

JEE MAIN ONLINE PAPER 2021

Held on February 26, 2021 (Morning)

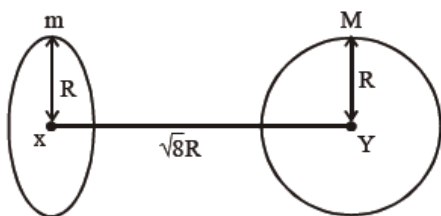
Instructions

1. This test will be a 3 hours Test.
2. This test consists of Physics, Chemistry and Mathematics questions with equal weightage of 100 marks.
3. Each question is of 4 marks.
4. In the question paper consisting of Physics (Q.no. 1 to 30), Chemistry (Q.no. 31 to 60) and Mathematics (Q.no. 61 to 90). There are two sections for each subject (Section-A : MCQ Type & Section-B : Numerical Response Type). Section-A consists of 20 multiple choice questions & Section-B consists of 10 Numerical Value type Questions. **Candidates have a choice to Answer 5 out of the 10 numerical value answer based questions per section.**
5. There will be only one correct choice in the given four choices in Section-A. For each question 4 marks will be awarded for correct choice, 1 mark will be deducted for incorrect choice and zero mark will be awarded for not attempted question. For Section-B questions 4 marks will be awarded for correct answer and zero for unattempted and incorrect answer.
6. Any textual, printed or written material, mobile phones, calculator etc. is not allowed for the students appearing for the test.
7. All calculations/written work should be done in the rough sheet provided.

PHYSICS

Section -A

- Q.1** Find the gravitational force of attraction between the ring and sphere as shown in the diagram, where the plane of the ring is perpendicular to the line joining the centres. If $\sqrt{8}R$ is the distance between the centres of a ring (of mass 'm') and a sphere (mass 'M') where both have equal radius 'R'.+



- (1) $\frac{\sqrt{8}}{9} \cdot \frac{GmM}{R}$ (2) $\frac{2\sqrt{2}}{3} \cdot \frac{GMm}{R^2}$
(3) $\frac{1}{3\sqrt{8}} \cdot \frac{GMm}{R^2}$ (4) $\frac{\sqrt{8}}{27} \cdot \frac{GmM}{R^2}$

- Q.2** Consider the combination of 2 capacitors C_1 and C_2 , with $C_2 > C_1$, when connected in parallel, the equivalent capacitance is $\frac{15}{4}$ time the equivalent capacitance of the same connected in series. Calculate the ratio of capacitors, $\frac{C_2}{C_1}$.

- (1) $\frac{15}{11}$ (2) $\frac{111}{80}$
(3) $\frac{29}{15}$ (4) $\frac{15}{4}$

- Q.3** In a typical combustion engine the work done by a gas molecule is given $W = \alpha^2 \beta e^{\frac{-\beta x^2}{kT}}$ where x is the displacement, k is the Boltzmann constant and T is the temperature. If α and β are constants, dimensions of α will be :
- (1) $[MLT^{-2}]$ (2) $[M^0LT^0]$
(3) $[M^2LT^{-2}]$ (4) $[MLT^{-1}]$

- Q.4** If λ_1 and λ_2 are the wavelengths of the third member of Lyman and first member of the Paschen series respectively, then the value of $\lambda_1 : \lambda_2$ is :
 (1) 1 : 9 (2) 7 : 108
 (3) 7 : 135 (4) 1 : 3
- Q.5** A short straight object of height 100 cm lies before the central axis of a spherical mirror whose focal length has absolute value $|f| = 40\text{cm}$. The image of object produced by the mirror is of height 25 cm and has the same orientation of the object. One may conclude from the information :
 (1) Image is real, same side of concave mirror.
 (2) Image is virtual, opposite side of concave mirror.
 (3) Image is real, same side of convex mirror.
 (4) Image is virtual, opposite side of convex mirror.
- Q.6** Assume that a tunnel is dug along a chord of the earth, at a perpendicular distance ($R/2$) from the earth's centre, where 'R' is the radius of the Earth. The wall of the tunnel is frictionless. If a particle is released in this tunnel, it will execute a simple harmonic motion with a time period :
 (1) $\frac{2\pi R}{g}$ (2) $\frac{g}{2\pi R}$
 (3) $\frac{1}{2\pi} \sqrt{\frac{g}{R}}$ (4) $2\pi \sqrt{\frac{R}{g}}$
- Q.7** An alternating current is given by the equation $i = i_1 \sin \omega t + i_2 \cos \omega t$. The rms current will be
 (1) $\frac{1}{\sqrt{2}} (i_1^2 + i_2^2)^{\frac{1}{2}}$ (2) $\frac{1}{\sqrt{2}} (i_1 + i_2)^2$
 (3) $\frac{1}{2} (i_1^2 + i_2^2)^{\frac{1}{2}}$ (4) $\frac{1}{\sqrt{2}} (i_1 + i_2)$
- Q.8** The normal density of a material is ρ and its bulk modulus of elasticity is K. The magnitude of increase in density of material, when a pressure P is applied uniformly on all sides, will be :
 (1) $\frac{\rho K}{P}$ (2) $\frac{\rho P}{K}$ (3) $\frac{K}{rP}$ (4) $\frac{PK}{\rho}$
- Q.9** A particle is moving with uniform speed along the circumference of a circle of radius R under the action of a central fictitious force F which is inversely proportional to R^3 . Its time period of revolution will be given by :
 (1) $T \propto R^2$ (2) $T \propto R^{\frac{3}{2}}$
 (3) $T \propto R^{\frac{5}{2}}$ (4) $T \propto R^{\frac{4}{3}}$
- Q.10** A planet revolving in elliptical orbit has :
 (A) a constant velocity of revolution.
 (B) has the least velocity when it is nearest to the sun.
 (C) its areal velocity is directly proportional to its velocity.
 (D) areal velocity is inversely proportional to its velocity.
 (E) to follow a trajectory such that the areal velocity is constant.
 Choose the correct answer from the options given below :
 (1) A only (2) D only
 (3) C only (4) E only
- Q.11** Given below are two statements : one is labelled as Assertion A and the other is labelled as Reason R.
Assertion A : Body 'P' having mass M moving with speed 'u' has head-on collision elastically with another body 'Q' having mass 'm' initially at rest. If $m \ll M$, body 'Q' will have a maximum speed equal to '2u' after collision.
Reason R : During elastic collision, the momentum and kinetic energy are both conserved. In the light of the above statements, choose the most appropriate answer from the options given below :
 (1) A is not correct but R is correct.
 (2) Both A and R are correct but R is NOT the correct explanation of A.
 (3) Both A and R are correct and R is the correct explanation of A.
 (4) A is correct but R is not correct.

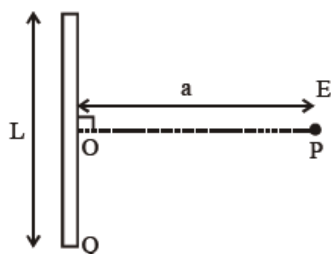
Q.12 Four identical solid spheres each of mass 'm' and radius 'a' are placed with their centres on the four corners of a square of side 'b'. The moment of inertia of the system about one side of square where the axis of rotation is parallel to the plane of the square is :

- (1) $\frac{4}{5}ma^2 + 2mb^2$ (2) $\frac{8}{5}ma^2 + mb^2$
 (3) $\frac{8}{5}ma^2 + 2mb^2$ (4) $\frac{4}{5}ma^2$

Q.13 In a Young's double slit experiment two slits are separated by 2 mm and the screen is placed one meter away. When a light of wavelength 500 nm is used, the fringe separation will be:

- (1) 0.25 mm (2) 0.50 mm
 (3) 0.75 mm (4) 1 mm

Q.14 Find the electric field at point P (as shown in figure) on the perpendicular bisector of a uniformly charged thin wire of length L carrying a charge Q. The distance of the point P from the centre of the rod is $a = \frac{\sqrt{3}}{2} L$.



- (1) $\frac{\sqrt{3}Q}{4\pi\epsilon_0 L^2}$ (2) $\frac{Q}{3\pi\epsilon_0 L^2}$
 (3) $\frac{Q}{2\sqrt{3}\pi\epsilon_0 L^2}$ (4) $\frac{Q}{4\pi\epsilon_0 L^2}$

Q.15 If two similar springs each of spring constant K_1 are joined in series, the new spring constant and time period would be changed by a factor:

- (1) $\frac{1}{2}, \sqrt{2}$ (2) $\frac{1}{4}, \sqrt{2}$
 (3) $\frac{1}{4}, 2\sqrt{2}$ (4) $\frac{1}{2}, 2\sqrt{2}$

Q.16 The temperature θ at the junction of two insulating sheets, having thermal resistances R_1 and R_2 as well as top and bottom temperatures θ_1 and θ_2 (as shown in figure) is given by :



- (1) $\frac{\theta_2 R_2 - \theta_1 R_1}{R_2 - R_1}$ (2) $\frac{\theta_1 R_2 - \theta_2 R_1}{R_2 - R_1}$
 (3) $\frac{\theta_1 R_2 + \theta_2 R_1}{R_1 + R_2}$ (4) $\frac{\theta_1 R_1 + \theta_2 R_2}{R_1 + R_2}$

Q.17 Given below are two statements : one is labelled as Assertion A and the other is labelled as Reason R.

Assertion A : An electron microscope can achieve better resolving power than an optical microscope.

Reason R : The de Broglie's wavelength of the electrons emitted from an electron gun is much less than wavelength of visible light.

In the light of the above statements, choose the correct answer from the options given below:

- (1) A is true but R is false.
 (2) Both A and R are true and R is the correct explanation of A.
 (3) Both A and R are true but R is NOT the correct explanation of A.
 (4) A is false but R is true.

Q.18 LED is constructed from Ga-As-P semiconducting material. The energy gap of this LED is 1.9 eV. Calculate the wavelength of light emitted and its colour.

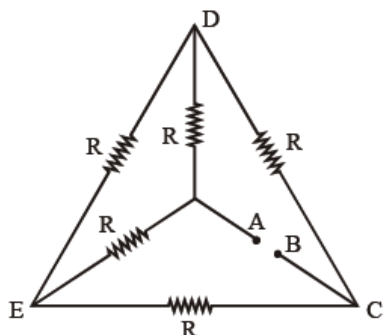
$[h = 6.63 \times 10^{-34} \text{ Js and } c = 3 \times 10^8 \text{ ms}^{-1}]$

- (1) 1046 nm and red colour
 (2) 654 nm and orange colour
 (3) 1046 nm and blue colour
 (4) 654 nm and red colour

Q.19 A large number of water drops, each of radius r, combine to have a drop of radius R. If the surface tension is T and mechanical equivalent of heat is J, the rise in heat energy per unit volume will be:

- (1) $\frac{2T}{j} \left(\frac{1}{r} - \frac{1}{R} \right)$ (2) $\frac{2T}{rJ}$
 (3) $\frac{3T}{rJ}$ (4) $\frac{3T}{J} \left(\frac{1}{r} - \frac{1}{R} \right)$

- Q.20** Five equal resistances are connected in a network as shown in figure. The net resistance between the points A and B is :



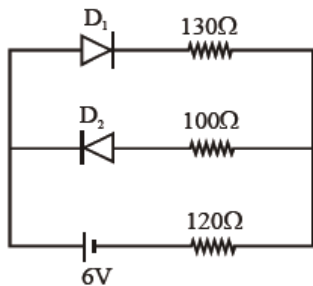
- (1) $2R$ (2) $R/2$
 (3) $3R/2$ (4) R

Section -B

- Q.21** A person standing on a spring balance inside a stationary lift measures 60 kg. The weight of that person if the lift descends with uniform downward acceleration of 1.8 m/s^2 will be N. [$g = 10 \text{ m/s}^2$]

- Q.22** In an electrical circuit, a battery is connected to pass 20 C of charge through it in a certain given time. The potential difference between two plates of the battery is maintained at 15 V. The work done by the battery is _____ J.

- Q.23** The circuit contains two diodes each with a forward resistance of $50 \text{ } \Omega$ and with infinite reverse resistance. If the battery voltage is 6 V, the current through the $120 \text{ } \Omega$ resistance is _____ mA.

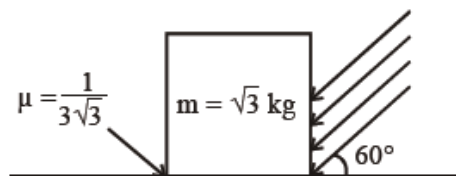


- Q.24** A radiation is emitted by 1000 W bulb and it generates an electric field and magnetic field at P, placed at a distance of 2 m. The efficiency of the bulb is 1.25%. The value of peak electric field at P is $x \times 10^{-1} \text{ V/m}$. Value of x is _____. (Rounded-off to the nearest integer)

[Take $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2\text{N}^{-1} \text{ m}^{-2}$
 $c = 3 \times 10^8 \text{ ms}^{-1}$]

- Q.25** A boy pushes a box of mass 2 kg with a force $\vec{F} = (20\hat{i} + 10\hat{j})\text{N}$ on a frictionless surface. If the box was initially at rest, then _____ m is displacement along the x-axis after 10 s.

- Q.26** As shown in the figure, a block of mass $\sqrt{3} \text{ kg}$ is kept on a horizontal rough surface of coefficient of friction $\frac{1}{3\sqrt{3}}$. The critical force to be applied on the vertical surface as shown at an angle 60° with horizontal such that it does not move, will be $3x$. The value of x will be [$g = 10 \text{ m/s}^2$; $\sin 60^\circ = \frac{\sqrt{3}}{2}$; $\cos 60^\circ = \frac{1}{2}$]



- Q.27** A container is divided into two chambers by a partition. The volume of first chamber is 4.5 litre and second chamber is 5.5 litre. The first chamber contain 3.0 moles of gas at pressure 2.0 atm and second chamber contain 4.0 moles of gas at pressure 3.0 atm. After the partition is removed and the mixture attains equilibrium, then, the common equilibrium pressure existing in the mixture is $x \times 10^{-1} \text{ atm}$. Value of x is ____.

- Q.28** The mass per unit length of a uniform wire is 0.135 g/cm . A transverse wave of the form $y = -0.21 \sin(x + 30t)$ is produced in it, where x is in meter and t is in second. Then, the expected value of tension in the wire is $x \times 10^{-2} \text{ N}$. Value of x is. (Round-off to the nearest integer)

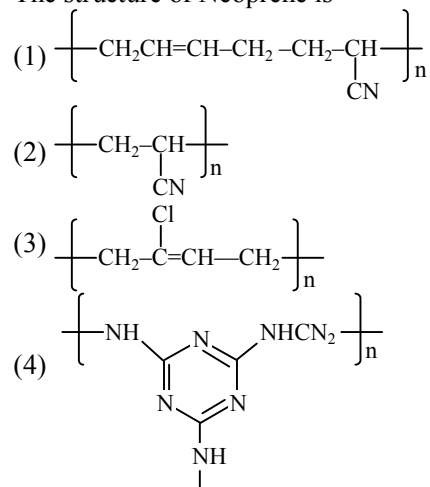
- Q.29** In a series LCR resonant circuit, the quality factor is measured as 100. If the inductance is increased by two fold and resistance is decreased by two fold, then the quality factor after this change will be _____.

- Q.30** The maximum and minimum amplitude of an amplitude modulated wave is 16V and 8V respectively. The modulation index for this amplitude modulated wave is $x \times 10^{-2}$. The value of x is _____.

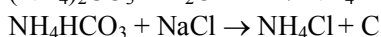
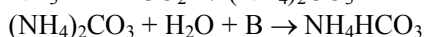
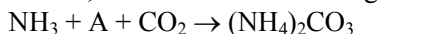
CHEMISTRY

Section -A

Q.31 The structure of Neoprene is -



Q.32 Find A, B and C in the following reactions :



- (1) A - O₂ ; B - CO₂ ; C - Na₂CO₃
 (2) A - H₂O ; B - O₂ ; C - Na₂CO₃
 (3) A - H₂O ; B - O₂ ; C - NaHCO₃
 (4) A - H₂O ; B - CO₂ ; C - NaHCO₃

Q.33 The presence of ozone in troposphere

- (1) Protects us from the UV radiation
 (2) Protects us from the X-ray radiation
 (3) Protects us from greenhouse effect
 (4) generates photochemical smog

Q.34 Match List-I with List-II

| List-I Electronic configuration of elements | List-II Δ_1 in kJ mol ⁻¹ |
|---|---|
| (a) 1s ² 2s ² | (i) 801 |
| (b) 1s ² 2s ² 2p ⁴ | (ii) 899 |
| (c) 1s ² 2s ² 2p ³ | (iii) 1314 |
| (d) 1s ² 2s ² 2p ¹ | (iv) 1402 |

Choose the most appropriate answer from the options given below -

- (1) (a) → (ii), (b) → (iii), (c) → (iv), (d) → (i)
 (2) (a) → (i), (b) → (iv), (c) → (iii), (d) → (ii)
 (3) (a) → (i), (b) → (iii), (c) → (iv), (d) → (ii)
 (4) (a) → (iv), (b) → (i), (c) → (ii), (d) → (iii)

Q.35 Given below are two statements : one is labelled as Assertion A and the other is labelled as Reason R.

Assertion A : Dipole-dipole interactions are the only non-covalent interactions, resulting in hydrogen bond formation.

Reason R : Fluorine is the most electronegative element and hydrogen bonds in HF are symmetrical. In the light of the above statements, choose the most appropriate answer from the options given below.

- (1) A is false but R is true
 (2) Both A and R are true and R is the correct explanation of A
 (3) A is true R is false
 (4) Both A and R are true but R is NOT the correct explanation of A

Q.36 Statements about heavy water are given below.

- A. Heavy water is used in exchange reactions for the study of reaction mechanisms.
 B. Heavy water is prepared by exhaustive electrolysis of water
 C. Heavy water has higher boiling point than ordinary water.
 D. Viscosity of H₂O is greater than D₂O
- (1) A, B and C only
 (2) A and B only
 (3) A and D only
 (4) A and C only

Q.37 The orbital having two radial as well as two angular nodes is -

- (1) 3p (2) 4f (3) 4d (4) 5d

Q.38 Match List -I with List - II

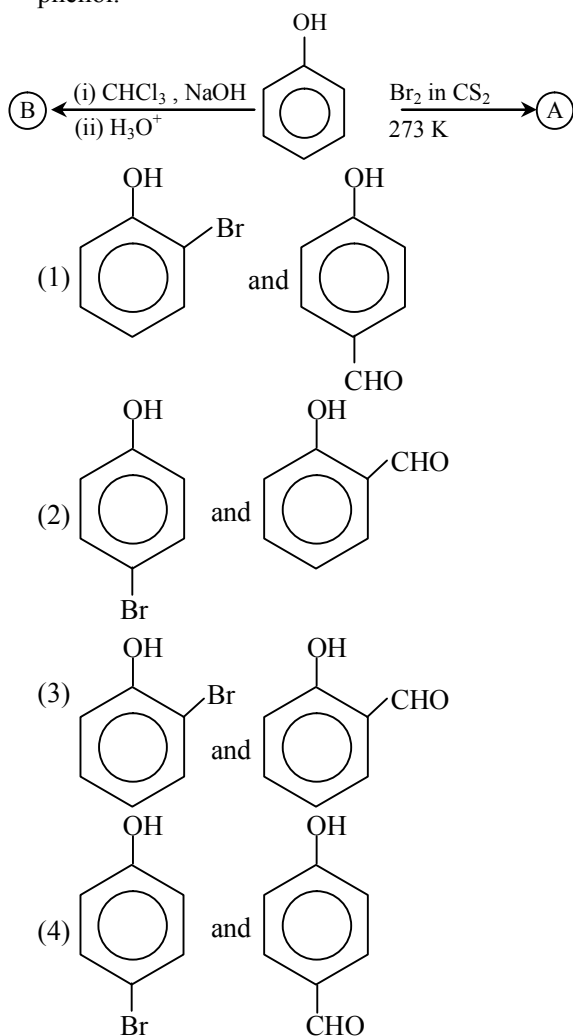
List - I (Ore) **List - II (Element Present)**

- (a) Kernite (i) Tin
 (b) Cassiterite (ii) Boron
 (c) Calamine (iii) Fluorine
 (d) Cryolite (iv) Zinc

Choose the most appropriate answer from the options given below.

- (1) (a) → (i), (b) → (iii), (c) → (iv), (d) → (ii)
 (2) (a) → (ii), (b) → (i), (c) → (iv), (d) → (iii)
 (3) (a) → (ii), (b) → (iv), (c) → (i), (d) → (iii)
 (4) (a) → (iii), (b) → (i), (c) → (ii), (d) → (iv)

Q.39 Identify the major products A and B respectively in the following reactions of phenol.



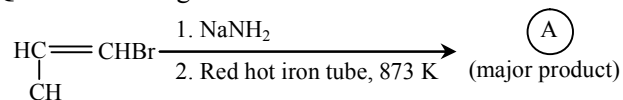
Q.40 Given below are two statements :

Statement I : A mixture of chloroform and aniline can be separated by simple distillation.

Statement II : When separating aniline from a mixture of aniline and water by steam distillation aniline boils below its boiling point. In the light of the above statements, choose the most appropriate answer from the options given below.

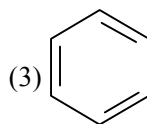
- (1) **Statement-I** is false but **Statement II** is true
- (2) **Both Statement-I** and **Statement II** are false
- (3) **Statement-I** is true but **Statement II** is false
- (4) **Both Statement-I** and **Statement II** are true

Q.41 For the given reaction :



(1) $\text{CH}_3\text{CH}_2\text{CH}_2\text{NH}_2$

(2)



(4)

Q.42 On treating a compound with warm dil. H_2SO_4 , gas X is evolved which turns $\text{K}_2\text{Cr}_2\text{O}_7$ paper acidified with dil. H_2SO_4 to a green compound Y. X and Y respectively are -

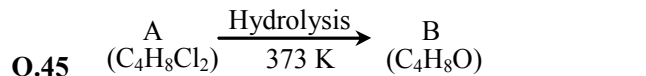
- (1) X = SO_2 , Y = Cr_2O_3
- (2) X = SO_3 , Y = Cr_2O_3
- (3) X = SO_2 , Y = $\text{Cr}_2(\text{SO}_4)_3$
- (4) X = SO_3 , Y = $\text{Cr}_2(\text{SO}_4)_3$

Q.43 Which of the following is 'a' FALSE statement?

- (1) Carius tube is used in the estimation of sulphur in an organic compound
- (2) Carius method is used for the estimation of nitrogen in an organic compound
- (3) Phosphoric acid produced on oxidation of phosphorus present in an organic compound is precipitated as $\text{Mg}_2\text{P}_2\text{O}_7$ by adding magnesia mixture.
- (4) Kjeldahl's method is used for the estimation of nitrogen in an organic compound

Q.44 Which of the following vitamin is helpful in delaying the blood clotting -

- (1) Vitamin C
- (2) Vitamin B
- (3) Vitamin E
- (4) Vitamin K



B reacts with Hydroxyl amine but does not give Tollen's test. Identify A and B

- (1) 1,1-Dichlorobutane and 2-Butanone
- (2) 2,2-Dichlorobutane and Butanal
- (3) 1,1-Dichlorobutane and Butanal
- (4) 2,2-Dichlorobutane and 2-butan-one

Q.46 Compound A used as a strong oxidizing agent is amphoteric in nature. It is the part of lead storage batteries. Compound A is :

- (1) PbO₂
- (2) PbO
- (3) PbSO₄
- (4) Pb₃O₄

Q.47 Which one of the following lanthanoids does not form MO₂? [M is lanthanoid metal]

- (1) Pr
- (2) Dy
- (3) Nd
- (4) Yb

Q.48 Given below are two statements :

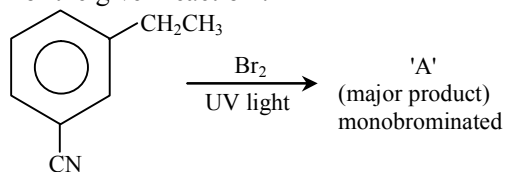
Statement I : o-Nitrophenol is steam volatile due to intramolecular hydrogen bonding.

Statement II : o-Nitrophenol has high melting due to hydrogen bonding.

In the light of the above statements, choose the most appropriate answer from the options given below :

- (1) Statement I is false but Statement II is true
- (2) Both statement I and statement II are true
- (3) Both statement I and statement II are false
- (4) Statement I is true but statement II is false

Q.49 For the given reaction :



- (1)
- (2)
- (3)
- (4)

Q.50 An amine on reaction with benzenesulphonyl chloride produces a compound insoluble in alkaline solution. This amine can be prepared by ammonolysis of ethyl chloride. The correct structure of amine is :

- (1)
- (2) CH₃CH₂NH₂
- (3) CH₃CH₂CH₂NHCH₃
- (4) CH₃CH₂CH₂^HN-CH₂CH₃

Section - B

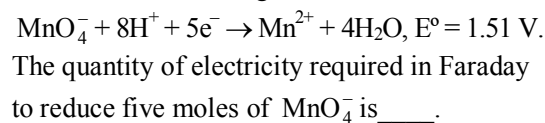
Q.51 For a chemical reaction $A + B \rightleftharpoons C + D$ ($\Delta_r H^\circ = 80 \text{ kJ mol}^{-1}$) the entropy change $\Delta_r S^\circ$ depends on the temperature T (in K) as $\Delta_r S^\circ = 2T \text{ (JK}^{-1} \text{ mol}^{-1}\text{)}$.

Minimum temperature at which it will become spontaneous is _____ K. (Integer)

Q.52 The number of significant figures in 50000.020×10^{-3} is _____.

Q.53 An exothermic reaction $X \rightarrow Y$ has an activation energy 30 kJ mol^{-1} . If energy change ΔE during the reaction is -20 kJ , then the activation energy for the reverse reaction in kJ is _____. (Integer answer)

Q.54 Consider the following reaction



Q.55 A certain gas obeys $P(V_m - b) = RT$. The value of $\left(\frac{\partial Z}{\partial P}\right)_T$ is $\frac{xb}{RT}$. The value of x is _____. (Integer answer) (Z : compressibility factor)

Q.56 A homogeneous ideal gaseous reaction $\text{AB}_{2(g)} \rightleftharpoons \text{A}_{(g)} + 2\text{B}_{(g)}$ is carried out in a 25 litre flask at 27°C. The initial amount of AB_2 was 1 mole and the equilibrium pressure was 1.9 atm. The value of K_p is $x \times 10^{-2}$. The value of x is _____. (Integer answer)

Q.57 Dichromate ion is treated with base, the oxidation number of Cr in the product formed is _____.

Q.58 224 mL of $\text{SO}_2(\text{g})$ at 298 K and 1 atm is passed through 100 mL of 0.1 M NaOH solution. The non-volatile solute produced is dissolved in 36 g of water. The lowering of vapour pressure of solution (assuming the solution is dilute) ($P_{(\text{H}_2\text{O})} = 24 \text{ mm of Hg}$) is $x \times 10^{-2} \text{ mm of Hg}$, the value of x is _____. (Integer answer)

Q.59 3.12 g of oxygen is adsorbed on 1.2 g of platinum metal. The volume of oxygen adsorbed per gram of the adsorbent at 1 atm and 300 K in L is _____.
[$R = 0.0821 \text{ L atm K}^{-1} \text{ mol}^{-1}$]

Q.60 Number of bridging CO ligands in $[\text{Mn}_2(\text{CO})_{10}]$ is _____.

MATHEMATICS

Section - A

Q.61 If \vec{a} and \vec{b} are perpendicular, then $\vec{a} \times (\vec{a} \times (\vec{a} \times (\vec{a} \times \vec{b})))$ is equal to

- (1) $\vec{0}$ (2) $\frac{1}{2}|\vec{a}|^4 \vec{b}$
(3) $\vec{a} \times \vec{b}$ (4) $|\vec{a}|^4 \vec{b}$

Q.62 A fair coin is tossed a fixed number of times. If the probability of getting 7 heads is equal to probability of getting 9 heads, then the probability of getting 2 heads is

- (1) $\frac{15}{2^{13}}$ (2) $\frac{15}{2^{12}}$
(3) $\frac{15}{2^8}$ (4) $\frac{15}{2^{14}}$

Q.63 Let A be a symmetric matrix of order 2 with integer entries. If the sum of the diagonal elements of A^2 is 1, then the possible number of such matrices is

- (1) 4 (2) 1
(3) 6 (4) 12

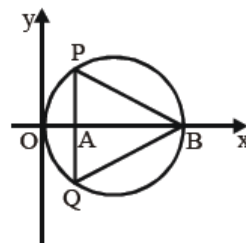
Q.64 In a increasing geometric series, the sum of the second and the sixth term is $\frac{25}{2}$ and the product of the third and fifth term is 25. Then, the sum of 4th, 6th and 8th terms is equal to

- (1) 30 (2) 26
(3) 35 (4) 32

Q.65 The value of $\sum_{n=1}^{100} \int_{n-1}^n e^{x-[x]} dx$, where $[x]$ is the greatest integer $\leq x$, is

- (1) $100(e-1)$ (2) $100(1-e)$
(3) $100e$ (4) $100(1+e)$

Q.66 In the circle given below, let $OA = 1$ unit, $OB = 13$ unit and $PQ \perp OB$. Then, the area of the triangle PQB (in square units) is



- (1) $24\sqrt{2}$ (2) $24\sqrt{3}$
(3) $26\sqrt{3}$ (4) $26\sqrt{2}$

Q.67 The sum of the infinite series

- $1 + \frac{2}{3} + \frac{7}{3^2} + \frac{12}{3^3} + \frac{17}{3^4} + \frac{22}{3^5} + \dots$ is equal to
(1) $\frac{13}{4}$ (2) $\frac{9}{4}$
(3) $\frac{15}{4}$ (4) $\frac{11}{4}$

Q.68 The value of

- $\lim_{h \rightarrow 0} 2 \left\{ \frac{\sqrt{3} \sin\left(\frac{\pi}{6} + h\right) - \cos\left(\frac{\pi}{6} + h\right)}{\sqrt{3}h(\sqrt{3} \cosh - \sinh)} \right\}$ is
(1) $\frac{4}{3}$ (2) $\frac{2}{\sqrt{3}}$ (3) $\frac{3}{4}$ (4) $\frac{2}{3}$

Q.69 The maximum value of the term independent of

- 't' in the expansion of $\left(tx^{\frac{1}{5}} + \frac{(1-x)^{\frac{1}{10}}}{t} \right)^{10}$ where

$x \in (0, 1)$ is

- (1) $\frac{10!}{\sqrt{3}(5!)^2}$ (2) $\frac{2 \cdot 10!}{3\sqrt{3}(5!)^2}$
(3) $\frac{2 \cdot 10!}{3(5!)^2}$ (4) $\frac{10!}{3(5!)^2}$

Q.70 The rate of growth of bacteria in a culture is proportional to the number of bacteria present and the bacteria count is 1000 at initial time $t = 0$. The number of bacteria is increased by 20% in 2 hours. If the population of bacteria is 2000 after $\frac{k}{\log_e \left(\frac{6}{5}\right)}$ hours, then $\left(\frac{k}{\log_e 2}\right)^2$ is

- equal to
 (1) 4 (2) 8
 (3) 2 (4) 16

Q.71 If $(1, 5, 35)$, $(7, 5, 5)$, $(1, \lambda, 7)$ and $(2\lambda, 1, 2)$ are coplanar, then the sum of all possible values of λ is

- (1) $\frac{39}{5}$ (2) $-\frac{39}{5}$ (3) $\frac{44}{5}$ (4) $-\frac{44}{5}$

Q.72 If $\frac{\sin^{-1} x}{a} = \frac{\cos^{-1} x}{b} = \frac{\tan^{-1} y}{c}$; $0 < x < 1$. then the value of $\cos\left(\frac{\pi c}{a+b}\right)$ is

- (1) $\frac{1-y^2}{y\sqrt{y}}$ (2) $1-y^2$
 (3) $\frac{1-y^2}{1+y^2}$ (4) $\frac{1-y^2}{2y}$

Q.73 The number of seven digit integers with sum of the digits equal to 10 and formed by using the digits 1,2 and 3 only is

- (1) 42 (2) 82
 (3) 77 (4) 35

Q.74 Let f be any function defined on \mathbb{R} and let it satisfy the condition :

$$|f(x) - f(y)| \leq |(x - y)^2|, \forall (x, y) \in \mathbb{R}$$

If $f(0) = 1$, then :

- (1) $f(x)$ can take any value in \mathbb{R}
 (2) $f(x) < 0, \forall x \in \mathbb{R}$
 (3) $f(x) = 0, \forall x \in \mathbb{R}$
 (4) $f(x) > 0, \forall x \in \mathbb{R}$

Q.75 The maximum slope of the curve $y = \frac{1}{2}x^4 - 5x^3 + 18x^2 - 19x$ occurs at the point

- (1) (2, 2) (2) (0, 0)
 (3) (2, 9) (4) $\left(3, \frac{21}{2}\right)$

Q.76 The intersection of three lines $x - y = 0$, $x + 2y = 3$ and $2x + y = 6$ is a
 (1) Right angled triangle
 (2) Equilateral triangle
 (3) Isosceles triangle
 (4) None of the above

Q.77 Consider the three planes
 $P_1 : 3x + 15y + 21z = 9$,
 $P_2 : x - 3y - z = 5$, and
 $P_3 : 2x + 10y + 14z = 5$
 Then, which one of the following is true ?
 (1) P_1 and P_2 are parallel
 (2) P_1 and P_3 are parallel
 (3) P_2 and P_3 are parallel
 (4) P_1, P_2 and P_3 all are parallel

Q.78 The value of $\begin{vmatrix} (a+1) & (a+2) & a+2 & 1 \\ (a+2) & (a+3) & a+3 & 1 \\ (a+3) & (a+4) & a+4 & 1 \end{vmatrix}$ is
 (1) $(a+2)(a+3)(a+4)$
 (2) -2
 (3) $(a+1)(a+2)(a+3)$
 (4) 0

Q.79 The value of $\int_{-\pi/2}^{\pi/2} \frac{\cos^2 x}{1+3^x} dx$ is
 (1) $\frac{\pi}{4}$ (2) 4π (3) $\frac{\pi}{2}$ (4) 2π

Q.80 Let $R = \{(P, Q) \mid P \text{ and } Q \text{ are at the same distance from the origin}\}$ be a relation, then the equivalence class of $(1, -1)$ is the set :

- (1) $S = \{(x, y) \mid x^2 + y^2 = 4\}$
 (2) $S = \{(x, y) \mid x^2 + y^2 = 1\}$
 (3) $S = \{(x, y) \mid x^2 + y^2 = \sqrt{2}\}$
 (4) $S = \{(x, y) \mid x^2 + y^2 = 2\}$

Section - B

Q.81 The difference between degree and order of a differential equation that represents the family of curves given by $y^2 = a \left(x + \frac{\sqrt{a}}{2}\right)$, $a > 0$ is

Q.82 The number of integral values of 'k' for which the equation $3\sin x + 4 \cos x = k + 1$ has a solution, $k \in \mathbb{R}$ is

Q.83 The number of solutions of the equation $\log_4(x - 1) = \log_2(x - 3)$ is

- Q.84** The sum of 162^{th} power of the roots of the equation $x^3 - 2x^2 + 2x - 1 = 0$ is
- Q.85** Let $m, n \in \mathbb{N}$ and $\gcd(2, n) = 1$. If
- $$30 \binom{30}{0} + 29 \binom{30}{1} + \dots + 2 \binom{30}{28} + 1 \binom{30}{29} = n \cdot 2^m,$$
- then $n + m$ is equal to (Here $\binom{n}{k} = {}^n C_k$)
- Q.86** If $y = y(x)$ is the solution of the equation $e^{\sin y} \cos y \frac{dy}{dx} + e^{\sin y} \cos x = \cos x$, $y(0) = 0$:
- then $1 + y\left(\frac{\pi}{6}\right) + \frac{\sqrt{3}}{2} y\left(\frac{\pi}{3}\right) + \frac{1}{\sqrt{2}} y\left(\frac{\pi}{4}\right)$ is equal to
- Q.87** Let $(\lambda, 2, 1)$ be a point on the plane which passes through the point $(4, -2, 2)$. If the plane is perpendicular to the line joining the points $(-2, -21, 29)$ and $(-1, -16, 23)$, then $\left(\frac{\lambda}{11}\right)^2 - \frac{4\lambda}{11} - 4$ is equal to
- Q.88** The area bounded by the lines $y = |x - 1| - 2$ is
- Q.89** The value of the integral $\int_0^{\pi} |\sin 2x| dx$ is
- Q.90** If $\sqrt{3}(\cos^2 x) = (\sqrt{3} - 1)\cos x + 1$, the number of solutions of the given equation when $x \in \left[0, \frac{\pi}{2}\right]$ is.

JEE MAIN ONLINE PAPER 2021

Held on February 26, 2021 (Morning)

Hints & Solutions

PHYSICS

1.[4] Gravitational field of ring

$$= - \frac{Gmx}{(R^2 + x^2)^{3/2}}$$

Force between sphere & ring

$$\frac{GmM(\sqrt{8R})}{(R^2 + 8R^2)^{3/2}}$$

$$= \frac{GmM}{R^2} \times \frac{\sqrt{8}}{27}$$

Ans. (4)

2.[Bonus] * Official Ans. by NTA is (2)

When connected in parallel

$$C_{eq} = C_1 + C_2$$

When in series

$$C'_{eq} = \frac{C_1 C_2}{C_1 + C_2}$$

$$C_1 + C_2 = \frac{15}{4} \left(\frac{C_1 C_2}{C_1 + C_2} \right)$$

$$4(C_1 + C_2)^2 = 15 C_1 C_2 = 0$$

$$4C_1^2 + 4C_2^2 - 7C_1 C_2 = 0$$

dividing by C_1^2

$$4 \left(\frac{C_2}{C_1} \right)^2 - \frac{7C_2}{C_1} + 4 = 0$$

$$\text{Let } \frac{C_2}{C_1} = x$$

$$4x^2 - 7x + 4 = 0$$

$$b^2 - 4ac = 49 - 64 < 0$$

No solution exists

3.[2] kT has dimension of energy

$$\frac{\beta x^2}{kT} \text{ is dimensionless}$$

$$[\beta] [L^2] = [ML^2 T^{-2}]$$

$$[\beta] = [MT^{-2}]$$

$\alpha^2 \beta$ has dimension of work

$$[\alpha^2] [MT^{-2}] = [ML^2 T^{-2}]$$

$$[\alpha] = [M^0 L^0 T^0]$$

4.[3] $\frac{1}{\lambda_1} = R \left[\frac{1}{1^2} - \frac{1}{4^2} \right]$

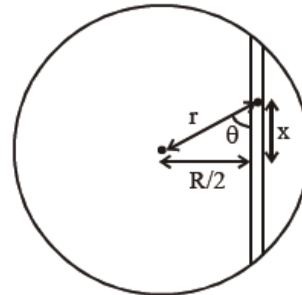
$$\frac{1}{\lambda_2} = R \left[\frac{1}{3^2} - \frac{1}{4^2} \right]$$

$$\frac{\lambda_1}{\lambda_2} = \frac{\left[\frac{1}{9} - \frac{1}{16} \right]}{\left[1 - \frac{1}{16} \right]} = \frac{7}{9 \times 15}$$

$$\frac{\lambda_1}{\lambda_2} = \frac{7}{135}$$

5.[4] Since orientation is same image is virtual Since image is smaller the mirror has to be convex

6.[4]



Force along the tunnel

$$F = - \left(\frac{GMmr}{R^3} \right) \cos \theta$$

$$F = - \frac{gm}{R} \times \left(\frac{GM}{R^2} = g, r \cos \theta = x \right)$$

$$a = - \frac{g}{R} x$$

$$\omega^2 = \frac{g}{R} \quad T = 2\pi \sqrt{\frac{R}{g}}$$

7.[1] $i = i_1 \sin \omega t + i_2 \sin (\omega t + 90^\circ)$

$$i = \sqrt{i_1^2 + i_2^2} \sin (\omega t + \phi)$$

$$i_{rms} = \frac{i_0}{\sqrt{2}} = \frac{\sqrt{i_1^2 + i_2^2}}{\sqrt{2}}$$

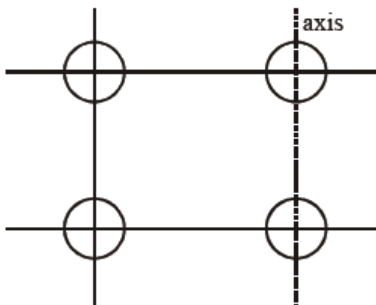
8.[2] $\rho = \frac{M}{V}$
 $\frac{d\rho}{\rho} = -\frac{dV}{V}$
 $k = -\frac{P}{\frac{dV}{V}} = \frac{P}{k}$
 $\frac{d\rho}{\rho} = \frac{P}{k} \Rightarrow d\rho = \frac{\rho P}{k}$

9.[1] $F \propto \frac{1}{R^3}$
 $\frac{K}{R^3} = m\omega^2 R$
 $\omega^2 = \frac{K}{m} \times \frac{1}{R^4}$
 $\left(\frac{2\pi}{T}\right)^2 = \frac{K}{m} \times \frac{1}{R^4}$
 $T^2 \propto R^4$
 $T \propto R^2$

10.[4] As per Kepler's 2nd law, Areal velocity is constant.

11.[3] For $e = 1$ & second body at rest
 $V_2 = \frac{2m_1 u_1}{m_1 + m_2} = \frac{2u(M)}{M + m} \approx 2u$
 Since $M \gg m$

12.[3]



$$I = 2 \times \left(\frac{2}{5} ma^2\right) + 2 \times \left(\frac{2}{5} ma^2 + mb^2\right)$$

$$I = \frac{8}{5} ma^2 + 2mb^2$$

13.[1] $\beta = \frac{\lambda D}{d} = \frac{500 \times 10^{-9} \times 1}{2 \times 10^{-3}}$
 $\beta = \frac{5}{2} \times 10^{-4} \text{ m} = 2.5 \times 10^{-1} \text{ mm}$
 $b = 0.25 \text{ mm}$

14.[3] $E = \frac{k\lambda}{a} (\sin \theta_1 + \sin \theta_2)$
 $E = \frac{1}{4\pi\epsilon_0} \times \frac{Q}{L} \times \frac{1}{\left(\frac{\sqrt{3}L}{2}\right)} \times (2 \sin \theta)$
 $\tan \theta = \frac{L/2}{\frac{\sqrt{3}L}{2}} = \frac{1}{\sqrt{3}}$
 $\sin \theta = \frac{1}{2}$
 $E = \frac{1}{4\pi\epsilon_0} \times \frac{2Q}{\sqrt{3}L^2} \times \left(2 \times \frac{1}{2}\right)$
 $E = \frac{Q}{2\sqrt{3}\pi\epsilon_0 L^2}$

15.[1] $\frac{1}{k_{eq}} = \frac{1}{k_1} + \frac{1}{k_2}$
 $\frac{1}{k_{eq}} = \frac{1}{k} + \frac{1}{k} \Rightarrow k_{eq} = \frac{k}{2}$
 $k' = \frac{k}{2}$
 $T = 2\pi \sqrt{\frac{M}{k}} \quad T' = 2\pi \sqrt{\frac{M}{k'}}$
 $\Rightarrow T' = 2\pi \sqrt{\frac{M}{k}} \times \sqrt{2}$
 $T' = \sqrt{2}T$

16.[3]



Heat flow rate will be same through both
 $\therefore \frac{\theta_1 - \theta}{R_1} = \frac{\theta - \theta_2}{R_2}$
 $R_2\theta_1 - R_2\theta = R_1\theta - R_1\theta_2$
 $\theta = \frac{R_2\theta_1 + R_1\theta_2}{R_1 + R_2}$

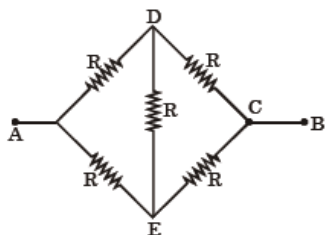
17.[2] Resolving power $\propto \frac{1}{\lambda}$

Since wavelength of electron is much less than visible light, its resolving power will be much more

18.[4] $\lambda = \frac{hc}{E} = \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{1.9 \times 1.6 \times 10^{-19}} = 6.54 \times 10^{-7}$
 = 654 nm
 Red color

19.[4] $n \times \frac{4}{3} \pi r^3 = \frac{4}{3} \pi R^3$
 $\therefore n^{1/3} r = R$
 \therefore total change in surface energy
 = $(n(4\pi r^2) - 4\pi R^2) T$
 $\Rightarrow 4\pi T (nr^2 - R^2)$
 \therefore Heat energy
 = $\frac{4\pi T(nr^2 - R^2)}{J \times \frac{4}{3} \pi R^3} = \frac{3T}{J} \left(\frac{nr^2}{R^3} - \frac{1}{R} \right)$
 Put $nr^3 = R^3$
 $\therefore \frac{3T}{J} \left(\frac{1}{r} - \frac{1}{R} \right)$

20.[4] This diagram can be drawn like



It is a wheat stone bridge

$\therefore R_{eq} = \frac{2R \times 2R}{2R + 2R} \Rightarrow R$

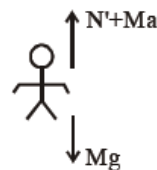
21.[492]



When lift is at rest

$N = mg$
 $\Rightarrow 60 \times 10 = 600 \text{ N}$

When lift moves with downward acceleration
 In frame of lift pseudo force will be in upward direction



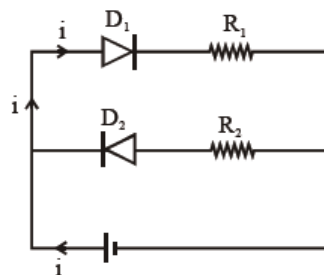
$N' = M(g - a)$
 $\Rightarrow 60(10 - 1.8)$
 $N' \Rightarrow 492 \text{ N}$

22.[300] Work done by battery = $Q(\Delta V)$

$\Rightarrow 20 \times 15 = 300 \text{ J}$

Ans. 300

23.[20]



In this circuit D_1 will be forward bias and D_2 will be reverse bias.

\therefore There will be no current through D_2 and R_2

Apply KVL in circuit we get

$+6 - 50i - 130i - 120i = 0$
 $= \frac{6}{300} \text{ A} = \frac{6}{300} \times 1000 \text{ mA}$
 $\Rightarrow 20 \text{ mA}$

24.[137] $I_{avg} = \frac{1}{2} \epsilon_0 E_0^2 C$

$\frac{1.25}{100} \times \frac{1000}{4\pi(2)^2} = \frac{1}{2} 8.85 \times 10^{-12} \times 3$

$\times 10^8 \times E_0^2$

$E_0^2 = 187.4$

$\therefore E_0 = 13.689 \text{ V/m}$

$= 136.89 \times 10^{-1} \text{ V/m}$

$\therefore x = 136.89$

Rounding off to nearest integer

$x = 137$

25.[500] $\vec{F} = (20\hat{i} + 10\hat{j})\text{N}$

$$\vec{a} = \frac{\vec{F}}{m} = \frac{20\hat{i} + 10\hat{j}}{2} \Rightarrow 10\hat{i} + 5\hat{j}$$

$$\therefore \vec{s} = \frac{1}{2} \vec{a}t^2 = \frac{1}{2}(10\hat{i} + 5\hat{j}) \times (10)^2$$

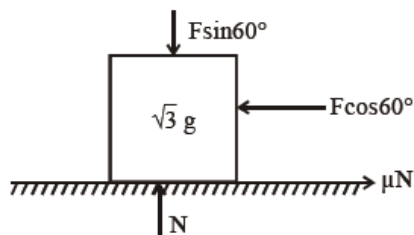
$$\Rightarrow 50(10\hat{i} + 5\hat{j})\text{m}$$

\therefore Displacement along x-axis

$$\Rightarrow 50 \times 10 \Rightarrow 500\text{ m}$$

\therefore Ans. 500

26.[3.33]



$$F \cos 60^\circ = \mu N \text{ or } \frac{F}{2} = \frac{1}{3\sqrt{3}} N \quad \dots(1)$$

$$\& N = \sin 60^\circ + \sqrt{3}g \dots (2)$$

From equation (1) & (2)

$$\frac{F}{2} = \frac{1}{3\sqrt{3}} \left(\frac{F\sqrt{3}}{2} + \sqrt{3}g \right)$$

$$\Rightarrow F = g = 10 \text{ Newton} = 3x$$

$$\text{So } x \frac{10}{3} = 3.33$$

27.[25] Let common equilibrium pressure of mixture is P atmp. then

$$U_1 + U_2 = U_{\text{mixture}}$$

$$\frac{f}{2} P_1 V_1 + \frac{f}{2} P_2 V_2 = \frac{f}{2} P (V_1 + V_2)$$

$$\frac{f}{2} (2)(4.5) + \frac{f}{2} (3)(5.5) = \frac{f}{2} p (4.5 + 5.5)$$

$$\Rightarrow P = 2.55 = x \times 10^{-1} \text{ atmp}$$

$$\text{So } x = 25.5 \approx 26 \text{ (Nearest integer)}$$

28.[12] $\mu = 0.135 \text{ gm/cm} = 0.0135 \text{ kg/m}$

$$y = -0.21 \sin(x + 30t)$$

(x in meter & t in sec)

$$v = \frac{\omega}{k} = \frac{30}{1} = 30 \text{ m/s}$$

$$v = \sqrt{\frac{T}{\mu}} \Rightarrow T = v^2 \mu = (30)^2 (0.0135)$$

$$= 12.15$$

$$= x \times 10^{-2} \text{ N}$$

$$\Rightarrow x = 1215$$

29.[282.84]

$$Q = \frac{X_L}{R} = \frac{\omega L}{R} = \frac{1}{\sqrt{LC}} \frac{L}{R} = \frac{\sqrt{L}}{R\sqrt{C}}$$

$$Q' = \frac{\sqrt{2L}}{\left(\frac{R}{2}\right)\sqrt{C}} = 2\sqrt{2}Q = 2\sqrt{2} (100)$$

$$= 282.84$$

30.[33] Modulation index = $\frac{A_{\text{max}} - A_{\text{min}}}{A_{\text{max}} + A_{\text{min}}}$

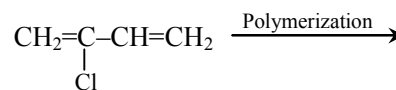
$$= \frac{16 - 8}{16 + 8} = \frac{8}{24} = \frac{1}{3} = 0.33$$

$$x \times 10^{-2} = 0.33$$

$$x = 33$$

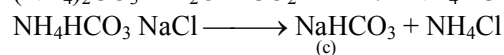
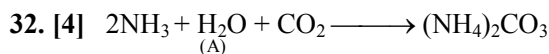
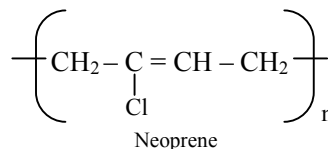
CHEMISTRY

31. [3]

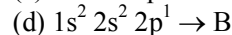
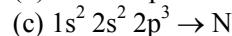
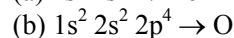
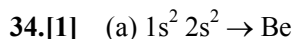


Chloroprene

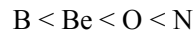
2 Chloro-1, 3-Butadiene



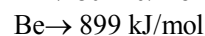
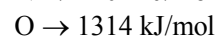
33.[4] The presence of ozone in troposphere generates photochemical smog.



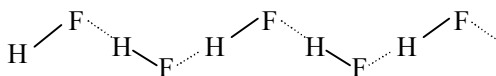
The ionization enthalpy order is



Be has more IE compared to B due to extra stability & N has more IE compared to oxygen due to extra stability



- 35.[1] Assertion is incorrect since in hydrogen bonding, Dipole-dipole interactions are noncovalent but ion-dipole interaction can also result in H-bond formation. Reason is correct since F is most electronegative element & structure is



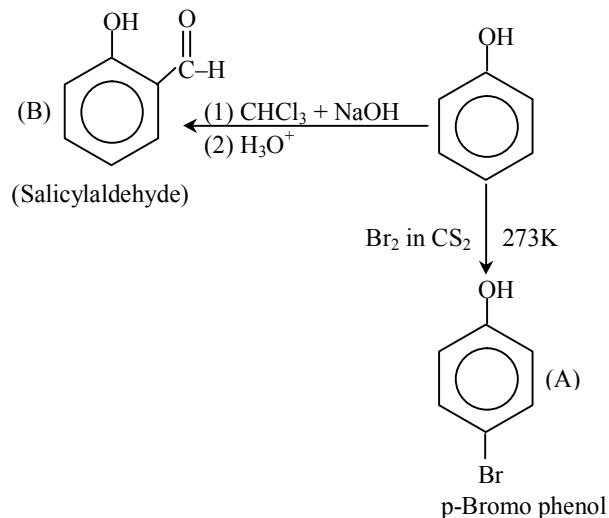
Symmetrical H-bonds are present

- 36.[1] Heavy water is used in exchange reactions for study of reaction mechanisms
Heavy water is prepared by exhaustive electrolysis of water.
B.P. of $D_2O = 374.4\text{ K}$
B.P. of $H_2O = 373\text{ K}$
Viscosity of $H_2O = 0.89$ centipoise
Viscosity of $D_2O = 1.107$ centipoise

- 37.[4] $n - l - 1 = 2$
 $l = 2$
 $n - 2 - 1 = 2$
 $n = 5$

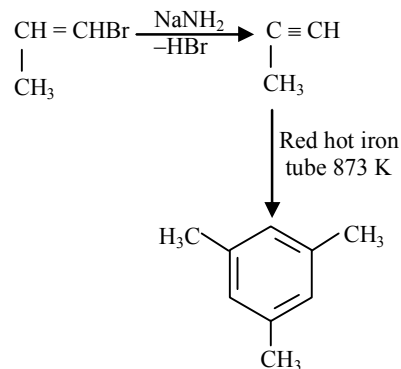
- 38.[2] Kernite = $Na_2B_4O_7 \cdot 4H_2O$
Cassiterite = SnO_2
Calamine = $ZnCO_3$
Cryolite = Na_3AlF_6

- 39.[2]



- 40.[4] **Statement 1 :** B.P. of chloroform = 334 K
B.P. of aniline = 457 K
thus can be separated of simple distillation.
Statement 2 : Mixture of aniline and water separated by simple distillation.

- 41.[4]

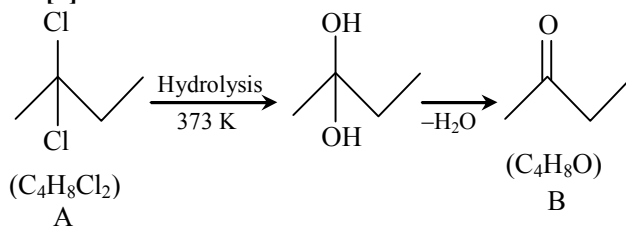


- 42.[3] $SO_2 + \text{dil } H_2SO_4 \longrightarrow SO_3(g)$
 $SO_2 + K_2Cr_2O_7 \xrightarrow[H_2SO_4]{\text{dil.}} Cr_2(SO_4)_3$

- 43.[2] Carius method is used in the estimation of halogen in organic compounds.

- 44.[4] Vitamin helpful in delaying the blood clotting is Vitamin K

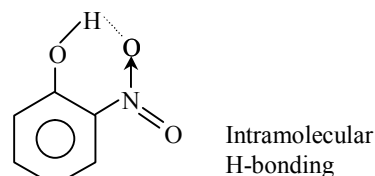
- 45.[4]



- 46.[1] PbO_2 is amphoteric and strong oxidizing agent and also a component of lead storage batteries.

- 47.[4] Yb is the only element that do not form MO_2 type oxide

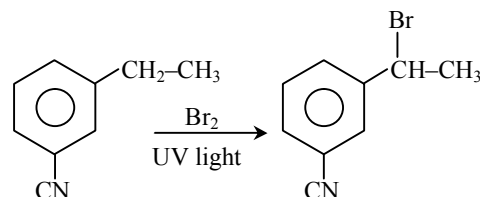
- 48.[4]



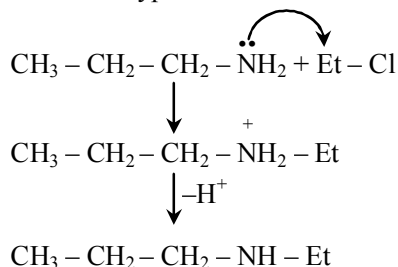
thus it is more volatile due to intramolecular H-bonding.

Melting point depends on packing efficiency not on H-bonding thus statement II is false

- 49.[3]

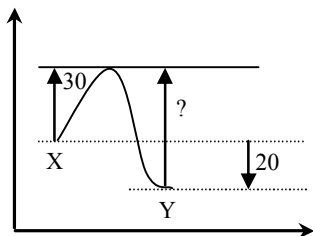
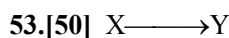


50.[4] It has to be 2° amine because on reaction with benzene sulphonylchloride it gives water in soluble product. As it is formed by ammonolysis of ethylchloride, so it has to be R-NH-Et type.



51.[200] $\Delta G^0 = \Delta H^0 - T \times \Delta S^0$
 $\Delta G^0 = \Delta H^0 - T \times (2T)$
 $T = 200\text{K}$

52.[7] 50000.020×10^{-3}



54.[25]

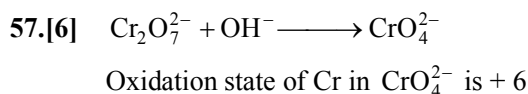
55.[1] $Z = 1 + \frac{Pb}{RT}$
 $\left(\frac{\partial Z}{\partial P}\right)_T = 0 + \frac{b}{RT} \times 1$

56.[72 to 75]

Official Ans. by NTA (74)

$$\begin{array}{rcl}
 \text{AB}_2 & = & \text{A} + 2\text{B} \\
 1 & - & - \\
 1-\alpha & \alpha & 2\alpha \\
 = 0.535 & 0.465 & 0.93 \\
 1.9 \times 25 = n_T \times 0.08206 \times 300 \\
 n_T = 1.93 = 1 + 2\alpha \\
 \alpha = 0.465
 \end{array}$$

$$K_p = \frac{\left(\frac{0.465}{1.93} \times 19\right) \left(\frac{0.93}{1.93} \times 1.9\right)^2}{\left(\frac{0.535}{1.93} \times 1.9\right)}$$



58.[18 to 24]

Official Ans. by NTA (12)

Case-I :

$$\begin{array}{ccc}
 \text{SO}_2 & + & 2\text{NaOH} \longrightarrow \text{NaSO}_3 + \text{H}_2\text{O} \\
 \frac{224}{0.0821 \times 2.98} & 10 \text{ mmol} & 5 \text{ mmol} \\
 = 9.2 \text{ m mol (L.R.)} & & (i = 3) \\
 P^S = P^0 \cdot X_{\text{solvent}} \\
 = 24 \times \frac{2}{(2 + 15 \times 10^{-3})} \\
 = 23.82
 \end{array}$$

$$\Delta P = 0.18 \text{ torr} = 1.8 \times 10^{-2} \text{ torr}$$

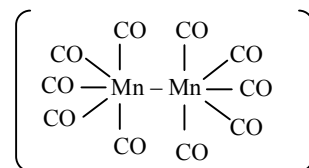
Case-II :

$$\begin{array}{ccc}
 \text{SO}_2 & + & \text{NaOH} \longrightarrow \text{NaHSO}_3 \\
 9.2 & 10 & - \\
 - & 0.8 & 9.2 \\
 \Delta P = P^0 \cdot X_{\text{solute}} \\
 = 24 \times \frac{(1.6 + 18.4)}{2020} \\
 = 0.2376 = 23.76 \times 10^{-2}
 \end{array}$$

59.[2]

$$\begin{array}{l}
 V = \frac{3.12}{32} \times 0.0821 \times 300 \\
 = 2.40 \text{ l} \\
 \therefore 1.2 \text{ gm adsorbs } 2.40 \text{ l} \\
 \therefore 1 \text{ gm adsorbs } 2 \text{ l}
 \end{array}$$

60.[0] $\text{Mn}_2(\text{CO})_{10}$ structure is



Zero bridging CO ligands are present

MATHEMATICS

61.[4] $\vec{a} \cdot \vec{b} = 0$
 $\vec{a} \times (\vec{a} \times \vec{b}) = (\vec{a} \cdot \vec{b})\vec{a} - (\vec{a} \cdot \vec{a})\vec{b} = -|\vec{a}|^2 \vec{b}$
 Now $\vec{a} \times (\vec{a} \times (-|\vec{a}|^2 \vec{b}))$
 $= -|\vec{a}|^2 (\vec{a} \times (\vec{a} \times \vec{b}))$
 $= -|\vec{a}|^2 (-|\vec{a}|^2 \vec{b}) = |\vec{a}|^4 \vec{b}$

62.[1] Let the coin be tossed n-times
 $P(H) = P(T) = \frac{1}{2}$
 $P(7 \text{ heads}) = {}^n C_7 \left(\frac{1}{2}\right)^{n-7} \left(\frac{1}{2}\right)^7 = \frac{{}^n C_7}{2^n}$
 $P(9 \text{ heads}) = {}^n C_9 \left(\frac{1}{2}\right)^{n-9} \left(\frac{1}{2}\right)^9 = \frac{{}^n C_9}{2^n}$
 $P(7 \text{ heads}) = P(9 \text{ heads})$
 ${}^n C_7 = {}^n C_9 \Rightarrow n = 16$
 $P(2 \text{ heads}) = {}^{16} C_2 \left(\frac{1}{2}\right)^{14} \left(\frac{1}{2}\right)^2 = \frac{15 \times 8}{2^{16}}$
 $P(2 \text{ heads}) = \frac{15}{2^{13}}$

63.[1] $A = \begin{pmatrix} a & b \\ b & c \end{pmatrix}$, $a, b, c \in I$
 $A^2 = \begin{pmatrix} a & b \\ b & c \end{pmatrix} \begin{pmatrix} a & b \\ b & c \end{pmatrix} = \begin{pmatrix} a^2 + b^2 & b(a+c) \\ b(a+c) & b^2 + c^2 \end{pmatrix}$
 Sum of the diagonal entries of
 $A^2 = a^2 + 2b^2 + c^2$
 Given $a^2 + 2b^2 + c^2 = 1$, $a, b, c, \in I$
 $b = 0$ & $a^2 + c^2 = 1$
Case-1 : $a = 0 \Rightarrow c = \pm 1$ (2-matrices)
Case-2 : $c = 0 \Rightarrow a = \pm 1$ (2-matrices)
 Total = 4 matrices

64.[3] a, ar, ar^2, \dots
 $T_2 + T_6 = \frac{25}{2} \Rightarrow ar(1 + r^4) = \frac{25}{2}$
 $a^2 r^2 (1 + r^4)^2 = \frac{625}{4} \dots(1)$
 $T_3 \cdot T_5 = 25 \Rightarrow (ar^2)(ar^4) = 25$
 $a^2 r^6 = 25 \dots(2)$
 On dividing (1) by (2)
 $\frac{(1+r^4)^2}{r^4} = \frac{25}{4}$

$$4r^8 - 17r^4 + 4 = 0$$

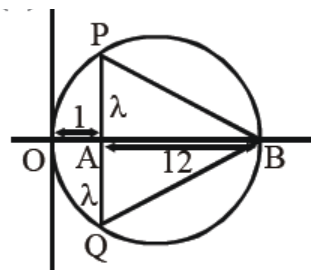
$$(4r^4 - 1)(r^4 - 4) = 0$$

$$r^4 = \frac{1}{4}, 4 \Rightarrow r^4 = 4$$

(an increasing geometric series)
 $a^2 r^6 = 25 \Rightarrow (ar^3)^2 = 25$
 $T_4 + T_6 + T_8 = ar^3 + ar^5 + ar^7$
 $= ar^3 (1 + r^2 + r^4)$
 $= 5(1 + 2 + 4) = 35$

65.[1] $\sum_{n=1}^{100} \int_{n-1}^n e^{\{x\}} dx$, period of $\{x\} = 1$
 $\sum_{n=1}^{100} \int_0^1 e^{\{x\}} dx = \sum_{n=1}^{100} \int_0^1 e^x dx$
 $\sum_{n=1}^{100} (e - 1) = 100(e - 1)$

66.[2]



$PA = AQ = \lambda$
 $OA \cdot AB$
 $= AP \cdot AQ$
 $\Rightarrow 1 \cdot 12 = \lambda \cdot \lambda$
 $\Rightarrow \lambda = 2\sqrt{3}$
 $\text{Area } \Delta PQB = \frac{1}{2} \times 2\lambda \times AB$
 $\Delta = \frac{1}{2} \cdot 4\sqrt{3} \times 12$
 $= 24\sqrt{3}$

67.[1] $S = 1 + \frac{2}{3} + \frac{7}{3^2} + \frac{12}{3^3} + \frac{17}{3^4} + \dots$
 $\frac{S}{3} = \frac{1}{3} + \frac{2}{3^2} + \frac{7}{3^3} + \frac{12}{3^4} + \dots$
 $\frac{2S}{3} = 1 + \frac{1}{3} + \frac{5}{3^2} + \frac{5}{3^3} + \frac{5}{3^4} + \dots + \text{up to infinite terms}$
 $\Rightarrow S = \frac{13}{4}$

68.[1]

$$L = \lim_{h \rightarrow 0} 2 \left(\frac{\sqrt{3} \left(\frac{1}{2} \cosh + \frac{\sqrt{3}}{2} \sinh \right) - \left(\frac{\sqrt{3}}{2} \cosh - \frac{\sinh}{2} \right)}{(\sqrt{3}h)(\sqrt{3})} \right)$$

$$L = \lim_{h \rightarrow 0} \frac{4 \sinh}{3h} \Rightarrow L = \frac{4}{3}$$

69.[2] Term independent of t will be the middle term due to exact same magnitude but opposite sign powers of t in the binomial expression given

$$\text{so } T_6 = {}^{10}C_5 (tx^2)^5 \left(\frac{1}{t} \right)^5$$

$$T_6 = f(x) = {}^{10}C_5 (x\sqrt{1-x}) ; \text{ for maximum}$$

$$f'(x) = 0 \Rightarrow x = \frac{2}{3} \text{ \& } f''\left(\frac{2}{3}\right) < 0$$

$$\text{So } f(x)_{\max} = {}^{10}C_5 \left(\frac{2}{3}\right) \cdot \frac{1}{\sqrt{3}}$$

$$70.[1] \frac{dB}{dt} = \lambda B \Rightarrow \int_{1000}^{1200} \frac{dB}{B} = \lambda \int_0^2 dt \Rightarrow \lambda = \frac{1}{2} \ln\left(\frac{6}{5}\right)$$

$$\int_{1000}^{2000} \frac{dB}{B} = \frac{1}{2} \ln\left(\frac{6}{5}\right) \int_0^T dt \Rightarrow T = \frac{2 \ln 2}{\ln\left(\frac{6}{5}\right)}$$

$$= k = 2 \ln 2$$

71.[3] A(1, 5, 35), B(7, 5, 5), C(1, λ , 7), D(2λ , 1, 2)

$$\overline{AB} = 6\hat{i} - 30\hat{k}, \overline{BC} = -6\hat{i} (\lambda - 5)\hat{j} + 2\hat{k}$$

$$\overline{CD} = (2\lambda - 1)\hat{i} + (1 - \lambda)\hat{j} - 5\hat{k}$$

Points are coplanar

$$\Rightarrow 0 = \begin{vmatrix} 6 & 0 & -30 \\ -6 & \lambda - 5 & 2 \\ 2\lambda - 1 & 1 - \lambda & -5 \end{vmatrix}$$

$$= 6(-5\lambda + 25 - 2 + 2\lambda) - 30(-6 + 6\lambda - (2\lambda^2 - \lambda - 10\lambda + 5))$$

$$= 6(-3\lambda + 23) - 30(-2\lambda^2 + 11\lambda - 5 - 6 + 6\lambda)$$

$$= 6(-3\lambda + 23) - 30(-2\lambda^2 + 17\lambda - 11)$$

$$= 6(-3\lambda + 23 + 10\lambda^2 - 85\lambda + 55)$$

$$= 6(10\lambda^2 - 88\lambda + 78) = 12(5\lambda^2 - 44\lambda + 39)$$

$$\Rightarrow 0 = 12(5\lambda^2 - 44\lambda + 39)$$

$$\lambda_1 + \lambda_2 = \frac{44}{5}$$

$$72.[3] \frac{\sin^{-1} x}{r} = a, \frac{\cos^{-1} x}{r} = b, \frac{\tan^{-1} y}{r} = c$$

$$\text{So, } a + b = \frac{\pi}{2r}$$

$$\cos\left(\frac{\pi c}{a + b}\right) = \cos\left(\frac{\pi \tan^{-1} y}{\frac{\pi}{2r}}\right)$$

$$= \cos(2 \tan^{-1} y), \text{ let } \tan^{-1} y = \theta$$

$$= \cos(2\theta)$$

$$= \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta} = \frac{1 - y^2}{1 + y^2}$$

73.[3] (I) First possibility is 1, 1, 1, 1, 2, 3

$$\text{required number} = \frac{7!}{5!} = 7 \times 6 = 42$$

(II) Second possibility is 1, 1, 1, 1, 2, 2, 2

$$\text{required number} = \frac{7!}{4! 3!} = \frac{7 \times 6 \times 5}{6} = 35$$

$$\text{Total} = 42 + 35 = 77$$

$$74.[4] \left| \frac{f(x) - f(y)}{(x - y)} \right| \leq |x - y|$$

$$x - y = h \text{ let } \Rightarrow x = y + h$$

$$\lim_{x \rightarrow 0} \left| \frac{f(y + h) - f(y)}{h} \right| \leq 0$$

$$\Rightarrow |f'(y)| \leq 0 \Rightarrow f'(y) = 0$$

$$\Rightarrow f(y) = k \text{ (constant)}$$

$$\text{and } f(0) = 1 \text{ given}$$

$$\text{So, } f(y) = 1 \Rightarrow f(x) = 1$$

$$75. [1] \frac{dy}{dx} = 2x^3 - 15x^2 + 36x - 19$$

Since, slope is maximum so,

$$\frac{d^2y}{dx^2} = 6x^2 - 30x + 36 = 0$$

$$\Rightarrow x^2 - 5x + 6 = 0 \quad \left| \quad \frac{d^2y}{dx^3} = 12x - 30 \right.$$

$$x = 2, 3 \quad \left| \quad \text{at } x = 2, \frac{d^2y}{dx^3} < 0 \right.$$

So, maxima

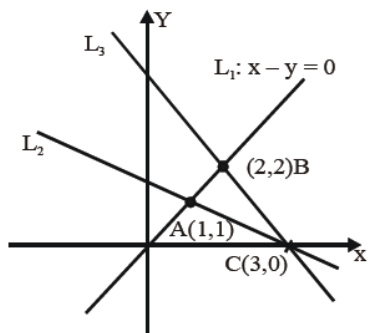
$$\text{at } x = 2$$

$$y = \frac{1}{2} \times 16 - 5 \times 8 + 18 \times 4 - 19 \times 2$$

$$= 8 - 40 + 72 - 38 = 80 - 78 = 2$$

point (2, 2)

76.[3]



$$L_1 : x - y = 0$$

$$L_2 : x + 2y = 3$$

$$L_3 : x + y = 6$$

on solving L_1 and L_2 :

$$y = L \text{ and } x = 1$$

L_1 and L_3 :

$$x = 2$$

$$y = 2$$

L_2 and L_3 :

$$x + y = 3$$

$$2x + y = 6$$

$$x = 3$$

$$y = 0$$

$$AC = \sqrt{4+1} = \sqrt{5}$$

$$BC = \sqrt{4+1} = \sqrt{5}$$

$$AB = \sqrt{1+1} = \sqrt{2}$$

so its an isosceles triangle

77. [2] $P_1 : x + 5y + 7z = 3,$

$P_2 : x - 3y - z = 5$

$P_3 : x + 5y + 7z = \frac{5}{2}$

so P_1 and P_3 are parallel.

78. [2] $R_2 \rightarrow R_2 - R_1$ and $R_3 \rightarrow R_3 - R_1$

$$\Delta = \begin{vmatrix} (a+1)(a+2) & a+2 & 1 \\ (a+2)(a+3-a-1) & 1 & 0 \\ a^2+7a+12-a^2-3a-2 & 2 & 0 \end{vmatrix}$$

$$= \begin{vmatrix} a^2+3a+2 & a+2 & 1 \\ 2(a+2) & 1 & 0 \\ 4a+10 & 2 & 0 \end{vmatrix}$$

$$= 4(a+2) - 4a - 10$$

$$= 4a + 8 - 4a - 10 = -2$$

79. [1] $I = \int_{-\pi/2}^{\pi/2} \frac{\cos^2 x}{1+3^x} dx$ (using king)

$$I = \int_{-\pi/2}^{\pi/2} \frac{\cos^2 x}{1+3^{-x}} dx = \int_{-\pi/2}^{\pi/2} \frac{3^x \cos^2 x}{1+3^x} dx$$

$$2I = \int_{-\pi/2}^{\pi/2} \frac{(1+3^x)\cos^2 x}{1+3^x} dx$$

$$= \int_{-\pi/2}^{\pi/2} \cos^2 x dx = 2 \int_0^{\pi/2} \cos^2 x dx$$

$$\Rightarrow I = \int_0^{\pi/2} \cos^2 x dx = \frac{\pi}{4}$$

80. [4] Equivalence class of $(1, -1)$ is a circle with centre at $(0,0)$ and radius = 2

$$\Rightarrow x^2 + y^2 = 2$$

$$S = \{(x,y) | x^2 + y^2 = 2\}$$

81.[2] $y^2 = a \left(x + \frac{\sqrt{a}}{2} \right) = ax + \frac{a^{3/2}}{2}$ (1)

$$\Rightarrow 2yy' = a$$

put in equation (1)

$$y^2 = (2yy') x + \frac{(2yy')^{3/2}}{2}$$

$$(y^2 - 2xy y') = \frac{(2yy')^{3/2}}{2}$$

squaring

$$(y^2 - 2xy y')^2 = \frac{y^3 (y')^3}{2}$$

$$\therefore \text{order} = 1$$

$$\text{degree} = 3$$

$$\text{Degree} - \text{order} = 3 - 1 = 2$$

82.[3] $3 \sin x + 4 \cos x = k + 1$

$$\Rightarrow k + 1 \in \left[-\sqrt{3^2 + 4^2}, \sqrt{3^2 + 4^2} \right]$$

$$\Rightarrow k + 1 \in [-5, 5]$$

$$\Rightarrow k \in [-6, 4]$$

No. of integral value of $k = 11$

83.[1] $\log_4 (x - 1) = \log_2 (x - 3)$

$$\Rightarrow \frac{1}{2} \log_2 (x - 1) = \log_2 (x - 3)$$

$$\Rightarrow \log_2 (x - 1)^{1/2} = \log_2 (x - 3)$$

$$\Rightarrow (x - 1)^{1/2} = x - 3$$

$$\Rightarrow x - 1 = x^2 + 9 - 6x$$

$$\Rightarrow x^2 - 7x + 10 = 0$$

$$\Rightarrow (x-2)(x-5) = 0$$

$$\Rightarrow x = 2.5$$

But $x \neq 2$ because it is not satisfying the domain of given equation i.e $\log_2(x-3) \rightarrow$ its domain $x > 3$

finally x is 5

\therefore No. of solutions = 1

84.[3] $x^3 - 2x^2 + 2x - 1 = 0$

$x = 1$ satisfying the equation

$\therefore x - 1$ is factor of

$$x^3 - 2x^2 + 2x - 1$$

$$= (x-1)(x^2 - x + 1) = 0$$

$$x = 1, \frac{1+i\sqrt{3}}{2}, \frac{1-i\sqrt{3}}{2}$$

$$x = 1, -\omega^2, -\omega$$

sum of 162^{th} power of roots

$$= (1)^{162} + (-\omega^2)^{162} + (-\omega)^{162}$$

$$= 1 + (\omega)^{324} + (\omega)^{162}$$

$$= 1 + 1 + 1 = 3$$

85.[45] $30({}^{30}C_0) + 29({}^{30}C_1) + \dots + 2({}^{30}C_{28}) + 1({}^{30}C_{29})$
 $= 30({}^{30}C_{30}) + 29({}^{30}C_{29}) + \dots + 2({}^{30}C_2)$
 $+ 1({}^{30}C_1)$

$$= \sum_{r=1}^{30} r({}^{30}C_r) = \sum_{r=1}^{30} r \left(\frac{30}{r} \right) ({}^{29}C_{r-1})$$

$$= 30 \sum_{r=1}^{30} {}^{29}C_{r-1}$$

$$= 30({}^{29}C_0 + {}^{29}C_1 + {}^{29}C_2 + \dots + {}^{29}C_{29})$$

$$= 30(2^{29}) = 15(2)^{30} = n(2)^m$$

$$\therefore n = 15, m = 30$$

$$n + m = 45$$

86.[1] Put $e^{\sin y} = t$

$$\Rightarrow e^{\sin y} \cos y \frac{dy}{dx} = \frac{dt}{dx}$$

$$\Rightarrow \text{D.E is } \frac{dt}{dx} + t \cos x = \cos x$$

$$\text{I. F.} = e^{\int \cos x dx} = e^{\sin x}$$

$$\Rightarrow \text{solution is } t \cdot e^{\sin x} = \int \cos x e^{\sin x}$$

$$\Rightarrow e^{\sin y} e^{\sin x} = e^{\sin x} + c$$

$$\because x = 0, y = 0 \Rightarrow c = 0$$

$$\Rightarrow e^{\sin y} = 1$$

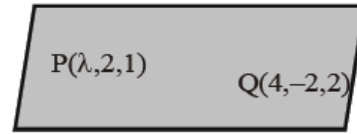
$$\Rightarrow y = 0$$

$$\Rightarrow 1 + y \left(\frac{\pi}{6} \right) + \frac{\sqrt{3}}{2} y \left(\frac{\pi}{3} \right) + \frac{1}{\sqrt{2}} y \left(\frac{\pi}{4} \right) = 1$$

87. [8]

$$A(-2, -21, 29)$$

$$B(-1, -16, 33)$$



$$\vec{AB} \cdot \vec{PQ} = 0$$

$$\Rightarrow (\hat{i} + 5\hat{j} - 6\hat{k}) \cdot ((4-\lambda)\hat{i} - 4\hat{j} + \hat{k}) = 0$$

$$\Rightarrow 4 - \lambda - 20 - 6 = 0$$

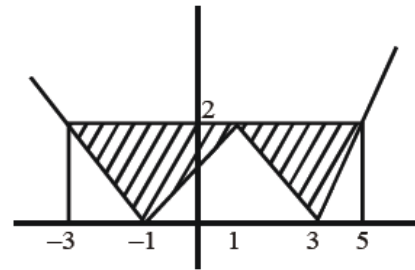
$$\Rightarrow \lambda = -22$$

$$\Rightarrow \left(\frac{\lambda}{11} \right)^2 - \frac{4\lambda}{11} - 4 = 4 + 8 - 4 = 8$$

88. [8] Remark :

Question is incomplete it should be area bounded

by $y = |x-1| - 2$ and $y = 2$



$$\text{Area} = 2 \left(\frac{1}{2} \cdot 4 \cdot 2 \right)$$

89.[2] Put $2x = t \Rightarrow 2dx = dt$

$$\Rightarrow I = \frac{1}{2} \int_0^{2\pi} |\sin t| dt$$

$$= \int_0^{\pi} |\sin t| dt$$

$$= 2$$

90.[1] $\sqrt{3}(\cos x)^2 - \sqrt{3} \cos x + \cos x - 1 = 0$

$$\Rightarrow (\sqrt{3} \cos x + 1)(\cos x - 1) = 0$$

$$\Rightarrow \cos x = 1 \text{ or } \cos x = -\frac{1}{\sqrt{3}} \text{ (reject)}$$

$$\Rightarrow x = 0 \text{ only}$$