\frac{1}{5}$ (4) $\frac{9}{50}$

Ans.

[3]

Sol.

Bag have 6 white and 4 black balls
Probability all drawn balls are white

$$\begin{aligned} &= \frac{1}{6} \left[\frac{{}^6C_1}{{}^{10}C_1} + \frac{{}^6C_2}{{}^{10}C_2} + \frac{{}^6C_3}{{}^{10}C_3} + \frac{{}^6C_4}{{}^{10}C_4} + \frac{{}^6C_5}{{}^{10}C_5} + \frac{{}^6C_6}{{}^{10}C_6} \right] \\ &= \frac{504}{2520} = \frac{1}{5} \end{aligned}$$

Q.17 If $\int_0^1 \frac{1}{(5+2x-2x^2)(1+e^{(2-4x)})} dx = \frac{1}{\alpha} \log_e \left(\frac{\alpha+1}{\beta} \right)$, $\alpha, \beta > 0$, then $\alpha^4 - \beta^4$ is equal to-

- (1) 19 (2) -21 (3) 0 (4) 21

Ans.

[4]

Sol.

$$\begin{aligned} I &= \frac{1}{2} \int_0^1 \frac{1}{\left(\frac{5}{2} - (x^2 - x) \right) \left(1 + e^{-4\left(x - \frac{1}{2}\right)} \right)} dx \\ &= \frac{1}{2} \int_0^1 \frac{1}{\left(\left(\frac{11}{4} \right) - \left(x - \frac{1}{2} \right)^2 \right) \left(1 + e^{-4\left(x - \frac{1}{2}\right)} \right)} dx \end{aligned}$$

$$\text{Let } x - \frac{1}{2} = t, dx = dt$$

$$= \frac{1}{2} \int_{-\frac{1}{2}}^{\frac{1}{2}} \frac{1}{\left(\left(\frac{\sqrt{11}}{2}\right)^2 - t^2\right)(1 + e^{-4t})} dt$$

$$= \frac{1}{2} \int_0^{\frac{1}{2}} \frac{1}{\left(\left(\frac{\sqrt{11}}{2}\right)^2 - t^2\right)(1 + e^{-4t})} + \frac{1}{\left(\left(\frac{\sqrt{11}}{2}\right)^2 - t^2\right)(1 + e^{4t})}$$

$$= \frac{1}{2} \int_0^{\frac{1}{2}} \frac{1}{\left(\frac{\sqrt{11}}{2}\right)^2 - t^2} dt = \frac{1}{2} \times \frac{1}{2\left(\frac{\sqrt{11}}{2}\right)} \ln \left| \frac{\frac{\sqrt{11}}{2} + t}{\frac{\sqrt{11}}{2} - t} \right|_0^{\frac{1}{2}}$$

$$= \frac{1}{2\sqrt{11}} \ln \left(\frac{\sqrt{11} + 1}{\sqrt{11} - 1} \right) = \frac{1}{2\sqrt{11}} \ln \left(\frac{(\sqrt{11} + 1)^2}{10} \right)$$

$$= \frac{1}{\sqrt{11}} \ln \left(\frac{\sqrt{11} + 1}{\sqrt{10}} \right)$$

$$\Rightarrow \alpha = \sqrt{11}, \beta = \sqrt{10} \Rightarrow \alpha^4 - \beta^4 = 21$$

Q.18 If the domain of the function $f(x) = \log_e(4x^2 + 11x + 6) + \sin^{-1}(4x + 3) + \cos^{-1}\left(\frac{10x + 6}{3}\right)$ is $(\alpha, \beta]$, then

$36|\alpha + \beta|$ is equal to-

(1) 54

(2) 72

(3) 63

(4) 45

Ans.

[4]

Sol.

$$4x^2 + 11x + 6 > 0 \Rightarrow (4x + 3)(x + 2) > 0$$

$$\Rightarrow x \in (-\infty, -2) \cup \left[\frac{-3}{4}, \infty\right) \quad \dots(i)$$

$$-1 \leq 4x + 3 \leq 1 \Rightarrow -4 \leq 4x \leq -2$$

$$-1 \leq x \leq -\frac{1}{2} \quad \dots(ii)$$

$$-1 \leq \frac{10x + 6}{3} \leq 1 \Rightarrow -3 \leq 10x + 6 \leq 3$$

$$\Rightarrow -9 \leq 10x \leq -3$$

$$\frac{-9}{10} \leq x \leq \frac{-3}{10} \quad \dots(iii)$$

$$(i), (ii), (iii) \Rightarrow \frac{-3}{4} < x \leq \frac{-1}{2}$$

$$\alpha = \frac{-3}{4}, \beta = \frac{-1}{2}$$

$$36|\alpha + \beta| = 36 \times \frac{5}{4} = 45$$

Q.19 Let $x = x(y)$ be the solution of the differential equation $2(y + 2) \log_e (y + 2) dx + (x + 4 - 2 \log_e (y + 2)) dy = 0$, $y > -1$ with $x(e^4 - 2) = 1$. Then $x(e^9 - 2)$ is equal to-

(1) 3

(2) $\frac{4}{9}$

(3) $\frac{32}{9}$

(4) $\frac{10}{3}$

Ans. [3]**Sol.**

Let $x + 4 = u$, $y + 2 = v$

$dx = du$, $dy = dv$

$(2v \ln v) du = -(u - 2 \ln v) dv$

$2v \ln v \frac{du}{dv} + u = 2 \ln v$

$$\frac{du}{dv} + \frac{1}{2v \ln v} \cdot u = \frac{1}{v}$$

IF = $e^{\int \frac{1}{2v \ln v} dv} = e^{\frac{1}{2} \ln(\ln v)} = (\ln v)^{\frac{1}{2}}$

$$u \cdot (\ln v)^{\frac{1}{2}} = \int \frac{1}{v} \cdot (\ln v)^{\frac{1}{2}} dv$$

$$u \cdot (\ln v)^{\frac{1}{2}} = \frac{2}{3} (\ln v)^{\frac{3}{2}} + c \quad \dots(i)$$

$y = e^4 - 2 \Rightarrow x = 1$

$\therefore v = e^4 \Rightarrow u = 5$

$$5 \cdot \left(4^{\frac{1}{2}}\right) = \frac{2}{3} \cdot (4)^{\frac{3}{2}} + c$$

$10 = \frac{16}{3} + c \Rightarrow c = \frac{14}{3}$

$y = e^9 - 2 \Rightarrow v = y + 2 = e^9$

$(i) \Rightarrow u \cdot 3 = \frac{2}{3} \times 27 + \frac{14}{3} = 18 + \frac{14}{3}$

$$x + 4 = u = 6 + \frac{14}{9}$$

$$x = 2 + \frac{14}{9} = \frac{32}{9}$$

Q.20 The mean and standard deviation of 10 observations are 20 and 8 respectively. Later on, it was observed that one observation was recorded as 50 instead of 40. Then the correct variance is

(1) 11

(2) 13

(3) 12

(4) 14

Ans. [2]**Sol.**

$$\frac{x_1 + x_2 + \dots + x_9 + 50}{10} = 20$$

$x_1 + x_2 + \dots + x_9 = 150$

$$64 = \frac{x_1^2 + x_2^2 + \dots + x_9^2 + 2500}{10} - 400$$

$$x_1^2 + x_2^2 + \dots + x_9^2 = 2140$$

New mean = $\frac{150 + 40}{10} = 19$

New $\sigma = \frac{2140 + 1600}{10} - (19)^2$

$\sigma = 13$

Section-B: Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE**. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g. 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer..

Q.21 Let $f(x) = \int \frac{dx}{(3+4x^2)\sqrt{4-3x^2}}$, $|x| < \frac{2}{\sqrt{3}}$. If $f(0) = 0$ and $f(1) = \frac{1}{\alpha\beta} \tan^{-1}\left(\frac{\alpha}{\beta}\right)$, $\alpha, \beta > 0$, then $\alpha^2 + \beta^2$ is

equal to _____

Ans. [28]

Sol. $f(x) = \int \frac{dx}{(3+4x^2)\sqrt{4-3x^2}}$

Put $x = \frac{1}{t}$, $dx = -\frac{1}{t^2} dt$

$$f(x) = \int \frac{-dt}{t^2 \left(3 + \frac{4}{t^2}\right) \sqrt{4 - \frac{3}{t^2}}}$$

$$= \int \frac{-t dt}{(3t^2 + 4) \sqrt{4t^2 - 3}}$$

$$4t^2 - 3 = \lambda^2 \Rightarrow 8t dt = 2\lambda d\lambda$$

$$f(x) = - \int \frac{\lambda d\lambda}{4 \cdot \left(3 \left(\frac{\lambda^2 + 3}{4}\right) + 4\right) \cdot \lambda}$$

$$= - \int \frac{d\lambda}{3\lambda^2 + 9 + 16} = - \int \frac{d\lambda}{3\lambda^2 + 25} = -\frac{1}{3} \int \frac{d\lambda}{\lambda^2 + \frac{25}{3}}$$

$$= -\frac{1}{3} \times \frac{\sqrt{3}}{5} \tan^{-1}\left(\frac{\sqrt{3}\lambda}{5}\right) + c$$

$$f(x) = -\frac{\sqrt{3}}{15} \tan^{-1}\left(\frac{\sqrt{3}\sqrt{4-3x^2}}{5x}\right) + c$$

$$f(0) = 0 \Rightarrow c = +\frac{\sqrt{3}\pi}{30}$$

$$f(1) = \frac{-\sqrt{3}}{30} \tan^{-1}\left(\frac{\sqrt{3}}{5}\right) + \frac{\sqrt{3}}{15} \times \frac{\pi}{2}$$

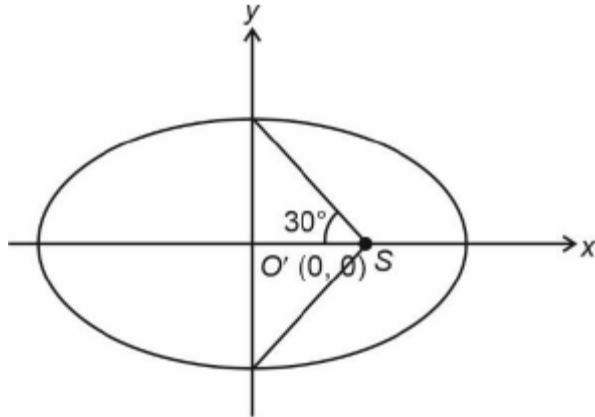
$$= \frac{\sqrt{3}}{15} \cot^{-1}\left(\frac{\sqrt{3}}{5}\right) = \frac{\sqrt{3}}{15} \tan^{-1}\left(\frac{5}{\sqrt{3}}\right) = \frac{1}{5\sqrt{3}} \tan^{-1}\left(\frac{5}{\sqrt{3}}\right)$$

$$\Rightarrow \alpha^2 + \beta^2 = 28$$

Q.22 Let an ellipse with center (1, 0) and latus rectum of length $\frac{1}{2}$ have its major axis along x-axis. If its minor axis subtends an angle 60° at the foci, then the square of the sum of the lengths of its minor and major axes is equal to _____.

Ans. [9]

Sol.



$$\frac{2b^2}{a} = \frac{1}{2}, \quad \tan 30^\circ = \frac{b}{ae}$$

$$b^2 = \frac{a}{4}, \quad \frac{1}{3} = \frac{b^2}{a^2 - b^2} \Rightarrow a^2 - b^2 = 3b^2 \Rightarrow b^2 = \frac{a^2}{4}$$

$$\Rightarrow a = 1, \quad b^2 = \frac{1}{4} \Rightarrow b = \frac{1}{2}$$

$$\Rightarrow (2a + 2b)^2 = 9$$

Q.23 A person forgets his 4-digit ATM pin code. But he remembers that in the code all the digits are different, the greatest digit is 7 and the sum of the first two digits is equal to the sum of the last two digits. Then the maximum number of trials necessary to obtain the correct code is _____.

Ans. [72]

Sol. abcd

$$a + b = c + d$$

$$0, 1, 2, 3, 4, 5, 6, 7$$

$$\text{Let } a + b = c + d = \lambda$$

There must be 7

$$\Rightarrow a + b = c + d = \lambda \geq 7$$

$$\lambda = 7, (a, b)/(c, d) \rightarrow (0, 7)/(1, 6)$$

$$\text{or } (2, 5)(3, 4) \rightarrow 24 \text{ numbers}$$

$$\lambda = 8, (a, b)/(c, d) \rightarrow (1, 7)/(2, 6)$$

$$\text{or } (3, 5) \rightarrow 16 \text{ numbers}$$

$$\lambda = 9, (a, b)/(c, d) \rightarrow (2, 7)/(3, 6)$$

$$\text{or } (4, 5) \rightarrow 16 \text{ numbers}$$

$$\lambda = 10, (a, b)/(c, d) \rightarrow (3, 7)/(4, 6) \rightarrow 8 \text{ numbers}$$

$$\lambda = 11, (a, b)/(c, d) \rightarrow (4, 7)/(5, 6) \rightarrow 8 \text{ numbers}$$

$$\lambda = 12, (a, b)/(c, d) \rightarrow (5, 7) \text{ Not possible}$$

$$\lambda = 13, (a, b)/(c, d) \rightarrow (6, 7) \text{ Not possible}$$

$$\lambda = 14, (a, b)/(c, d) \rightarrow (7, 7) \text{ Not possible}$$

$$\Rightarrow \text{Total numbers} = 72$$

Q.24 The number of elements in the set $\{n \in \mathbb{N} : 10 \leq n \leq 100 \text{ and } 3^n - 3 \text{ is a multiple of } 7\}$ is _____.

Ans. [15.00]

Sol. $3^n - 3 = 7k$

$$3 \equiv 3 \pmod{7}$$

$$3^2 \equiv 2 \pmod{7}$$

$$3^3 \equiv -1 \pmod{7}$$

$$\begin{aligned}3^6 &\equiv 1 \pmod{7} \\3^7 &\equiv 3 \pmod{7} \\&\vdots \\3^{13} &\equiv 3 \pmod{7} \\n &\text{ can be } 13, 19, 25, \dots, 97 \\&\text{ Total 15 such } n \text{ exist}\end{aligned}$$

Q.25 Let $A = \{1, 2, 3, 4\}$ and R be a relation on the set $A \times A$ defined by $R = \{(a, b), (c, d) : 2a + 3b = 4c + 5d\}$. Then the number of elements in R is _____.

Ans. [06.00]

Sol. $2a + 3b = 4c + 5d$

Maximum value of $2a + 3b = 20$ at $(4, 4)$

Minimum value of $4c + 5d = 9$ at $(1, 1)$

So, $4c + 5d$ can be equal to 9, 13, 14, 17, 18, 19

$2a + 3b$ can be 9 $\Rightarrow (a, b) = (3, 1)$

$(c, d) = (1, 1)$

$2a + 3b$ can be 13 $\Rightarrow (a, b) = (2, 3)$

$(c, d) = (2, 1)$

$2a + 3b$ can be 14 $\Rightarrow (a, b) = (4, 2)$ OR $(1, 4)$

$(c, d) = (1, 2)$

$2a + 3b$ can be 17 $\Rightarrow (a, b) = (4, 3)$

$(c, d) = (3, 1)$

$2a + 3b$ can be 18 $\Rightarrow (a, b) = (3, 4)$

$(c, d) = (2, 2)$

Q.26 Consider the triangles with vertices $A(2, 1)$, $B(0, 0)$ and $C(t, 4)$, $t \in [0, 4]$. If the maximum and the minimum perimeters of such triangles are obtained at $t = \alpha$ and $t = \beta$ respectively, then $6\alpha + 21\beta$ is equal to _____.

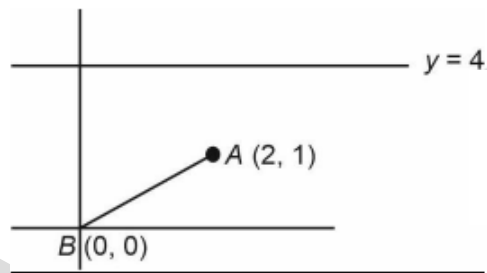
Ans. [48.00]

Sol. To minimize $CA + CB$, take image of B in

$y = 4$

$B' = (0, 8)$

AB'



$$y - 8 = \frac{-7}{2}(x - 0)$$

when $y = 4$

$$-4 = \frac{-7}{2}(x)$$

$$x = \frac{8}{7} \Rightarrow \beta = \frac{8}{7}$$

Maximization will be possible if $\alpha = 0$ or 4

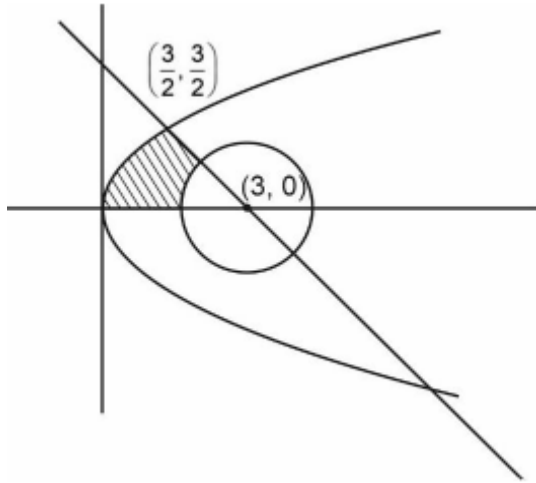
When compared $\alpha = 4$

$$6\alpha + 21\beta = 48$$

Q.27 If the area bounded by the curve $2y^2 = 3x$, lines $x + y = 3$, $y = 0$ and outside the circle $(x - 3)^2 + y^2 = 2$ is A , then $4(\pi + 4A)$ is equal to _____.

Ans. [42.00]

Sol.



$$A = \int_0^{3/2} \left((3-y) - \frac{2y^2}{3} \right) dy - \pi(\sqrt{2})^2 \cdot \frac{1}{8}$$

$$= \frac{36-9-6}{8} - \frac{\pi}{4} = \frac{21}{8} - \frac{\pi}{4}$$

Q.28 If the line $x = y = z$ intersects the line $x\sin A + y\sin B + z\sin C - 18 = 0 = x\sin 2A + y\sin 2B + z\sin 2C - 9$, where A, B, C are the angle of a triangle ABC , then $80 \left(\sin \frac{A}{2} \sin \frac{B}{2} \sin \frac{C}{2} \right)$ is equal to _____.

Ans. [5]

Sol.

$$x = y = z = k \text{ (let)}$$

$$\therefore k(\sin A + \sin B + \sin C) = 18$$

$$\Rightarrow k \left(4 \cos \frac{A}{2} \cdot \cos \frac{B}{2} \cdot \cos \frac{C}{2} \right) = 18 \quad \dots(i)$$

$$k(\sin 2A + \sin 2B + \sin 2C) = 9$$

$$\Rightarrow k(4 \sin A \cdot \sin B \cdot \sin C) = 9 \quad \dots(ii)$$

$$(ii)/(i)$$

$$8 \sin \frac{A}{2} \cdot \sin \frac{B}{2} \cdot \sin \frac{C}{2} = \frac{9}{18}$$

$$\Rightarrow 80 \sin \frac{A}{2} \cdot \sin \frac{B}{2} \cdot \sin \frac{C}{2} = 5$$

Q.29 If the sum of the series

$$\left(\frac{1}{2} - \frac{1}{3} \right) + \left(\frac{1}{2^2} - \frac{1}{2 \cdot 3} + \frac{1}{3^2} \right) + \left(\frac{1}{2^3} - \frac{1}{2^2 \cdot 3} + \frac{1}{2 \cdot 3^2} - \frac{1}{3^3} \right) + \left(\frac{1}{2^4} - \frac{1}{2^3 \cdot 3} + \frac{1}{2^2 \cdot 3^2} - \frac{1}{2 \cdot 3^3} + \frac{1}{3^4} \right) + \dots$$

is $\frac{\alpha}{\beta}$, where α and β are co-prime, then $\alpha + 3\beta$ is equal to _____.

Ans. [7]

Sol. Let $a = \frac{1}{2}$, $b = \frac{1}{3}$

Given : $(a - b) + (a^2 - ab + b^2) + (a^3 - a^2b + ab^2 - b^3) + \dots$

$$\Rightarrow \frac{1}{a+b} ((a^2 - b^2) + (a^3 + b^3) + (a^4 - b^4) + \dots)$$

$$\Rightarrow \left(\frac{1}{a+b} \right) (a^2 + a^3 + a^4 \dots - (b^2 - b^3 + b^4 \dots))$$

$$= \left(\frac{1}{a+b} \right) \left(\frac{a^2}{1-a} - \frac{b^2}{1+b} \right)$$

$$= \frac{1}{\frac{1}{2} + \frac{1}{3}} \left(\frac{\frac{1}{4}}{1 - \frac{1}{2}} - \frac{\frac{1}{9}}{1 + \frac{1}{3}} \right)$$

$$= \frac{6}{5} \left(\frac{1}{2} - \frac{1}{12} \right)$$

$$= \frac{6}{5} \left(\frac{5}{12} \right) = \frac{1}{2} = \frac{\alpha}{\beta}$$

$$\alpha + 3\beta = 1 + 6 = 7$$

Q.30 Let the plane P contain the line $2x + y - z - 3 = 0 = 5x - 3y + 4z + 9$ and be parallel to the line $\frac{x+2}{2} =$

$\frac{3-y}{-4} = \frac{z-7}{5}$. Then the distance of the point $A(8, -1, -19)$ from the plane P measured parallel to the line

$\frac{x}{-3} = \frac{y-5}{4} = \frac{z-2}{-12}$ is equal to _____.

Ans. [26]

Sol. Plane containing the line $2x + y - z - 3 = 0 = 5x - 3y + 4z + 9$ is $2x + y - z - 3 + \lambda(5x - 3y + 4z + 9) = 0$
 $\Rightarrow x(2 + 5\lambda) + y(1 - 3\lambda) + z(4\lambda - 1) + 9\lambda - 3 = 0$

This plane is parallel to the line

$$\frac{x+2}{2} = \frac{3-y}{-4} = \frac{z-7}{5}$$

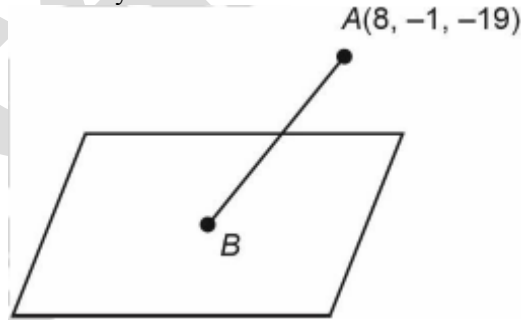
$$\therefore (2 + 5\lambda)(2) + (1 - 3\lambda)(4) + (4\lambda - 1)5 = 0$$

$$\Rightarrow 4 + 10\lambda + 4 - 12\lambda + 20\lambda - 5 = 0$$

$$\Rightarrow 18\lambda = -3 \Rightarrow \lambda = \frac{-1}{6}$$

$$\therefore \text{Plane P : } \frac{7}{6}x + \frac{3}{2}y - \frac{5}{3}z - \frac{9}{2} = 0$$

$$\Rightarrow 7x + 9y - 10z - 27 = 0$$



$$AB : \frac{x-8}{-3} = \frac{y+1}{4} = \frac{z+19}{12} = k$$

$$\begin{aligned} B &= (-3k + 8, 4k - 1, 12k - 19) \\ B \text{ lies on plane P.} \\ 7(-3k + 8) + 9(4k - 1) - 10(12k - 19) &= 27 \\ \Rightarrow -21k + 56 + 36k - 9 - 120k + 190 &= 27 \\ \Rightarrow -105k &= -210 \\ \Rightarrow k &= 2 \\ \therefore B &= (2, 7, 5) \\ AB &= \sqrt{36 + 64 + 576} \\ &= \sqrt{676} = 26 \end{aligned}$$

PHYSICS

Section-A: Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Q.31 A flask contains Hydrogen and Argon in the ratio 2 : 1 by mass. The temperature of the mixture is 30°C. The ratio of average kinetic energy per molecule of the two gases (K argon/K hydrogen) is: (Given : Atomic Weight of Ar = 39.9)

- (1) 2 (2) 1 (3) 39.9 (4) $\frac{39.9}{2}$

Ans. [2]

Sol. $KE = \frac{1}{2}mv_{avg}^2 = \frac{4RT}{\pi}$
 $\Rightarrow \frac{KE_{H_2}}{KE_{Ar}} = 1$

Q.32 A 12 V battery connected to a coil of resistance 6 Ω through a switch, drives a constant current in the circuit. The switch is opened in 1 ms. The emf induced across the coil is 20 V. The inductance of the coil is :

- (1) 10 mH (2) 8 mH (3) 5 mH (4) 12 mH

Ans. [1]

Sol. $V = 12 \text{ volt}$
 $R = 6 \Omega$
 $t = 1 \text{ ms}$
 $\frac{d\phi}{dt} = L \frac{dI}{dt}$
 $20 = L \times \frac{2}{10^{-3}}$
 $L = 10 \text{ mH}$

Q.33 Two identical particles each of mass 'm' go round a circle of radius a under the action of their mutual gravitational attraction. The angular speed of each particle will be :

- (1) $\sqrt{\frac{Gm}{a^3}}$ (2) $\sqrt{\frac{Gm}{8a^3}}$ (3) $\sqrt{\frac{Gm}{4a^3}}$ (4) $\sqrt{\frac{Gm}{2a^3}}$

Ans. [3]

Sol. $m\omega^2 a = \frac{Gmm}{4a^2}$
 $\omega = \sqrt{\frac{Gm}{4a^3}}$

Q.34 The position vector of a particle related to time t is given by

$$\vec{r} = (10t\hat{i} + 15t^2\hat{j} + 7t\hat{k})\text{m}$$

The direction of net force experienced by the particle is :

- (1) Positive x-axis (2) In x-y plane (3) Positive y-axis (4) Positive z-axis

Ans. [3]

Sol. $\vec{F} = 30\hat{j}$

Q.35 The half-life of a radioactive nucleus is 5 years. The fraction of the original sample that would decay in 15 years is :

- (1) $\frac{1}{8}$ (2) $\frac{1}{4}$ (3) $\frac{7}{8}$ (4) $\frac{3}{4}$

Ans. [3]

Sol. $N = N_0 2^{-t/T_{1/2}}$

$$\Rightarrow N = \frac{N_0}{8}$$

$$\Rightarrow \text{Decayed amount} = \frac{N_0}{8}$$

Q.36 Match List-I with List II of Electromagnetic waves with corresponding wavelength range:

List I

List II

(A) Microwave

(I) 400 nm to 1 nm

(B) Ultraviolet

(II) 1 nm to 10^{-3} nm

(C) X-Ray

(III) 1 mm to 700 nm

(D) Infra-red

(IV) 0.1 m to 1 mm

Choose the correct answer from the options given below:

(1) (A)-(IV), (B)-(I), (C)-(II), (D)-(III)

(2) (A)-(IV), (B)-(I), (C)-(III), (D)-(II)

(3) (A)-(IV), (B)-(II), (C)-(I), (D)-(III)

(4) (A)-(I), (B)-(IV), (C)-(II), (D)-(III)

Ans. [1]

Sol. $\lambda_X < \lambda_{UV} < \lambda_{IR} < \lambda_{MW}$

Q.37 A wire of length 'L' and radius 'r' is clamped rigidly at one end. When the other end of the wire is pulled by a force f , its length increases by ' ℓ '. Another wire of same material of length '2L' and radius '2r' is pulled by a force '2f'. Then the increase in its length will be:

- (1) 4ℓ (2) $\ell/2$ (3) 2ℓ (4) ℓ

Ans. [4]

Sol. $\sigma = \frac{\ell}{L} = \frac{F}{\pi r^2 y}$

$$\sigma' = \frac{\ell'}{2L} = \frac{2F}{4\pi r^2 y} \Rightarrow \ell' = \ell$$

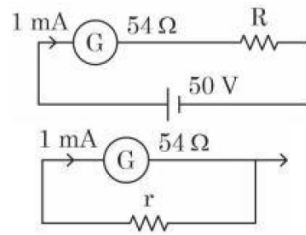
Q.38 The de Broglie wavelength of an electron having kinetic energy E is λ . If the kinetic energy of electron becomes $\frac{E}{4}$, then its de-Broglie wavelength will be:

- (1) $\sqrt{2}\lambda$ (2) $\frac{\lambda}{\sqrt{2}}$ (3) $\frac{\lambda}{2}$ (4) 2λ

Ans. [4]

Sol. $\lambda = \frac{h}{\sqrt{2mKE}}$

Q.39 For designing a voltmeter of range 50 V and an ammeter of range 10 mA using a galvanometer which has a coil of resistance 54Ω showing a full scale deflection for 1 mA as in figure.



- (A) for voltmeter $R \approx 50 \text{ k}\Omega$
- (B) for ammeter $r \approx 0.2 \Omega$
- (C) for ammeter $r \approx 6 \Omega$
- (D) for voltmeter $R \approx 5 \text{ k}\Omega$
- (E) for voltmeter $R \approx 500 \Omega$

Choose the correct answer from the options given below:

- (1) (A) and (C) (2) (C) and (E) (3) (C) and (D) (4) (A) and (B)

Ans. [1]

Sol. $50 = (R_G + R)10^{-3}$
 $5000 = 54 + R$
 $R \approx 50 \text{ k}\Omega$
 $10^{-3} \times 54 = r \times 9 \times 10^{-3}$
 $r = 6 \Omega$

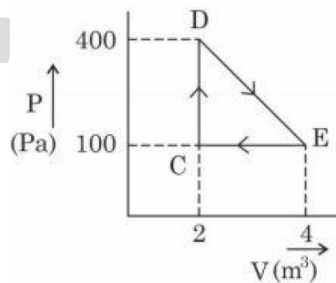
Q.40 The height of transmitting antenna is 180 m and the height of the receiving antenna is 245 m. The maximum distance between them for satisfactory communication in line of sight will be: (given $R = 6400 \text{ km}$)

- (1) 96 km (2) 56 km (3) 48 km (4) 104 km

Ans. [4]

Sol. $R_{\text{max}} = \sqrt{2 \times 180 \times 6400 \times 10^3} + \sqrt{2 \times 245 \times 6400 \times 10^3}$
 $= 6 \times 80 \times 10^2 + 7 \times 80 \times 10^2$
 $= 104 \text{ km}$

Q.41 A thermodynamic system is taken through cyclic process. The total work done in the process is :



- (1) 200 J (2) 300 J (3) 100 J (4) Zero

Ans. [2]

Sol. $W = \frac{2 \times 300}{2} \text{ J} = 300 \text{ J}$

- Q.42** A single slit of width 'a' is illuminated by a monochromatic light of wavelength 600 nm. The value of 'a' for which first minimum appears at $\theta = 30^\circ$ on the screen will be :
- (1) $1.2 \mu\text{m}$ (2) $3 \mu\text{m}$ (3) $1.8 \mu\text{m}$ (4) $0.6 \mu\text{m}$

Ans. [1]

Sol. $d\sin\theta = \lambda$
 $\Rightarrow d = 2\lambda = 1.2 \mu\text{m}$

- Q.43** A vector in x – y plane makes an angle of 30° with y-axis. The magnitude of y-component of vector is $2\sqrt{3}$. The magnitude of x-component of the vector will be :
- (1) $\frac{1}{\sqrt{3}}$ (2) 6 (3) 2 (4) $\sqrt{3}$

Ans. [3]

Sol. $a_y = 2\sqrt{3}$
 $\therefore a_x = a_y \tan 30^\circ = 2\sqrt{3} \times \frac{1}{\sqrt{3}}$

- Q.44** The position of a particle related to time is given by $x = (5t^2 - 4t + 5)$ m. The magnitude of velocity of the particle at $t = 2$ s will be :
- (1) 06 ms^{-1} (2) 14 ms^{-1} (3) 10 ms^{-1} (4) 16 ms^{-1}

Ans. [4]

Sol. $x = 5t^2 - 4t + 5$
 $\Rightarrow v = 10t - 4$
 $\Rightarrow v = 16 \text{ m/s}$

- Q.45** The electric field due to a short electric dipole at a large distance (r) from center of dipole on the equatorial plane varies with distance as :
- (1) r (2) $\frac{1}{r^2}$ (3) $\frac{1}{r^3}$ (4) $\frac{1}{r}$

Ans. [3]

Sol. $E = \frac{2kp}{r^3}$

- Q.46** In a linear Simple Harmonic Motion (SHM)
- (A) Restoring force is directly proportional to the displacement.
(B) The acceleration and displacement are opposite in direction.
(C) The velocity is maximum at mean position.
(D) The acceleration is minimum at extreme points.

Choose the correct answer from the options given below:

- (1) (C) and (D) only (2) (A), (C) and (D) only
(3) (A), (B) and (C) only (4) (A), (B) and (D) only

Ans. [3]

Sol. $F = -kx$
 $a = -\omega^2 x$
Velocity is maximum at mean position.

- Q.47** The speed of a wave produced in water is given by $v = \lambda^a g^b \rho^c$. Where λ , g and ρ are wavelength of wave, acceleration due to gravity and density of water respectively. The values of a, b and c respectively, are
- (1) 1, -1, 0 (2) $\frac{1}{2}$, 0, $\frac{1}{2}$ (3) 1, 1, 0 (4) $\frac{1}{2}$, $\frac{1}{2}$, 0

Ans. [4]

Sol. $[v] = [\lambda^a g^b \rho^c]$
 $\Rightarrow [LT^{-1}] = [L]^a [LT^{-2}]^b [ML^{-3}]^c$

Q.48 A body is released from a height equal to the radius (R) of the earth. The velocity of the body when it strikes the surface of the earth will be: (Given g = acceleration due to gravity on the earth.)

- (1) $\sqrt{2gR}$ (2) \sqrt{gR} (3) $\sqrt{4gR}$ (4) $\sqrt{\frac{gR}{2}}$

Ans. [2]

Sol.
$$-\frac{GMm}{2R} = -\frac{GMm}{R} + \frac{1}{2}mv^2$$

$$\Rightarrow \frac{1}{2}mv^2 = \frac{GMm}{2R}$$

$$v = \sqrt{\frac{GM}{R}} = \sqrt{gR}$$

Q.49 Given below are two statements:

Statement I : The equivalent resistance of resistors in a series combination is smaller than least resistance used in the combination.

Statement II: The resistivity of the material is independent of temperature.

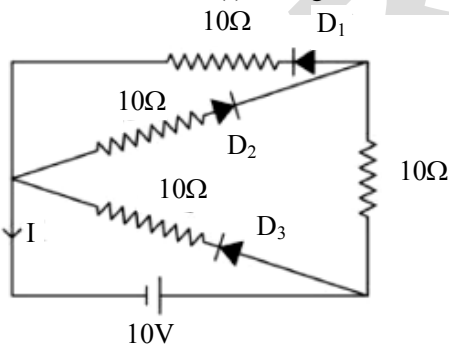
In the light of the above statements, choose the correct answer from the options given below:

- (1) Both Statement I and Statement II are false
 (2) Both Statement I and Statement II are true
 (3) Statement I is true but Statement II is false
 (4) Statement I is false but Statement II is true

Ans. [1]

Sol. $R_{\text{series}} > R_1 \text{ or } R_2$
 as $R_{\text{series}} = R_1 + R_2$
 $\rho = \rho_0 (1 + \alpha\Delta T)$

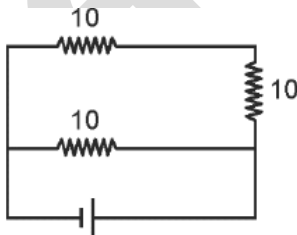
Q.50 In the given circuit, the current (I) through the battery will be



- (1) 2.5 A (2) 1 A (3) 2 A (4) 1.5 A

Ans. [4]

Sol.



$$\Rightarrow R_{\text{eq}} = \frac{20}{3} \Omega$$

$$I = \frac{30}{20} \text{ A} = 1.5 \text{ A}$$

Section-B: Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE**. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g. 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

Q.51 The fundamental frequency of vibration of a string between two rigid support is 50 Hz. The mass of the string is 18 g and its linear mass density is 20 g/m. The speed of the transverse waves so produced in the string is _____ ms^{-1} .

Ans. [90]

Sol. $\frac{v}{2\ell} = 50$

$$v = 100 \times \ell = \frac{100 \times 18}{20} = 90 \text{ m/s}$$

Q.52 A block of mass 10 kg is moving along x-axis under the action of force $F = 5x$ N. The work done by the force in moving the block from $x = 2$ m to 4 m will be _____ J.

Ans. [30]

Sol. $F = 5x$

$$W = \frac{5}{2}(x_f^2 - x_i^2) = \frac{5}{2} \times 12 = 30 \text{ J}$$

Q.53 A solid sphere and a solid cylinder of same mass and radius are rolling on a horizontal surface without slipping. The ratio of their radius of gyrations respectively ($k_{\text{sph}} : k_{\text{cyl}}$) is $2 : \sqrt{x}$. The value of x is _____.

Ans. [5]

Sol. Considering rotational axis as the diametrical axis for sphere and axis of cylinder. Then

$$K_1^2 = \frac{2}{5}R^2 \text{ and } K_2^2 = \frac{1}{2}R^2$$

$$\therefore \frac{K_1}{K_2} = \sqrt{\frac{2/5}{1/2}} = \sqrt{\frac{4}{5}}$$

$$\Rightarrow \frac{K_1}{K_2} = \frac{2}{\sqrt{5}}$$

$$\therefore x = 5$$

Q.54 An electron in a hydrogen atom revolves around its nucleus with a speed of $6.76 \times 10^6 \text{ ms}^{-1}$ in an orbit of radius 0.52 \AA . The magnetic field produced at the nucleus of the hydrogen atom is _____ T.

Ans. [40]

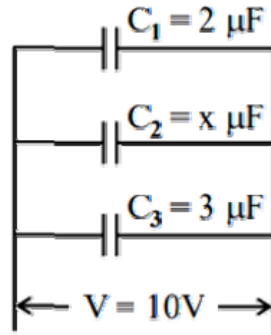
Sol. $B = \frac{\mu_0 I}{2r} = \frac{\mu_0 e \times \omega}{2\pi \times 2 \times r}$
 $= \frac{10^{-7} \times 1.6 \times 6.76 \times 10^6 \times 10^{-19}}{0.52 \times 0.52 \times 10^{-20}} = 40$

Q.55 There is an air bubble of radius 1.0 mm in a liquid of surface tension 0.075 Nm^{-1} and density 1000 kg m^{-3} at a depth of 10 cm below the free surface. The amount by which the pressure inside the bubble is greater than the atmospheric pressure is _____ Pa ($g = 10 \text{ ms}^{-2}$)

Ans. [1150]

Sol. $\Delta P = \rho gh + \frac{2T}{r} = 1000 + \frac{2 \times 0.075}{10^{-3}}$
 $= 1000 + 150 = 1150$

Q.56 In the given figure the total charge stored in the combination of capacitors is $100 \mu\text{C}$. The value of 'x' is _____.



Ans. [5]

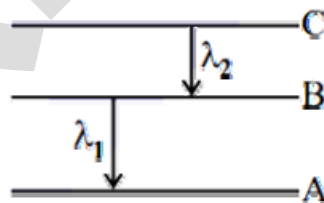
Sol. $10(2 + x + 3) = 100$
 $\Rightarrow x = 5$

Q.57 A 20 cm long metallic rod is rotated with 210 rpm about an axis normal to the rod passing through its one end. The other end of the rod is in contact with a circular metallic ring. A constant and uniform magnetic field 0.2 T parallel to the axis exists everywhere. The emf developed between the centre and the ring is _____ mV. Take $\pi = \frac{22}{7}$

Ans. [88]

Sol. $\varepsilon = \frac{B\omega l^2}{2}$
 $= 0.2 \times \frac{210 \times 2\pi}{60} \times \frac{(0.2)^2}{2}$
 $= \frac{0.2 \times 210 \times 22 \times 0.04}{7 \times 60}$
 $= 88 \text{ mV}$

Q.58 As per given figure A, B and C are the first, second and third excited energy levels of hydrogen atom respectively. If the ratio of the two wavelengths (i.e. $\frac{\lambda_1}{\lambda_2}$) is $\frac{7}{4n}$, then the value of n will be _____.



Ans. [5]

Sol. $\frac{\lambda_1}{\lambda_2} = \frac{\left(\frac{1}{9} - \frac{1}{16}\right)}{\left(\frac{1}{4} - \frac{1}{9}\right)} = \frac{7}{4n}$
 $\Rightarrow \frac{\lambda_1}{\lambda_2} = \frac{7}{20}$

Q.59 The refractive index of a transparent liquid filled in an equilateral hollow prism is $\sqrt{2}$. The angle of minimum deviation for the liquid will be _____°.

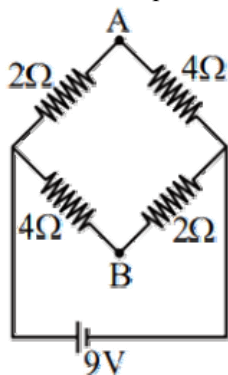
Ans. [30]

Sol.
$$\sqrt{2} = \frac{\sin\left(30 + \frac{\delta}{2}\right)}{\frac{1}{2}}$$

$$\Rightarrow 45^\circ = 30^\circ + \frac{\delta}{2}$$

$$\delta = 30^\circ$$

Q.60 A network of four resistances is connected to 9 V battery, as shown in figure. The magnitude of voltage difference between the points A and B is _____ V.



Ans. [3]

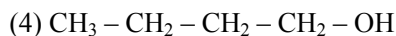
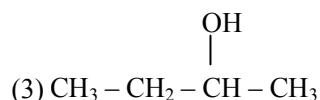
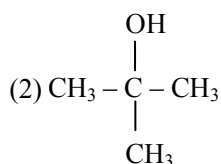
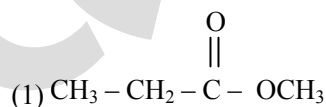
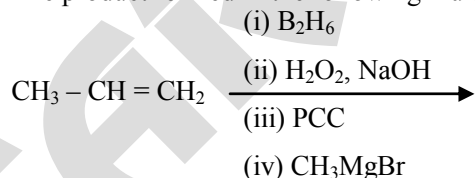
Sol. $I_A = I_B = 1.5 \text{ A}$

$$V_A - V_B = 4 \times 1.5 - 2 \times 1.5 = 3$$

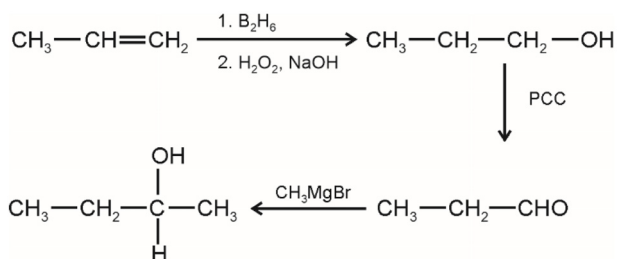
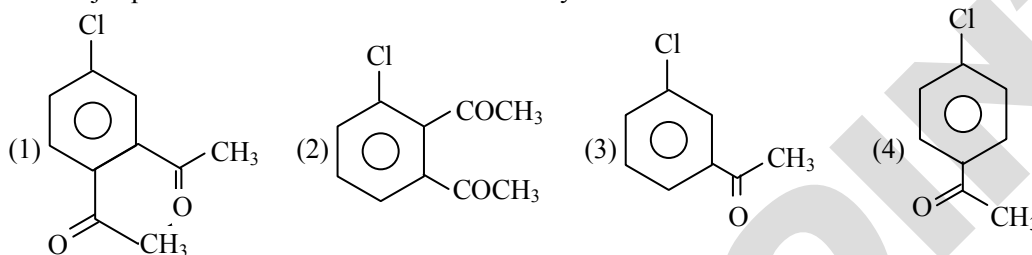
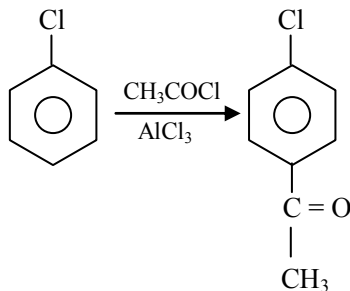
CHEMISTRY

Section-A: This section contains 20 multiple choice questions. Each question has 4 choices(1), (2), (3) and (4), out of which **ONLY ONE** is correct..

Q.61 The product formed in the following multistep reaction is :



Ans. [3]

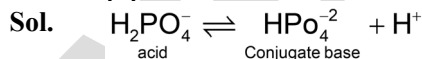
Sol.

Q.62 The major product formed in the Friedel-Craft acylation of chlorobenzene is

Ans. [4]
Sol.

Q.63 Which of the following statement(s) is/are correct ?

- (A) The pH of 1×10^{-8} M HCl solution is 8
 (B) The conjugate base of H_2PO_4^- is HPO_4^{2-}
 (C) K_w increases with increase in temperature
 (D) When a solution of a weak monoprotic acid is titrated against a strong base at half neutralisation point,

$$\text{pH} = \frac{1}{2} \text{pK}_a$$

Choose the correct answer from the options given below :

- (1) (B), (C) (2) (A), (D) (3) (A), (B), (C) (4) (B), (C), (D)

Ans. [1]


K_w increase with increase in temperature as dissociation of water increases with increase in temperature. When weak monoprotic acid is titrated against strong base, at half neutralization point, the solution becomes acidic buffer and its pH is given by

$$\text{pH} = \text{pK}_a + \log \frac{[\text{Salt}]}{[\text{Acid}]}$$

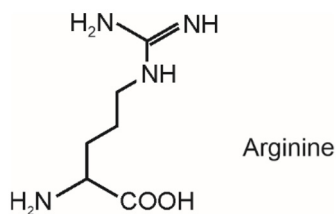
$$\Rightarrow \text{pH} = \text{pK}_a + 0 \quad \text{as } [\text{salt}] = [\text{acid}]$$

Q.64 Which is not true for arginine ?

- (1) It has a fairly high melting point (2) It is associated with more than one pK_a values
 (3) It has high solubility in benzene (4) It is a crystalline solid

Ans. [3]

Sol.



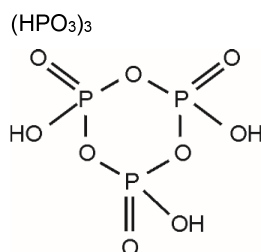
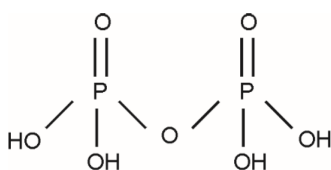
Since arginine is polar, it is not soluble in benzene.

Q.65 The number of P – O – P bonds in $H_4P_2O_7$, $(HPO_3)_3$ and P_4O_{10} are respectively
 (1) 0, 3, 6 (2) 0, 3, 4 (3) 1, 2, 4 (4) 1, 3, 6

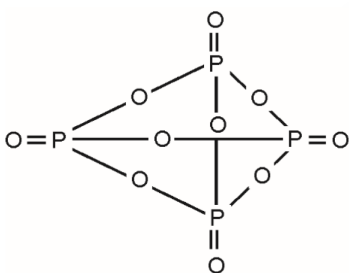
Ans. [4]

Sol.

$H_4P_2O_7$:



P_4O_{10}



Q.66 The possibility of photochemical smog formation will be minimum at
 (1) Srinagar, Jammu and Kashmir in January
 (2) Kolkata in October
 (3) Mumbai in May
 (4) New-Delhi in August (Summer)

Ans. [1]

Sol. Photochemical smog occurs in warm, dry and sunny climate. Hence the correct answer is option (1)

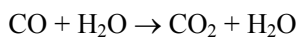
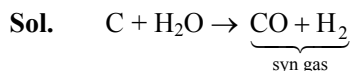
Q.67 The complex with highest magnitude of crystal field splitting energy (Δ_0) is
 (1) $[Ti(OH_2)_6]^{3+}$ (2) $[Cr(OH_2)_6]^{3+}$ (3) $[Mn(OH_2)_6]^{3+}$ (4) $[Fe(OH_2)_6]^{3+}$

Ans. [2]

Sol.	Complex	CFSE
	$[Ti(OH_2)_6]^{3+}$	$-0.4 \Delta_0$
	$[Cr(H_2O)_6]$	$-1.2 \Delta_0$
	$[Mn(H_2O)_6]^{3+}$	$-0.6 \Delta_0$
	$[Fe(H_2O)_6]^{3+}$	0

- Q.68** During water-gas shift reaction
- (1) Carbon monoxide is oxidized to carbon dioxide
 - (2) Water is evaporated in presence of catalyst
 - (3) Carbon is oxidized to carbon monoxide
 - (4) Carbon dioxide is reduced to carbon monoxide

Ans. [1]

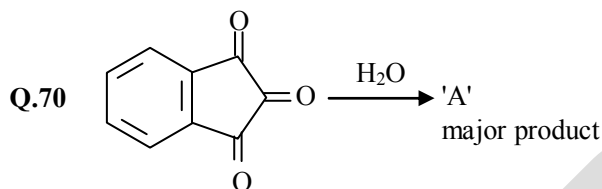


Water gas shift reaction

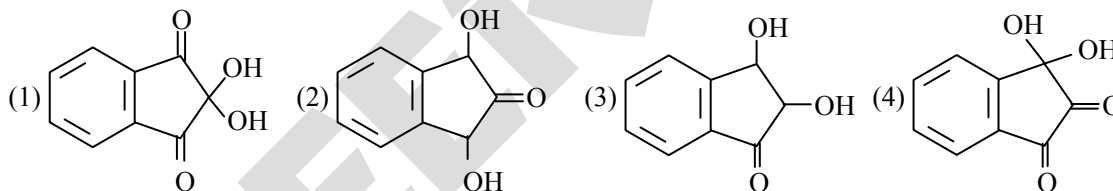
- Q.69** Which of the following statement is correct for paper chromatography ?
- (1) Water present in the pores of the paper forms the stationary phase
 - (2) Paper sheet forms the stationary phase
 - (3) Water present in the mobile phase gets absorbed by the paper which then forms the stationary phase
 - (4) Paper and water present in its pores together form the stationary phase

Ans. [1]

Sol. In paper chromatography water present in the pores of the paper forms the stationary phase.

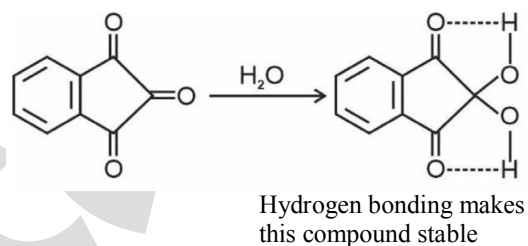


'A' formed in the above reaction is

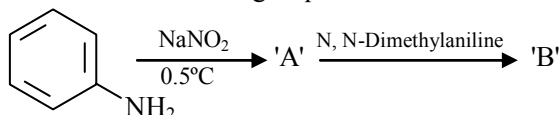


Ans. [1]

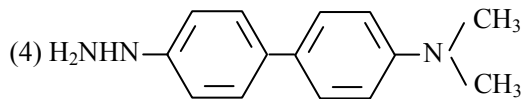
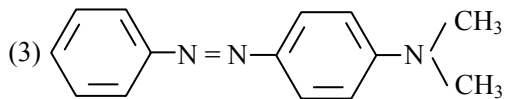
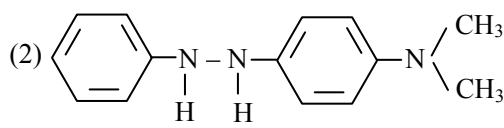
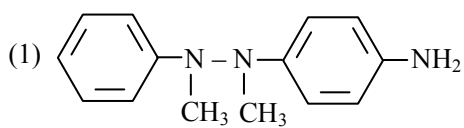
Sol.



- Q.71** Consider the following sequence of reactions

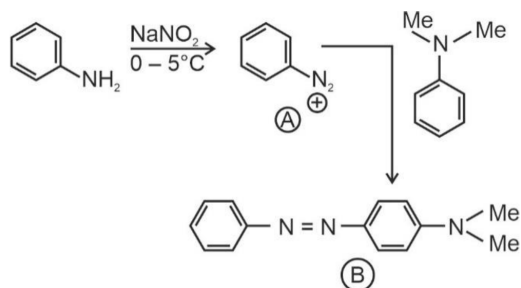


The product 'B' is



Ans. [3]

Sol.



Q.72 Given below are two statements

Statement I : According to Bohr's model of hydrogen atom, the angular momentum of an electron in a given stationary state is quantised.

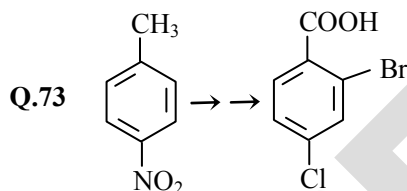
Statement II : The concept of electron in Bohr's orbit, violates the Heisenberg uncertainty principle.

In the light of the above statements, choose the most appropriate answer from the options given below

- (1) Statement I is incorrect but Statement II is correct
- (2) Both Statement I and Statement II are correct
- (3) Both Statement I and Statement II are incorrect
- (4) Statement I is correct but Statement II is incorrect

Ans. [2]

Sol. Both Statement I and Statement II are correct

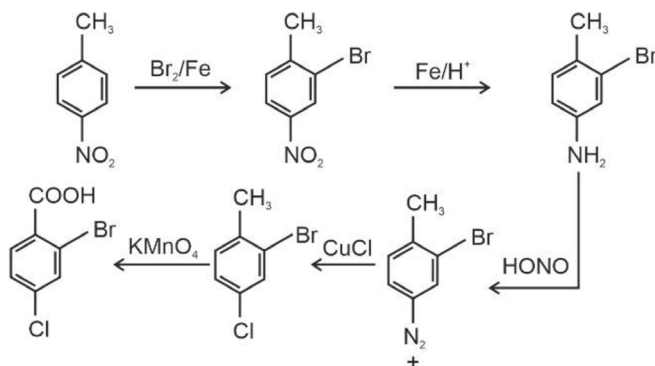


In the above conversion the correct sequence of reagents to be added is

- (1) (i) KMnO_4 , (ii) Br_2/Fe , (iii) Fe/H^+ , (iv) Cl_2
- (2) (i) Br_2/Fe , (ii) Fe/H^+ , (iii) KMnO_4 , (iv) Cl_2
- (3) (i) Fe/H^+ , (ii) HONO , (iii) CuCl , (iv) KMnO_4 , (v) Br_2
- (4) (i) Br_2/Fe , (ii) Fe/H^+ , (iii) HONO , (iv) CuCl (v) KMnO_4

Ans. [4]

Sol.



Q.74 Which one of the following is not an example of calcination ?

- (1) $\text{CaCO}_3 \xrightarrow{\Delta} \text{CaO} + \text{CO}_2$ (2) $\text{Fe}_2\text{O}_3 \cdot x\text{H}_2\text{O} \xrightarrow{\Delta} \text{Fe}_2\text{O}_3 + x\text{H}_2\text{O}$
 (3) $2\text{PbS} + 3\text{O}_2 \xrightarrow{\Delta} 2\text{PbO} + 2\text{SO}_2$ (4) $\text{CaCO}_3 \cdot \text{MgCO}_3 \xrightarrow{\Delta} \text{CaO} + \text{MgO} + 2\text{CO}_2$

Ans. [3]

Sol. $2\text{PbS} + 3\text{O}_2 \xrightarrow{\Delta} 2\text{PbO} + 2\text{SO}_2$
 The above reaction is an example of roasting

Q.75 Consider the following statement

- (A) NF_3 molecules has a trigonal planar structure.
 (B) Bond length of N_2 is shorter than O_2
 (C) Isoelectronic molecules or ions have identical bond order.
 (D) Dipole moment of H_2S is higher than that of water molecule.

Choose the correct answer from the options given below :

- (1) (A) and (B) are correct (2) (A) and (D) are correct
 (3) (C) and (D) are correct (4) (B) and (C) are correct

Ans. [4]

Sol. NF_3 is pyramidal
 B.O of $\text{N}_2 = 3$, B.O of $\text{O}_2 = 4$
 Hence bond length of N_2 is shorter than O_2
 Isoelectronic species have identical bond order



Dipole moment of H_2O is more than that of H_2S due to higher electronegativity of O.

Q.76 Given below are two statements : One is labelled as Assertion A and the other is labelled as Reason R:

Assertion (A) : BeCl_2 and MgCl_2 produce characteristic flame.

Reason (R) : The excitation energy is high in BeCl_2 and MgCl_2 .

In the light of the above statements, choose the correct answer from the options given below :

- (1) (A) is true but (R) is false
 (2) Both (A) and (R) are true but (R) is NOT the correct explanation of (A)
 (3) Both (A) and (R) are true and (R) is the correct explanation of (A)
 (4) (A) is false but (R) is true

Ans. [4]

Sol. BeCl_2 and MgCl_2 do not produce characteristic flame because excitation energy is high in BeCl_2 and MgCl_2 . Hence, the correct answer is option (4)

Q.77 Which of the following expressions is correct in case of a CsCl unit cell (edge length 'a')?

- (1) $r_{\text{Cs}^+} + r_{\text{Cl}^-} = \frac{a}{2}$ (2) $r_{\text{Cs}^+} + r_{\text{Cl}^-} = \frac{\sqrt{3}}{2}a$ (3) $r_{\text{Cs}^+} + r_{\text{Cl}^-} = \frac{a}{\sqrt{2}}$ (4) $r_{\text{Cs}^+} + r_{\text{Cl}^-} = a$

Ans. [2]

Sol. CsCl has body centered type structure in which Cs^+ occupies at corner of a cube and Cl^- occupies the centre of the cube.

$$2r_{\text{Cs}^+} + 2r_{\text{Cl}^-} = \sqrt{3}a \quad (\text{where } a \text{ is the edge length of the cube})$$

$$r_{\text{Cs}^+} + r_{\text{Cl}^-} = \frac{\sqrt{3}}{2}a$$

Q.78 For a good quality cement, the ratio of silica to alumina is found to be

- (1) 1.5 (2) 4.5 (3) 2 (4) 3

Ans. [4]

Sol. For a good quality cement, the ratio of silica to alumina lies between 2.5 and 4

Q.79 Match List I with List II

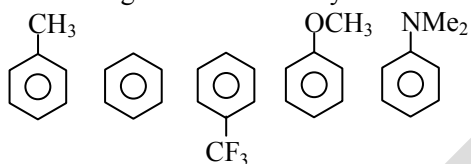
List I (Monomer)	List II (Polymer)
(A) Tetrafluoroethene	(i) Orlon
(B) Acrylonitrile	(ii) Natural rubber
(C) Caprolactam	(iii) Teflon
(D) Isoprene	(iv) Nylon-6

Choose the correct answer from the options given below :

- (1) (A)-(iii), (B)-(i), (C)-(iv), (D)-(ii)
- (2) (A)-(iv), (B)-(i), (C)-(ii), (D)-(iii)
- (3) (A)-(iii), (B)-(iv), (C)-(ii), (D)-(i)
- (4) (A)-(ii), (B)-(iii), (C)-(iv), (D)-(i)

Ans. [1]
Sol.

List I (Monomer)	List II (Polymer)
(A) Tetrafluoroethene	(i) Teflon
(B) Acrylonitrile	(ii) Orlon
(C) Caprolactam	(iii) Nylon-6
(D) Isoprene	(iv) Natural rubber

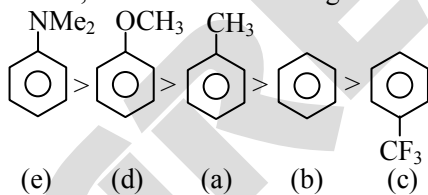
Q.80 Decreasing order of reactivity towards electrophilic substitution for the following compounds is


- (1) $d > a > e > c > b$
- (2) $e > d > a > b > c$
- (3) $a > d > e > b > c$
- (4) $c > b > a > d > e$

Ans. [2]
Sol.

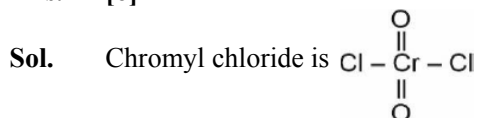
Reactivity of aromatic compounds towards electrophilic substitution depends on the electron density on benzene ring. Higher the electron density on benzene ring, more be the reactivity towards electrophilic substitution reaction.

Hence, the correct decreasing order is



Section-B: Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE**. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g. 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer..

Q.81 In Chromyl chloride, the oxidation state of chromium is (+) _____.

Ans. [6]


Hence the O.S. of Cr is +6

- Q.82** The vapour pressure of 30% (w/v) aqueous solution of glucose is _____ mm Hg at 25°C.
[Given: The density of 30% (w/v), aqueous solution of glucose is 1.2 g cm⁻³ and vapour pressure of pure water is 24 mm Hg.] (Molar mass of glucose is 180 g mol⁻¹)

Ans. [23]

Sol. Wt. of solution = 100 × 1.2 = 120 gm

Wt. of water = 120 – 30 = 90 gm

Now using formula

$$\frac{P_0 - P}{P} = \frac{\text{moles of glucose}}{\text{moles of water}}$$

$$\frac{24 - P}{P} = \frac{\frac{30}{180}}{\frac{90}{180}} = \frac{3}{90}$$

$$24 \times 90 - P \times 90 = 3 P$$

$$\Rightarrow P = 23.22$$

- Q.83** The volume (in mL) of 0.1 M AgNO₃ required for complete precipitation of chloride ions present in 20 mL of 0.01 M solution of [Cr(H₂O)₅Cl]Cl₂ as silver chloride is _____

Ans. [4]

Sol. (Cr(H₂O)₅Cl) Cl₂ → (Cr(H₂O)₅Cl) 2Cl⁻

Molarity of Cl⁻ ions = 0.01 × 2 = 0.02 M

∴ Millimoles of Cl⁻ ions in the given solution
= 20 × 0.02

∴ Millimoles of AgNO₃ required = 20 × 0.2

$$V \times 0.1 = 20 \times 0.02$$

$$V = 4 \text{ mL}$$

- Q.84** For a reversible reaction A \rightleftharpoons B, the $\Delta H_{\text{forward reaction}} = 20 \text{ kJ mol}^{-1}$. The activation energy of the uncatalyzed forward reaction is 300 kJ mol⁻¹. When the reaction is catalysed keeping the reactant concentration same, the rate of the catalysed forward reaction at 27°C is found to be same as that of the uncatalyzed reaction at 327°C. The activation energy of the catalysed backward reaction is _____ kJ mol⁻¹.

Ans. [130]

Sol. As per the question

$$Ae^{\frac{300 \times 10^3}{600 \times R}} = Ae^{\frac{-E_a}{300 \times R}}$$

$$\Rightarrow \frac{10^3}{2} = \frac{E_a}{300}$$

$$\Rightarrow E_a = 150 \times 10^3 \text{ J mol}^{-1}$$

$$\Rightarrow E_a = 150 \text{ kJ mol}^{-1}$$

∴ Activation energy of catalysed backward reaction

$$= E_a - \Delta H$$

$$= 150 - 20 = 130 \text{ kJ mol}^{-1}$$

- Q.85** The homoleptic and octahedral complex of Co²⁺ and H₂O has _____ unpaired electron(s) in the t_{2g} set of orbitals.

Ans. [1]

Sol. [Co(H₂O)₆]²⁺ = d⁷ (H.S.) = t_{2g}⁵ e_g²

- Q.86** The number of correct statements from the following is _____
(A) Conductivity always decreases with decrease in concentration for both strong and weak electrolytes.
(B) The number of ions per unit volume that carry current in a solution increases on dilution.
(C) Molar conductivity increases with decrease in concentration.
(D) The variation in molar conductivity is different for strong and weak electrolytes.
(E) For weak electrolytes, the change in molar conductivity with dilution is due to decrease in degree of dissociation.

Ans. [3]

Sol. Except (B) and (E), all statements are correct.

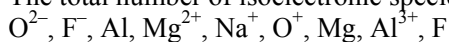
- Q.87** The total change in the oxidation state of manganese involved in the reaction of KMnO_4 and potassium iodide in the acidic medium is _____.

Ans. [5]



Hence the change in O.S. of Mn is (5).

- Q.88** The total number of isoelectronic species from the given set is _____.



Ans. [5]

Sol.

Species	No. of electrons
O^{2-}	10
F^-	10
Al	13
Mg^{2+}	10
Na^+	10
O^+	7
Mg	12
Al^{3+}	10
F	9

Hence five species among the given are isoelectronic species.

- Q.89** 20 mL of 0.5 M NaCl is required to coagulate 200 mL of As_2S_3 solution in 2 hours. The coagulating value of NaCl is _____.

Ans. [50]

Sol. Coagulating value = $\frac{20 \times 0.5}{200} \times 1000 = 50$

- Q.90** 30.4 kJ of heat is required to melt one mole of sodium chloride and the entropy change at the melting point is $28.4 \text{ J K}^{-1} \text{ mol}^{-1}$ at 1 atm. The melting point of sodium chloride is _____ K (Nearest Integer)

Ans. [1070]

Sol. Melting point = $\frac{\Delta H_{\text{fus}}}{\Delta S}$
 $= \frac{30.4 \times 10^3}{28.4} = 1070 \text{ K}$